

20. Solid state

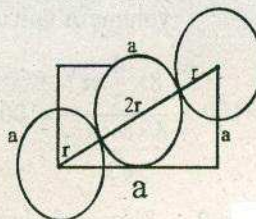
Q1.

Sol:

In FCC

$$4r = \sqrt{2}a$$

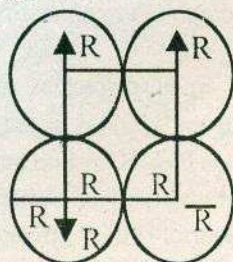
$$r = \frac{\sqrt{2}a}{4} = \frac{1.414 \times 0.574 \text{ nm}}{4} = 0.203 \text{ nm}$$



Smallest distance betⁿ two atoms = $2r = 0.406 \text{ nm}$ **Ans**

Q2.

Sol: Consider one face



To enclose all these spheres we have to increase the side length by $2R$

$$\therefore \text{new side length} = 2R + 2R = 4R$$

$$\therefore \text{Volume of such cube} = (4R)^3 = 64R^3 \quad \text{Ans}$$

$$\text{Volume of sphere} = 8 \times \frac{4}{3} \pi R^3$$

$$\% \text{ volume occupied by atom} = \frac{8 \times (4/3) \times \pi R^3}{64R^3} \times 100 = \frac{\pi}{6} \times 100 = 52.33\% \quad \text{Ans}$$

Q3.

Sol: $AC = \sqrt{2}AB$

$$4r = \sqrt{2} \times 3.61 \text{ \AA}$$

$$r = 1.276 \text{ \AA}$$

If r' is the size of small atom that perfectly fit then $2r + 2r' = BC$

$$2.5523 + 2r' = 3.61$$

$$2r' = 1.05773$$

$$r' = 0.528 \text{ \AA} \approx 0.53 \text{ \AA} \quad \text{Ans}$$

Q4.

Sol: $P.F = \frac{2 \times \frac{4}{3} \pi r^3}{\left(\frac{4}{\sqrt{3}}r\right)^3} = 0.68 \quad \text{Ans}$ (In BCC no. of effective atoms also $\sqrt{3}a = 4r \Rightarrow a = \frac{4r}{\sqrt{3}}$)

Q5.

Sol: % occupied space = $\frac{\text{Rank} \times \text{volume of each si atom}}{\text{volume of unit cell}} \times 100$

$$= \frac{8 \times \frac{4}{3} \pi r^3}{\left(\frac{8r}{\sqrt{3}}\right)^3} \times 100 = \frac{8 \times \frac{4}{3} \pi r^3}{\frac{8 \times 8 \times 8}{3\sqrt{3}} r^3} \times 100 = \frac{4\pi}{8 \times 8\sqrt{3}} \times 100 = \frac{3.14 \times 100}{16/\sqrt{3}} = 33.99\%$$

\therefore % vacant space = 100 - % occupied space
= (100 - 34) % = 66%

Ans

Q6.

Sol: P.F = $\frac{\text{Rank} \times \text{volume of each atom}}{\text{volume of unit cell}}$

$$P.F_{\text{BCC}} = \frac{2 \times \frac{4}{3} \pi r^3}{\left(\frac{4r}{\sqrt{3}}\right)^3} = 0.68 \quad (\text{In BCC } 4r = \sqrt{3}a)$$

Ans

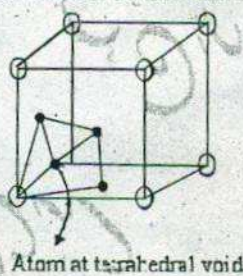
$$P.F_{\text{SCC}} = \frac{1 \times \frac{4}{3} \pi r^3}{(2r)^3} = 0.524 \quad (\because \text{in SCC } 2r = l)$$

Ans

Q7.

Sol: Diamond has FCC structure with a tetrahedron of atoms. This implies that carbon atom must be present at alternate tetrahedral voids of the FCC structure.

\therefore No. of effective atom in one unit cell



$$= 8 \times \frac{1}{8} + 6 \times \frac{1}{2} + \frac{1}{2} \times 8 = 8$$

Ans

↓ ↓ ↓
Corners face tetrahedral void
atoms atoms atoms

Q8.

Sol: Body centered like structure

In LiAg, the bigger atom will form the simple cubic unit cell & smaller atom will be at the centre of body. This type of structure is called body centred cubic like structure.

Q9.

