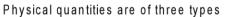
INFINITY NOTES ON UNITS & DIMENSIONS

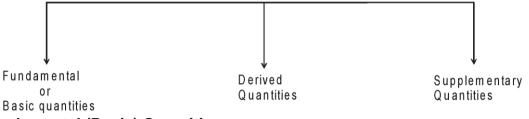
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1.

PHYSICAL QUANTITIES :

The quantities which can be measured by an instrument and by means of which we can describe the laws of physics are called physical quantities. Till class X we have studied many physical quantities eg. length, velocity, acceleration, force, time, pressure, mass, density etc.

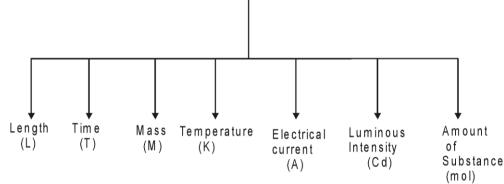




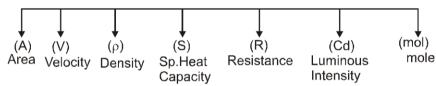
Fundamental (Basic) Quantities :

- These are the elementary quantities which covers the entire span of physics.
- Any other quantities can be derived from these.
- All the basic quantities are chosen such that they should be different, that means independent of each other. (i.e., distance (d), time (t) and velocity (v) cannot be chosen as basic quantities (because d

they are related as V = t). An International Organization named CGPM : General Conference on weight and Measures, chose seven physical quantities as basic or fundamental.

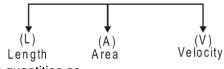


These are the elementary quantities (in our planet) that's why chosen as basic quantities. In fact any set of independent quantities can be chosen as basic quantities by which all other physical quantities can be derived. i.e.,



Can be chosen as basic quantities (on some other planet, these might also be used as basic quantities)





cannot be used as basic quantities as Area = $(Length)^2$ so they are not independent.

2. Derived Quantities :

Physical quantities which can be expressed in terms of basic quantities (M,L,T....) are called derived quantities.

i.e., Momentum P = mv

displacement ML

= (m) time = $T = M^1 L^1 T^{-1}$

Here [M¹L¹T⁻¹] is called dimensional formula of momentum, and we can say that momentum has 1 Dimension in M (mass)

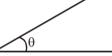
1 Dimension in L (length)

and -1 Dimension in T (time)

The representation of any quantity in terms of basic quantities (M, L, T....) is called dimensional formula and in the representation, the powers of the basic quantities are called dimensions.

3. Supplementary quantities :

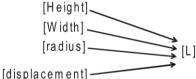
Besides seven fundamental quantities two supplementary quantities are also defined. They are



- Plane angle (The angle between two lines)
- Solid angle

II. FINDING DIMENSIONS OF VARIOUS PHYSICAL QUANTITIES :

• Height, width, radius, displacement etc. are a kind of length. So we can say that their dimension is [L]



here [Height] can be read as "Dimension of Height"

- Area = Length × Width
 - So, dimension of area is [Area] = [Length] × [Width] = $[L] \times [L] = [L^2]$

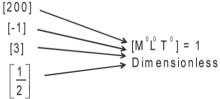
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For circle
Area = \pi r^2
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 $[Area] = [\pi] [r^2]$

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= [1] [L^2]
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 $= [L^2]$

Here π is not a kind of length or mass or time so π shouldn't affect the dimension of Area. Hence its dimension should be 1 (M⁰L⁰T⁰) and we can say that it is dimensionless. From similar logic we can say that all the numbers are dimensionless.



 [Volume] = [Length] × [Width] × [Height] = L × L × L= [L³] For sphere

Volume = $\frac{4}{3}\pi r^3$ [Volume] = $\begin{bmatrix} \frac{4}{3}\pi \end{bmatrix}$ [r³] = (1) [L³] = [L³] So dimension of volume will be alway

So dimension of volume will be always [L³] whether it is volume of a cuboid or volume of sphere.

<u>Dimension of a physical quantity will be same, it doesn't depend on which formula we are using</u> for that quantity.

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mass Density = volume [mass] Μ $[Density] = [volume] = \overline{L^3} = [M^1 L^{-3}]$ displacement time Velocity (v) =[Displacement] [time] $= \overline{\mathsf{T}} = [\mathsf{M}^{\mathsf{O}}\mathsf{L}^{\mathsf{1}}\mathsf{T}^{-\mathsf{1}}]$ [v] = dv Acceleration (a) = dt $\label{eq:alpha} [a] = \begin{tabular}{ll} \frac{dv \rightarrow kind \mbox{ of velocity}}{dt \rightarrow kind \mbox{ of time}} &= \begin{tabular}{ll} \frac{LT^{-1}}{T} = LT^{-2} \end{tabular}$ Momentum (P) = mv[P] = [M] [v]= [M] [LT⁻¹] $= [M^{1}L^{1}T^{-1}]$ Force (F) = ma[F] = [m] [a] $= [M] [LT^{-2}]$ = $[M^{1}L^{1}T^{-2}]$ (You should remember the dimensions of force because it is used several times) Work or Energy = force × displacement [Work] = [force] [displacement] $= [M^{1}L^{1}T^{-2}][L]$ $= [M^{1}L^{2}T^{-2}]$ work Power = time [work] $M^{1}L^{2}T^{-2}$ $[Power] = [time] = T = [M^{1}L^{2}T^{-3}]$ Force Pressure = Area $[Force] M^{1}L^{1}T^{-2}$ $[Pressure] = \frac{[Area]}{[Area]} = \frac{M^2 L^2}{L^2} = M^1 L^{-1} T^{-2}$ **Dimensions of angular quantities :** Angle (θ) • Arc (Angular displacement) $\theta = radius$ [Arc] $[\theta] = \frac{[\text{Arc}]}{[\text{radius}]} = \frac{L}{L} = [M^{0}L^{0}T^{0}] \text{ (Dimensionless)}$ Angular velocity (ω) = $\frac{\theta}{t}$; [ω] = $\frac{[\theta]}{[t]}$ = $\frac{1}{T}$ = [M^oL^oT⁻¹] Angular acceleration (α) = $\frac{d\omega}{dt}$; $[\alpha] = \frac{[d\omega]}{[dt]} = \frac{M^0 L^0 T^{-1}}{T} = [M^0 L^0 T^{-2}]$ Torque = Force × Arm length • [Torque] = [force] × [arm length] $= [M^{1}L^{1}T^{-2}] \times [L] = [M^{1}L^{2}T^{-2}]$ Physical Constants :