Sol: No. of effective atoms of A in cubic C unit cell $= 8 \times \frac{1}{8} = 1$

No. of effective atoms of B in cubic unit cell $= 6 \times \frac{1}{2} = 3$

\therefore Molecular formula of the compound = AB_3 **Ans**

Q10.

Sol: Rank of Atom A $= \frac{1}{8} \times 8 = 1$

Rank of Atom B = 1

\therefore Molecular formula of the compound = AB

Q11.

Sol: In cubic closest packed structure

A is forming fcc structure, \Rightarrow Rank = 4 & so B must be present in tetrahedral void so that it can have rank of 8, so that molecular formula of AB_2 is possible.

Now co-ordination no. of B (atom in tetrahedral void) = 4 **Ans**

Because tetrahedral void is formed by 4 atom

Co-ordination no. of A = 8 **Ans**

Because any atom at corner contributed by 8 unit cell & so have 8 tetrahedral voids around it.

Q12.

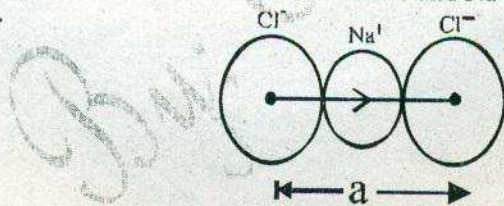
Sol: density $= \frac{\text{Rank} \times \text{Formula wt of NaCl}}{N_A \times \text{volume of unit cell}}$

Rank of NaCl structure = 4

Formula unit wt = $23 + 35.5 = 58.5$ g

Distance betⁿ Na^+ & Cl^- = 0.2819 nm.

In NaCl structure Cl^- form Fcc structure and Na^+ will be present in each octahedral void.



$a = 2$ (Distⁿ betⁿ Na^+ & Cl^-) = 2×0.2819 nm.

\therefore volume of cube = a^3

Density $= \frac{4 \times 58.5}{N_A \times (0.5638 \times 10^{-7} \text{ cm})^3}$

$2.165 \text{ g/cc} = \frac{4 \times 58.5}{N_A \times 0.179 \times 10^{-21}}$

$N_A = \frac{4 \times 58.5}{0.179 \times 2.165} \times 10^{21} = 6.023 \times 10^{23}$ **Ans**

For side length of 1 mole of cube

$$\therefore \text{density} = \frac{\text{mass of 1 moles}}{\text{volume of 1 mole}}$$

$$\text{Volume of 1 mole} = \frac{58.5 \text{ g}}{2.165} = 27.02 \text{ cm}^3$$

\therefore If the side length of cube containing 1 mole of substance.

$$a^3 = 27.02 \text{ cm}^3 \Rightarrow a = 3 \text{ cm} \quad \text{Ans}$$

No. of molecules in 1 mole of NaCl = 6.023×10^{23}

No. of ions in whole volume = $2 \times 6.023 \times 10^{23} = 1.2046 \times 10^{24}$

\therefore No of ions along are side = $(1.2046 \times 10^{24})^{1/3} = 1.064 \times 10^8$ ions **Ans**

Q13.

Sol: Volume of unit cell = $(3.803 \times 10^{-8} \text{ cm})^3 = 55.0 \times 10^{-24}$ ions **Ans**

Also no. of atoms of Rh present in unit cell = 4

$$\therefore \text{Volume / atom of Rh} = \frac{55.0 \times 10^{-24} \text{ cm}^3}{4} = 13.75 \times 10^{-24}$$

\therefore Volume of Avogadro no. of Rh = $13.75 \times 10^{-24} \times 6.023 \times 10^{23} = 8.282 \text{ cm}^3$ **Ans**

Q14.

Sol: At. Wt. of Pd = 106.4 g

$$R_{\text{Pd}} = 1.375 \text{ \AA}$$

In FCC structure, $\sqrt{2}a = 4r_{\text{Pd}}$

$$a = 2\sqrt{2} r_{\text{Pd}} = 2 \times 1.414 \times 1.375 \text{ \AA} = 3.88 \times 10^{-8} \text{ cm}$$

\therefore Volume = $(a)^3 = 58.795 \times 10^{-24} \text{ cm}^3$

$$\begin{aligned} \text{Density} &= \frac{\text{Rank} \times \text{At. wt. pd}}{6.023 \times 10^{23} \times \text{volume}} = \frac{4 \times 106.4}{6.023 \times 10^{23} \times 58.795 \times 10^{-24}} \\ &= 1.202 \times 10^1 = 12.02 \text{ gm/cm}^3 \quad \text{Ans} \end{aligned}$$

Q15.