• Gravitational Constant :

If two bodies of mass m_1 and m_2 are placed at r distance, both feel gravitational attraction force, whose value is,

$$(m_1) \xrightarrow{F_g} (m_2)$$

Gravitational force Fg =

where G is a constant called Gravitational constant.

$$[F_{9}] = \frac{[G][m_{1}][m_{2}]}{[r^{2}]}$$
$$[M^{1}L^{1}T^{-2}] = \frac{[G][M][M]}{[L^{2}]}$$
$$[G] = M^{-1}L^{3}T^{-2}$$

• Specific heat capacity :

To increase the temperature of a body by ΔT , Heat required is $Q = ms \Delta T$ Here s is called specific heat capacity.

[Q] = [m] [s] [ΔT]

Here Q is heat : A kind of energy so $[Q] = M^{1}L^{2}T^{-2}$ $[M^{1}L^{2}T^{-2}] = [M] [s] [K]$ $[s] = [M^{0}L^{2}T^{-2}K^{-1}]$

Gas constant (R) :

For an ideal gas, relation between pressure (P) Value (V), Temperature (T) and moles of gas (n) is PV = nRT where R is a constant, called gas constant. [P] [V] = [n] [R] [T](1) $\frac{[Force]}{[Area]} \text{ [Area \times Length]} = [Force] \times [Length] = [M^{1}L^{1}T^{-2}] [L^{1}] = M^{1}L^{2}T^{-2}$ From equation (1) [P] [V] = [n] [R] [T] $\Rightarrow [M^{1}L^{2}T^{-2}] = [mol] [R] [K] \Rightarrow [R] = [M^{1}L^{2}T^{-2} \text{ mol}^{-1} \text{ K}^{-1}]$

• Coefficient of viscosity :

If any spherical ball of radius r moves with velocity v in a viscous liquid, then viscous force acting on it is given by ∇

 $F_v = 6\pi\eta rv$

Here $\boldsymbol{\eta}$ is coefficient of viscosity

$$\begin{bmatrix} F_v \end{bmatrix} = [6\pi] [\eta] [r] [v] \\ M^1 L^1 T^{-2} = (1) [\eta] [L] [LT^{-1}] \\ [\eta] = M^1 L^{-1} T^{-1}$$

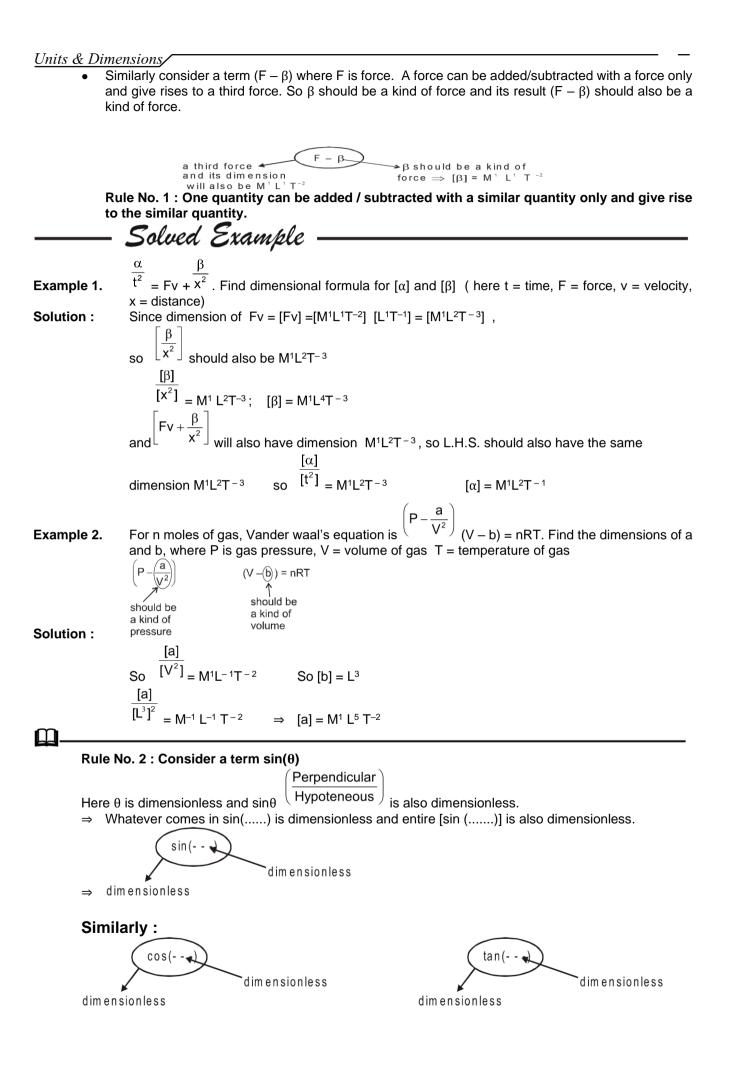
• Planck's constant :

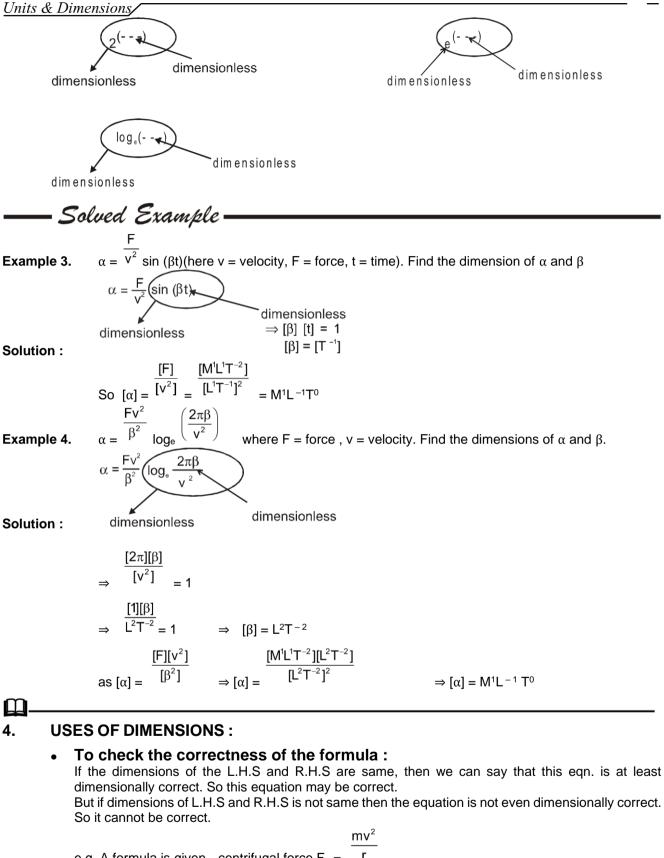
If light of frequency υ is falling , energy of a photon is given by

 $E = hv \qquad \text{Here } h = \text{Planck's constant}$ [E] = [h] [v] $v = \text{frequency} = \frac{1}{\text{Time Period}} \Rightarrow [v] = \frac{1}{[\text{Time Period}]} = \begin{bmatrix}\frac{1}{T}\\ \hline \end{bmatrix}$ so $M^{1}L^{2}T^{-2} = [h] [T^{-1}]$ $[h] = M^{1}L^{2}T^{-1}$

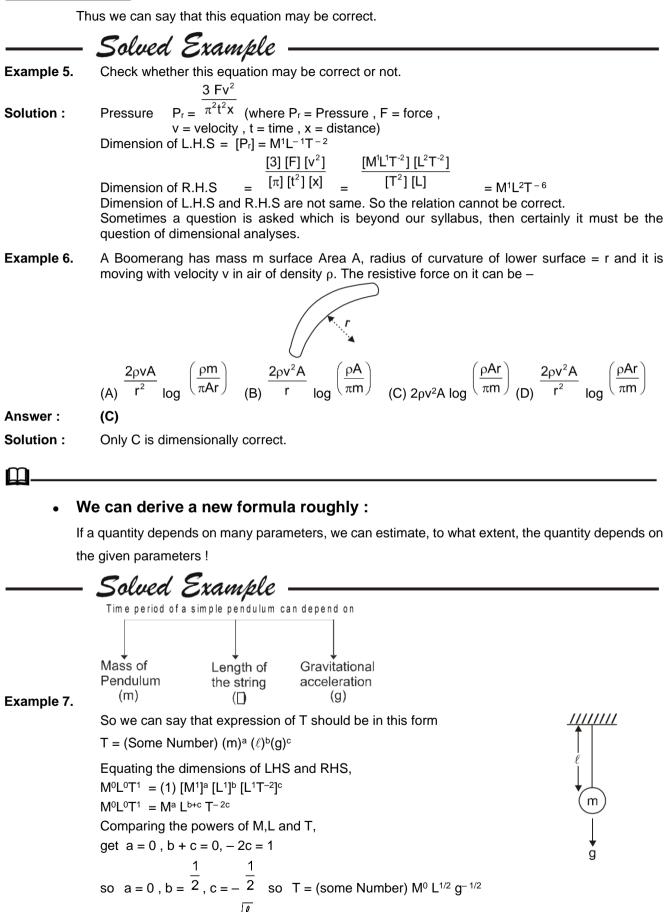
3. Some special features of dimensions :

Suppose in any formula, (L + α) term is coming (where L is length). As length can be added only with a length, so α should also be a kind of length.
 So [α] = [L]