Sol: Volume of FCC = $31.699 (\text{\AA})^3$

$$a^3 = 31.699 (\text{\AA})^3$$

$$a = 3.165 \text{ \AA}$$

Also in FCC = $\sqrt{2}a = 4r$

$$r = \frac{\sqrt{2}a}{4} = \frac{\sqrt{2} \times 3.165 \text{ \AA}}{4} = 1.1187 \text{ \AA} \quad \text{Ans}$$

\therefore Volume of 1 atom = $\frac{4}{3} \pi r^3 = \frac{4}{3} \times \pi \times (1.1187 \text{ \AA})^3 = 5.8675 (\text{\AA})^3$ **Ans**

Q16.

Sol: Density of Al should be given

Anyway density of Al is known from the periodic table with density mentioned in it

$$d_{\text{Al}} = 2.7 \text{ g/ml (must be given)}$$

$$\text{Rank Al} = 4$$

$$\text{At wt Al} = 27$$

$$\text{Volume of unit cell} = (4.094 \times 10^{-8} \text{ cm})^3$$

$$d_{\text{Al}} = \frac{4 \times 27}{N_A (4.094 \times 10^{-8})^3} \Rightarrow N_A = \frac{4 \times 27}{2.7 \times (4.094 \times 10^{-8})^3} = \frac{40 \times 10^{24}}{68.62}$$

$$N_A = 5.83 \times 10^{23} \quad \text{Ans}$$

Q17.

Sol: Specific gravity of metal = 10.2 at 25°C

$$d_{\text{metal}} = 10.2 \text{ g/cm}^3$$

Body centred structure with $a = 3.147 \text{ \AA}$

$$\text{Rank of BCC} = 2$$

$$d_{\text{metal}} = \frac{2 \times \text{At.wt}}{N_A \times (a)^3} = \frac{2 \times \text{At.wt}}{6.023 \times 10^{23} \times (3.147 \times 10^{-8} \text{ cm})^3}$$

$$\frac{10.2 \times 6.023 \times (3.147)^3 \times 10^{-1}}{2} = \text{At.wt}$$

$$\text{At wt of metal} = 95.7 \text{ gm} \quad \text{Ans}$$

Q18.

Sol: No. of molecules per unit cell in FCC = 4

$$\text{density} = 5.267 \text{ g/cc}$$

$$N_A = 6.023 \times 10^{23}$$

$$\text{Mol. wt (ZnSe)} = 144.4 \text{ gm}$$

$$\therefore \text{density} = \frac{\text{Rank} \times \text{mol.wt}}{6.023 \times 10^{23} \times a^3} \Rightarrow a^3 = \frac{4 \times 144.4 \text{ gm}}{6.023 \times 10^{23} \times 5.267}$$

$$\Rightarrow a = 5.661 \times 10^{-8} \text{ cm} = 5.667 \text{ \AA} \quad \text{Ans}$$

Q19.

$$\text{Sol: } d_{\text{fcc}} = \frac{4 \times 60}{6.023 \times 10^{23} \times (4 \times 10^{-8})^3} = 6.23 \text{ g/cc} \quad \text{Ans}$$

Q20.

$$\text{Sol: } d_{\text{po}} = \frac{\text{Rank} \times \text{At mass}}{N_A \times (a)^3}$$

$$91.5 \times 10^{-3} \text{ g/cc} = \frac{1 \times 209}{6.023 \times 10^{23} \times a^3}$$

$$a^3 = \frac{1 \times 209}{6.023 \times 10^{23} \times 91.5 \times 10^{-3}} = 3.79 \times 10^{-21}$$

$$a = 1.56 \times 10^{-7} \text{ cm} \quad \text{Ans}$$

Q21.

Sol: Let n is the no. of unit cell present in 50 gm of element

$$d_{\text{metal}} = \frac{\text{Rank} \times \text{At wt}}{N_A \times a^3} \Rightarrow 8.5 \text{ g/cc} = \frac{1 \times \text{At wt}}{6.023 \times 10^{23} \times (3 \times 10^{-8} \text{ cm})^3}$$

At wt = 138.23 g.

\therefore no. of unit cell in 138.23 gm = N_A

$$\therefore \frac{1}{138.23} \times N_A$$

$$\therefore \frac{50}{138.23} \times 6.023 \times 10^{23} = 2.178 \times 10^{23} \quad \text{Ans}$$

Q22.