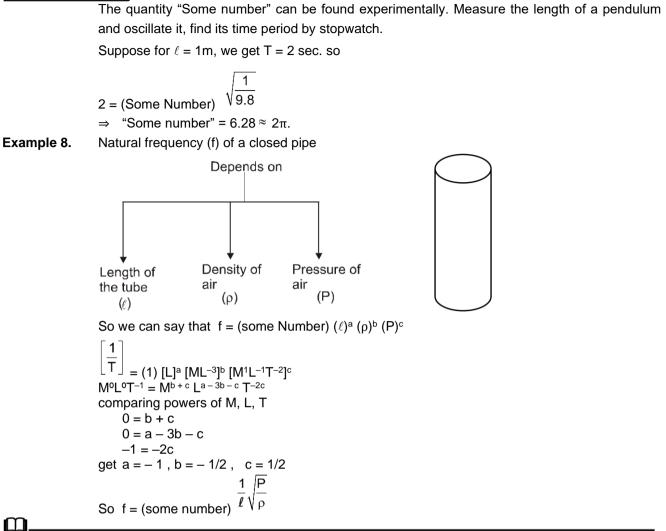




e.g. A formula is given centrifugal force $F_e = r$ (where m = mass , v = velocity , r = radius) we have to check whether it is correct or not. Dimension of L.H.S is $[F] = [M^1L^1T^{-2}]$ Dimension of R.H.S is $\frac{[m] [v^2]}{[r]} = \frac{[M] [LT^{-1}]^2}{[L]} = [M^1L^1T^{-2}]$ So this eqn. is at least dimensionally correct.



T = (Some Number)



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We can express any quantity in terms of the given basic quantities.

Solved Example

Example 9. If velocity (V), force (F) and time (T) are chosen as fundamental quantities, express (i) mass and (ii) energy in terms of V,F and T Solution : Let M = (some Number) $(V)^{a}(F)^{b}(T)^{c}$ Equating dimensions of both the sides $M^{1}L^{0}T^{0} = (1) [L^{1}T^{-1}]^{a} [M^{1}L^{1}T^{-2}]^{b} [T^{1}]^{c}$ $M^{1}L^{0}T^{0} = M^{b}L^{a+b}T^{-a-2b+c}$ get a = -1, b = 1, c = 1M = (Some Number) (V⁻¹ F¹ T¹) \Rightarrow $[M] = [V^{-1} F^1 T^1]$ Similarly we can also express energy in terms of V, F, T Let [E] = [some Number] [V]^a [F]^b [T]^c $[ML^{2}T^{-2}] = [M^{0}L^{0}T^{0}] [LT^{-1}]^{a} [MLT^{-2}]^{b} [T]^{c}$ ⇒ $[M^{1}L^{2}T^{-2}] = [M^{b} L^{a+b} T^{-a-2b+c}]$ ⇒ 1 = b; 2 = a + b; -2 = -a - 2b + c⇒ get a =1 ; b = 1 ; c = 1 : $E = (\text{some Number}) V^1 F^1 T^1 \text{ or } [E] = [V^1][F^1][T^1].$

To find out unit of a physical quantity :

Suppose we want to find the unit of force. We have studied that the dimension of force is $[Force] = [M^1L^1T^{-2}]$

As unit of M is kilogram (kg) , unit of L is meter (m) and unit of T is second (s) so unit of force can be written as $(kg)^1 (m)^1 (s)^{-2} = kg m/s^2$ in MKS system. In CGS system, unit of force can be written as $(g)^1 (cm)^1 (s)^{-2} = g cm/s^2$.

T = (Some Number)

III. LIMITATIONS OF DIMENSIONAL ANALYSIS :

From Dimensional analysis we get so the expression of T can be

$$T = 2\sqrt{\frac{\ell}{g}}$$

$$T = \sqrt{\frac{\ell}{g}} \sin(\dots)$$
or
$$T = 50\sqrt{\frac{\ell}{g}}$$

$$T = \sqrt{\frac{\ell}{g}} \log(\dots)$$
or
$$T = 2\pi\sqrt{\frac{\ell}{g}}$$

$$T = \sqrt{\frac{\ell}{g}} + (t_0)$$

- Dimensional analysis doesn't give information about the "some Number": The dimensional constant.
- This method is useful only when a physical quantity depends on other quantities by multiplication and power relations.

(i.e., $f = x^{a} y^{b} z^{c}$)

It fails if a physical quantity depends on sum or difference of two quantities

$$(i.e.f = x + y - z)$$

i.e., we cannot get the relation

 $S = ut + \frac{1}{2}at^2$ from dimensional analysis.

- This method will not work if a quantity depends on another quantity as sine or cosine, logarithmic or exponential relation. The method works only if the dependence is by power functions.
- We equate the powers of M,L and T hence we get only three equations. So we can have only three variable (only three dependent quantities)

So dimensional analysis will work only if the quantity depends only on three parameters, not more than that.

Example 10. Solution :

Can Pressure (P), density (ρ) and velocity (v) be taken as fundamental quantities ? P, ρ and v are not independent, they can be related as P = ρv^2 , so they cannot be taken as fundamental variables.

To check whether the 'P', ' ρ ', and 'V' are dependent or not, we can also use the following mathematical method :

 $[P] = [M^{1}L^{-1}T^{-2}] \\ [\rho] = [M^{1}L^{-3}T^{0}] \\ [V] = [M^{0}L^{1}T^{-1}]$

Check the determinant of their powers :

$$\begin{vmatrix} 1 & -1 & -2 \\ 1 & -3 & 0 \\ 0 & 1 & -1 \end{vmatrix} = 1 (3) - (-1)(-1) - 2 (1) = 0,$$

So these three terms are dependent.

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DIMENSIONS BY SOME STANDARD FORMULAE :-

In many cases, dimensions of some standard expression are asked

e.g. find the dimension of $(\mu_0 \epsilon_0)$

for this, we can find dimensions of μ_0 and ϵ_0 , and multiply them, but it will be very lengthy process. Instead of this, we should just search a formula, where this term ($\mu_0\epsilon_0$) comes.

It comes in
$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$
 (where $c = speed of light)
$$\Rightarrow \mu_0 \epsilon_0 = \frac{1}{c^2}$$

$$[\mu_0 \epsilon_0] = \frac{1}{c^2} = \frac{1}{(L/T)^2} = L^{-2} T^2$$
Solued Example
Example 11. Find the dimensions of
(i) $\epsilon_0 E^2$ ($\epsilon_0 = permittivity$ in vacuum, $E = electric field$)
 $\frac{B^2}{\mu_0}$ (B = Magnetic field, $\mu_0 = magnetic permeability$)
(ii) $\frac{1}{\sqrt{LC}}$ (L = Inductance, C = Capacitance)
(iv) RC (R = Resistance, C = Capacitance)
(v) RC (R = Resistance, L = Inductance)
 $\frac{L}{R}$
(vi) \overline{B} (E = Electric field, B = Magnetic field)
(vii) $\overline{C\epsilon_0}$ (G = Universal Gravitational constant, $\epsilon_0 = permittivity$ in vacuum)
 $\frac{\Phi_0}{\Phi_m}$
(viii) $\frac{\Phi_0}{\Phi_m}$ (ϕ_e = Electrical flux; ϕ_m = Magnetic flux)
Solution : (i) Energy density = $[\epsilon_0 E^2]$
 $\left[\frac{1}{2}\epsilon_0 E^2\right]_{=} \frac{[mergy]}{[volume]} = \frac{ML^2T^{-2}}{L^3} = M^1L^{-1}T^{-2}$
(ii) $\frac{1}{2} \frac{B^2}{\mu_0} = Magnetic energy density$
 $\left[\frac{1}{2} \frac{B^2}{\mu_0}\right]_{=} [Magnetic Energy density]$
 $\left[\frac{B^2}{\mu_0}\right]_{=} \frac{[mergy]}{[volume]} = \frac{ML^2T^{-2}}{L^3} = M^{1}L^{-1}T^{-2}$$

(iii)
$$\overline{\sqrt{LC}} = \text{angular frequency of } L - C \text{ oscillation}$$

$$\begin{bmatrix} \frac{1}{\sqrt{LC}} \end{bmatrix}_{=} [\omega] = \frac{1}{T} = T^{-1}$$
(iv) RC = Time constant of RC circuit = a kind of time [RC] = [time] = T^1
(v) \overline{R} = Time constant of L – R circuit
 $\begin{bmatrix} L \\ \overline{R} \end{bmatrix}_{=} [time] = T^1$
(vi) magnetic force $F_m = qvB$, electric force $F_e = qE$
 $\Rightarrow [F_m] = [F_e] \Rightarrow [qvB] = [qE] \Rightarrow \begin{bmatrix} E \\ \overline{B} \end{bmatrix}_{=} [v] = LT^{-1}$
(vii) Gravitational force $F_g = \frac{Gm^2}{r^2}$, Electrostatic force $F_e = \frac{4\pi\epsilon_0}{r^2} \frac{q^2}{r^2}$
 $\begin{bmatrix} \frac{Gm^2}{r^2} \end{bmatrix}_{=} \begin{bmatrix} \frac{1}{4\pi\epsilon_0} & \frac{q^2}{r^2} \end{bmatrix}$; $[G\epsilon_0] = \begin{bmatrix} \frac{q^2}{m^2} \end{bmatrix}_{=} \begin{bmatrix} \frac{(it)^2}{m^2} \end{bmatrix}_{=A^2T^2M^{-2}}$
(viii) $\begin{bmatrix} \frac{\phi_e}{\phi_m} \end{bmatrix}_{=} \begin{bmatrix} ES \\ BS \end{bmatrix}_{=} \begin{bmatrix} E \\ B \end{bmatrix}_{=} [v]$ (from part (vi)) = LT^{-1}

Dimensions of quantities related to Electromagnetic and Heat (only for XII and XIII students)

(i) Charge (q) : We know that electrical current
$$i = \frac{dq}{dt} = \frac{a \text{ small charge flow}}{\text{small time interval}}$$