Sol: $d_{hkl} = \frac{a}{\sqrt{h^2 + k^2 + l^2}}$

$$d_{111} = \frac{a}{\sqrt{1^2 + 1^2 + 1^2}} = 0.3079 \text{ nm}$$

$$a = 0.3079 \text{ nm} \times \sqrt{3} = 0.3079 \times 1.732 \text{ nm} = 0.5333 \text{ nm} \quad \text{Ans}$$

Q23.

Sol: For (a, b, c)

	x-axis	y-axis	z-axis
Intercepts	a	b	c
Wiess indices	$\frac{a}{a} = 1$	$\frac{b}{b} = 1$	$\frac{c}{c} = 1$
Miller indices	$\frac{1}{1} = 1$	$\frac{1}{1} = 1$	$\frac{1}{1} = 1$
\therefore Miller indices =	[1 1 1] Ans		

For (2a, b, c)

	x-axis	y-axis	z-axis
Intercepts	2a	b	c
Wiess indices	$\frac{2a}{a} = 2$	$\frac{b}{b} = 1$	$\frac{c}{c} = 1$
Reverse	$\frac{1}{2}$	$\frac{1}{1}$	$\frac{1}{1}$
Miller indices	$\frac{1}{2} \times 2 = 1$	$1 \times 2 = 2$	$1 \times 2 = 2$
Miller indices =	[1 2 2] Ans		

For (2a, -3b, -3c)

	x-axis	y-axis	z-axis
Intercepts	2a	-3b	-3c
Wiess indices	$\frac{2a}{a} = 2$	$\frac{-3b}{b} = -3$	$\frac{-3c}{c} = -3$
Reverse	$\frac{1}{2}$	$\frac{-1}{3}$	$-\frac{1}{3}$
Miller indices	$\frac{1}{2} \times 6 = 3$	$-\frac{1}{3} \times 6 = -2$	$-\frac{1}{3} \times 6 = -2$
\therefore Miller indices =	[3 $\bar{2}$ $\bar{2}$] Ans		

Q24.

Sol: $a = 3 \times 10^{-10} \text{ m}$

$$(a) d_{100} = \frac{a}{\sqrt{1^2 + 0^2 + 1^2}} = a = 3 \times 10^{-10}$$

Bragg's equation

$$2d \sin \theta = n\lambda, n = 1, 2, 3, \dots$$

For smallest diffraction angle, $n = 1$

$$\sin \theta = \frac{\lambda}{2d} = \frac{1.5 \times 10^{-10}}{2 \times 3 \times 10^{-10}} = \frac{1}{4} \Rightarrow \theta = \sin^{-1}\left(\frac{1}{4}\right) = 15.48^\circ \quad \text{Ans}$$

$$(b) d_{111} = \frac{1}{\sqrt{1^2 + 1^2 + 1^2}} = \frac{a}{\sqrt{3}} = \sqrt{3} \times 10^{-10} \text{ m} = 1.732 \times 10^{-10} \text{ m}$$

Bragg's equation

$$2d \sin \theta = n\lambda, n = 1, 2, 3, \dots$$

For smallest diffraction angle, $n = 1$

$$\sin \theta = \frac{\lambda}{2d} = \frac{1.5 \times 10^{-10} \text{ m}}{2 \times 1.732 \times 10^{-10} \text{ m}}$$

$$\sin \theta = 0.433 \Rightarrow \theta = \sin^{-1}(0.433) = 25.66^\circ \quad \text{Ans}$$

Q25.

Sol: BCC structure

$$d_K = 0.856 \times 10^3 \text{ kg/m}^3 = 0.856 \text{ g/cc}$$

$$d = \frac{2 \times 39}{6.023 \times 10^{23} \times a^3} \Rightarrow a^3 = \frac{2 \times 39}{6.023 \times 10^{23} \times 0.856} \text{ CC}$$

$$a = 5.334 \times 10^{-8} \text{ cm} = 5.334 \text{ \AA} = 533.4 \text{ pm} \quad \text{Ans}$$

$$d_{(2,0,0)} = \frac{a}{\sqrt{2^2 + 0^2 + 0^2}} = \frac{a}{2} = 266.7 \text{ pm}$$

$$d_{(1,1,0)} = \frac{a}{\sqrt{1^2 + 1^2 + 0^2}} = \frac{a}{\sqrt{2}} = \frac{533.4}{1.414} \text{ pm} = 377.1 \text{ pm} \quad \text{Ans}$$

$$d_{(2,2,2)} = \frac{a}{\sqrt{2^2 + 2^2 + 2^2}} = \frac{a}{2\sqrt{3}} = \frac{533.4}{2 \times 1.732} \text{ pm} = 154.0 \text{ pm} \quad \text{Ans}$$