(i) Charge (q) : We know that electrical current $i = \frac{dq}{dt} = \frac{a \text{ small charge flow}}{\text{small time interval}}$
(ii) $Permittivity in Vacuum (\epsilon_0)$: Electrostatic force between two charges $F_e = \frac{k}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r^2}$
(iii) Permittivity in Vacuum (ϵ_0) : Electrostatic force between two charges $F_e = \frac{k}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r^2}$
(iii) Electric Field (E) : Electrical force per unit charge $E = \frac{F}{q}$
(iii) Electrical Potential (V) : Electrical potential energy per unit charge $V = \frac{V}{q}$
(iv) Electrical Potential (V) : Electrical potential energy per unit charge $V = \frac{V}{q}$
(V) $= \begin{bmatrix} U \\ q \end{bmatrix} = \begin{bmatrix} M^{1/2}T^{-2} \\ (A^{1}T^{1}) \end{bmatrix} = M^{1}L^{2}T^{-3}A^{-1}$
(V) Resistance (R) : From Ohm's law $V = iR$
(V) $= [I][R]$
(M'L^{2}T^{-3}A^{-1}] = [A^{1}][R] ; (R] = M^{1}L^{2}T^{-3}A^{-2}

(vi) Capacitance (C) : C =
$$\frac{\mathbf{q}}{\mathbf{V}} \Rightarrow$$
 [C] = $\frac{\mathbf{q}}{\mathbf{V}} = \frac{\mathbf{q}}{\mathbf{M}^{1}\mathbf{L}^{2}\mathbf{T}^{-3}\mathbf{A}^{-1}}$]

 $\overline{[C]} = M^{-1}L^{-2}T^{4}A^{2}$ (vii) Magnetic field (B) : magnetic force on a current carrying wire $F_m = i \ell B \Rightarrow [F_m] = [i] [\ell] [B]$ $[M^{1}L^{1}T^{-2}] = [A^{1}][L^{1}][B]$ $[B] = M^{1}L^{0}T^{-2}A^{-1}$ F μ_o i₁i₂ (viii) Magnetic permeability in vacuum (μ_0) : Force/length between two wires $\overline{\ell} = 2\pi \overline{r}$ $M^{1}L^{1}T^{-2}$ [μ_O] [A][A] $L^1 = [2\pi]$ [L] \Rightarrow [μ_0] = M¹L¹T⁻² A⁻² (ix) Inductance (L) : Magnetic potential energy stored in an inductor U =1/2 L i² [U] = [1/2] [L] [i]² $[M^1 L^2 T^{-2}] = (1) [L] (A)^2$ $[L] = M^{1}L^{2}T^{-2}A^{-2}$ (x) Thermal Conductivity : Rate of heat flow through a conductor $\frac{dQ}{dt} = KA \left(\frac{dT}{dx}\right)$ [dQ] [dT] $r_{M} a_{1}^{1} 2 \tau - 2 \tau$ $[M^{1}L^{2}T^{-2}]$ [dT] [K] [dQ] $[T] = [K] [L^2] [L^1]$ [dt] = [k] [A] [dx] $[K] = M^{1}L^{1}T^{-3}K^{-1}$ (xi) Stefan's Constant (σ) : If a black body has temperature (T), then Rate of radiation energy emitted dE [dE] $dt = \sigma_A T^4 : [dt] = [\sigma]_{[A][T^4]}$ $[M^{1}L^{2}T^{-2}]$ $= \begin{bmatrix} \sigma \end{bmatrix} \begin{bmatrix} L^2 \end{bmatrix} \begin{bmatrix} K^4 \end{bmatrix} : \begin{bmatrix} \sigma \end{bmatrix} = \begin{bmatrix} M^1 L^0 T^{-3} K^{-4} \end{bmatrix}$ [T] (xii) Wien's Constant : Wavelength corresponding to max. spectral intensity. $\lambda_m = T$ (where T = temp. of the black body) [b] [b] [L] = [K] $[\lambda_m] = [T]$: $[b] = [L^1 K^1]$ UNIT Unit: Measurement of any physical quantity is expressed in terms of an internationally accepted certain basic standard called unit.

- **SI Units :** In 1971, an international Organization "CGPM" : (General Conference on weight and Measure) decided the standard units, which are internationally accepted. These units are called SI units (International system of units)
- 1. SI Units of Basic Quantities :

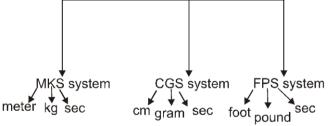
Base Quantity	SI Units				
Dase quantity	Name	Symbol	Definition		
Length	metre	m	The metre is the length of the path traveled by light in vacuum during a time interval of 1/299, 792, 458 of a second (1983)		
Mass	kilogram	kg	The kilogram is equal to the mass of the international prototype of the kilogram (a platinum-iridium alloy cylinder) kept at International Bureau of Weights and Measures, at Sevres, near Paris, France. (1889)		
Time	second	s	The second is the duration of 9, 192, 631, 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the cesium-133 atom (1967)		
Electric Current	ampere	A	The ampere is that constant current which, if maintained in two straight parallel conductors of infinite length, of negligible circular cross-section, and placed 1 metre apart in vacuum, will produce between these conductors a force equal to 2×10^{-7} Newton per metre of length. (1948)		
Thermodynamic Temperature	kel∨in	к	The kelvin, is the fraction 1/273.16 of the thermodynam temperature of the triple point of water. (1967)		
Amount of Substance	mole	mol	The mole is the amount of substance of a system, which contains as many elementary entities as there are atoms in 0.012 kilogram of carbon-12. (1971)		
Luminous Intensity	candela	cd	The candela is the luminous intensity, in a given direction, of a source that emits monochromatic radiation of frequency 540×10^{12} hertz and that has a radiant intensity in that direction of 1/683 watt per steradian (1979).		

2. Two supplementary units were also defined :

- Plane angle Unit = radian (rad)
- Solid angle Unit = Steradian (sr)

3. Other classification :

If a quantity involves only length, mass and time (quantities in mechanics), then its unit can be written in MKS, CGS or FPS system.



• For MKS system :

In this system Length, mass and time are expressed in meter, kg and second. respectively. It comes under SI system.

• For CGS system :

4.

In this system, Length, mass and time are expressed in cm, gram and second. respectively.

• For FPS system : In this system, length, mass and time are measured in foot, pound and second. respectively.

SI units of derived Quantities :

displacement (metre)

Velocity = time (second) So unit of velocity will be m/s

- change in velocity m/s m
- Acceleration = $time = s = s^2$
- Momentum = mv, so unit of momentum will be = (kg) (m/s) = kg m/s
- Force = ma, Unit will be = $(kg) \times (m/s^2) = kg m/s^2$ called newton (N)
- Work = FS, unit = (N) × (m) = N m called joule (J) work
- Power = ^{time}, Unit = J / s called watt (W)

5. Units of some physical Constants :

• Unit of "Universal Gravitational Constant" (G)

$$F = \frac{G(m_1)(m_2)}{r^2} \implies \frac{kg \times m}{s^2} = \frac{G(kg)(kg)}{m^2} \text{ so unit of } G = \frac{m^3}{kg s^2}$$

- Unit of specific heat capacity (s) : $Q = ms \Delta T$; J = (kg) (S) (K), Unit of s = J / kg K
 - $F \mu_0 i_1 i_2$

• Unit of μ_0 : force per unit length between two long parallel wires is: $\overline{\ell} = \overline{2\pi} \frac{1}{r}$

$$\frac{N}{m} = \frac{\mu_0}{(1)} \frac{(A)(A)}{(m)}$$
 Unit of $\mu_0 = \frac{N}{A^2}$

6. SI Prefix : Suppose distance between kota to Jaipur is 3000 m. so

$$= 3 \times 1000 \text{ m}$$

kilo(k)

d = 3000 m $k^{i|0}(k)$ = 3 km (here 'k' is the prefix used for 1000 (10³))

Suppose thickness of a wire is 0.05 m

$$= 5 \times 10^{-2} \text{ m}$$

d = 0.05 m centi(c)

= 5 cm (here 'c' is the prefix used for (10^{-2}))

Similarly, the magnitude of physical quantities vary over a wide range. So in order to express the very large magnitude as well as very small magnitude more compactly, "CGPM" recommended some standard prefixes for certain power of 10.

Power of 10	Prefix	Symbol	Power of 10	Prefix	Symbol
10 ¹⁸	exa	E	10 ⁻¹	deci	d
10 ¹⁵	peta	Р	10 ⁻²	centi	с
10 ¹²	tera	Т	10 ⁻³	milli	m
10 ⁹	giga	G	10 ⁻⁶	micro	μ
10 ⁶	mega	М	10 ⁻⁹	nano	n
10 ³	kilo	K	10 ⁻¹²	pico	р
10 ²	hecto	h	10 ⁻¹⁵	femto	f
10 ¹	deca	da	10 ⁻¹⁸	atto	а

Solved Example

Example 12.	Convert all in me	ters (m) :			
	(i) 5 μm.	(ii) 3 km	(iii) 20 mm	(iv) 73 pm	(v) 7.5 nm
Solution :	(i) $5 \mu m = 5 \times 10^{-10}$ (ii) $3 km = 3 \times 10^{-10}$ (iii) $20 mm = 20 \times 10^{-10}$ (iv) $73 pm = 73 \times 10^{-10}$ (v) $7.5 nm = 7.5^{-10}$	0 ³ m × 10 ^{−3} m ×10 ^{−12} m			
Example 13.	F = 5 N convert in $\underline{kg \times m}$	(10 ³ g)(100 cm)	g cm		
Solution :	$F = 5 s^2 = (5)$	s ² =	5×10^{5} s ² (in CGS	S system).	

	<u>g cm</u>
	This unit (s ²) is also called dyne
	m ³
	G = 6.67 × 10 ⁻¹¹ $\overline{\text{kg s}^2}$ convert it into CGS system.
	m^3 (100 cm) ³ cm ³
Solution :	$G = 6.67 \times 10^{-11} \frac{m^3}{kg s^2} = (6.67 \times 10^{-11}) \frac{(100 \text{ cm})^3}{(1000g)s^2} = 6.67 \times 10^{-8} \frac{\text{cm}^3}{\text{gs}^2}$
Example 15.	ρ = 2 g/cm ³ convert it into MKS system.
	10^{-3} kg
Solution :	$\rho = 2 \text{ g/cm}^3 = (2) \frac{10^{-3} \text{ kg}}{(10^{-2} \text{m})^3}$ $= 2 \times 10^3 \text{ kg/m}^3$
	$= 2 \times 10^3 \text{ kg/m}^3$
Example 16.	V = 90 km/hour convert it into m/s.
	(1000 m)
Solution :	$V = 90 \text{ km/hour} = (90) \overline{(60 \times 60 \text{ second})}$
	V = (90) $\left(\frac{1000}{3600}\right) \frac{m}{s}$
	<u> 5 m</u>
	$V = 90 \times \frac{18}{5}$
	V = 25 m/s
m	

POINT TO REMEMBER : 7.

To convert km/hour into m/sec, multiply by $\frac{1}{18}$.

Solved Example

Example 17. Convert 7 pm into µm. Let 7 pm = (x) μ m, Now lets convert both LHS & RHS into meter Solution : $7 \times (10^{-12})m = (x) \times 10^{-6} m$ get $x = 7 \times 10^{-6}$ So 7 pm = $(7 \times 10^{-6}) \mu m$ Some SI units of derived quantities are named after the scientist, who has contributed in that field a lot. \square

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8. SI Derived units, named after the scientist :

S.N Physical Quantity		SI Units					
		Unit name	Symbol of the unit	Expression in terms of other units	Expression in terms of base units		
1.	Frequency (f = $\frac{1}{T}$)	hertz	Hz	Oscillation s	s ⁻¹		
2.	Force (F = ma)	newton	N		Kg m / s²		
3.	Energy, Work, Heat (W = Fs)	joule	J	Nm	Kg m² / s²		
4.	Pressure, stress $(P = \frac{F}{A})$	pascal	Pa	N / m ²	Kg/m s²		
5.	Power, (Power = W)	watt	W	J/s	Kg m² / s³		
6.	Electric charge (q = it)	coulomb	С		As		
7.	Electric Potential Emf. (V = <mark>U</mark>)	volt	V	J/C	Kg m² / s³ A		
8.	Capacitance (C = $\frac{q}{v}$)	farad	F	C/V	A ² s ⁴ / kgm ²		
9.	Electrical Resistance (V = i R)	ohm	Ω	V / A	kg m² / s³ A²		
10.	Electrical Conductance (C = $\frac{1}{R} = \frac{i}{V}$)	siemens (mho)	s, 7	A/V	s ³ A ² / kg m ²		
11.	Magnetic field	tesla	Т	Wb/m²	Kg / s² A ¹		
12.	Magn etic flux	weber	Wb	V s or J/A	kg m²/s² A ¹		
13.	Inductance	henry	Н	Wb/A	kg m² / s² A²		
14.	Activity of radioactive material	becquerel	Bq	Disintegration second	s ⁻¹		

9. Some SI units expressed in terms of the special names and also in terms of base units:

	SI Units			
Physical Quantity	In terms of special names	In terms of base units		
Torque ($\tau = Fr$)	N m	Kg m 2 / s 2		
Dynamic Viscosity ($F_v = \eta A \frac{dv}{dr}$)	Poiseiulle (P□) or Pa s	Kg / m s		
Impulse (J = F Δt)	Ns	Kg m / s		
Modulus of elasticity (Y = $\frac{stress}{strain}$)	N / m ²	Kg / m s²		
Surface Tension Constant (T) $(T = \frac{F}{\Box})$	N/m or J/m ²	Kg / s ²		
Specific Heat capacity (s) (Q = ms∆ T)	J/kg K (old unit s <mark>cal</mark>)	$m^2 s^{-2} \kappa^{-1}$		
Thermal conductivity (K) $\left(\frac{dQ}{dt} = KA \frac{dT}{dr}\right)$	W / m K	m kg s⁻³ Ƙ¹		
Electric field Intensity E = $\frac{F}{q}$	V/m or N/C	m kg s ⁻³ A ⁻¹		
Gas constant (R) (PV = nRT) or molar Heat Capacity (C = $\frac{Q}{M\Delta T}$)	J / K mol	m² kg s -² K⁻¹ mol⁻¹		

10. CHANGE OF NUMERICAL VALUE WITH THE CHANGE OF UNIT :

Suppose we have

l

= 7 cm
$$\frac{\text{If we convert}}{\text{it into metres, we get}} = \frac{7}{100}$$
 m

we can say that if the unit is increased to 100 times (cm \rightarrow m), 1 (_ 7)

$$\operatorname{mes}\left(7 \to \frac{7}{100}\right)$$

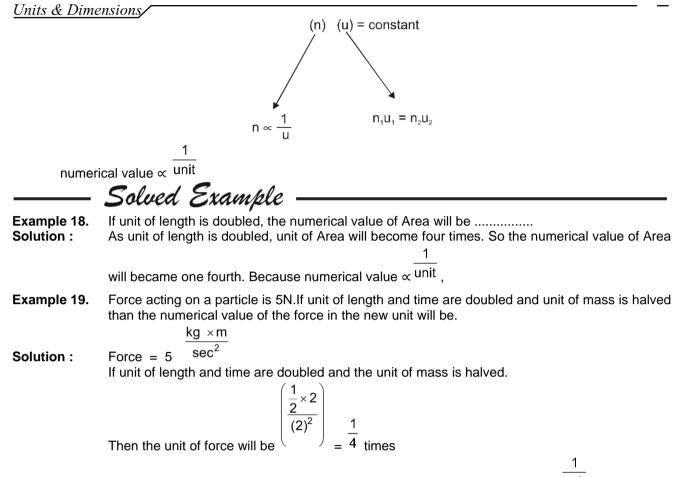
the numerical value became 100 till So we can say

Numerical value \propto unit

We can also tell it in a formal way like the following :

Magnitude of a physical quantity = (Its Numerical value) (unit) = (n) (u)

Magnitude of a physical quantity always remains constant, it will not change if we express it in some other unit. So



Hence the numerical value of the force will be 4 times. (as numerical value $\propto \overline{\text{unit}}$)