Closest distance betⁿ atoms = $2r$

In BCC, $\sqrt{3}a = 4r$

$$2r = \frac{\sqrt{3}}{2} a = \frac{1.732}{2} \times 533.4 \text{ pm} = 461.8 \text{ pm} = 462 \text{ pm}$$

$$\text{Radius of K; } r = \frac{462}{2} \text{ pm} = 231 \text{ pm} \quad \text{Ans}$$

Q26.

Sol: $r_{\text{Na}^+} = 0.98 \times 10^{-10} \text{ m}$

$$r_{\text{Cl}^-} = 1.81 \times 10^{-10} \text{ m}$$

$$\text{radius ratio} = \frac{r_{\text{Na}^+}}{r_{\text{Cl}^-}} = \frac{0.98 \times 10^{-10} \text{ m}}{1.81 \times 10^{-10} \text{ m}}$$

Radius ratio = 0.5414 belongs to (0.414, 0.732)

In case of octahedral voids

Radius ratio lies between 0.414 to 0.732

so Na^+ will be present in Octahedral void.

\therefore Co-ordination no. of $\text{Na}^+ = 6$

Also co-ordination no. of $\text{Cl}^- = 6$ (6 Octahedral void around any Cl^- ion)

Q27.

Sol: CsCl has Body centered cubic structure in which Cl^- form simple cubic unit cell & Cs^+ ion will be present at body centered void.

In BCC void the radius ratio has range 0.732 to 0.999.

\therefore Critical / limiting radius ratio = 0.732 **Ans**

It can be calculated in this way

In simple cubic unit cell of Cl^-

$2r^- = a$ (a : side length of cube)

Also $2(r^+ + r^-) = \sqrt{3}a$

$$\frac{2(r^+ + r^-)}{2(r^-)} = \frac{\sqrt{3}a}{a} = \sqrt{3} \Rightarrow \frac{r^+ + r^-}{r^-} = \sqrt{3}$$

$$1 + \frac{r^+}{r^-} = \sqrt{3} \Rightarrow \frac{r^+}{r^-} = \sqrt{3} - 1 = 0.732 \quad \text{Ans}$$

Q28.

Sol: In CCP

$$\text{Packing fraction} = \frac{\text{total volume occupied by atoms}}{\text{Total volume of unit cell}} = \frac{4 \times \frac{4}{3} \pi r^3}{a^3}$$

$$\text{Also } \sqrt{2}a = 4r \Rightarrow a = 2\sqrt{2}r$$

$$\therefore \text{P.f.} = \frac{4 \times \frac{4}{3} \pi r^3}{(2\sqrt{2}r)^3} = \frac{16\pi}{3 \times 16\sqrt{2}} = \frac{\pi}{3\sqrt{2}} = 0.7406$$

$$\therefore \text{Void fraction} = 1 - \text{packing fraction} = 1 - 0.7406 = 0.2594 \quad \text{Ans}$$

$$\text{P.F.}_{\text{hcp}} = \frac{6 \times \frac{4}{3} \pi r^3}{24\sqrt{2}r^3} = \frac{\pi}{3\sqrt{2}} = 0.7406$$

$$\text{Volume of hcp} = 6 \times \frac{\sqrt{3}}{4} a^2 \times c = 6 \times \frac{\sqrt{3}}{4} \times (2r)^2 \times 4 \times \frac{\sqrt{2}}{3} r = 24\sqrt{2}r^3$$

$$\therefore \text{Void fraction} = 1 - \text{P.F.}_{\text{hcp}} = 1 - 0.7406 = 0.2594 \quad \text{Ans}$$

Q29.

$$\text{Sol: } d = \frac{\text{Rank} \times \text{Mol.wt}}{6.023 \times 10^{23} \times \text{volume}}$$

$$\Rightarrow 0.92 = \frac{\text{Rank} \times 18}{6.023 \times 10^{23} \times (a^2 \sin 60^\circ \times C)}$$

(angle given should be 60°)

$$\text{rank} = \frac{0.92 \times 6.023 \times 10^{23} \times (4.53 \times 10^{-8})^2 \times \frac{\sqrt{3}}{2} \times 7.41 \times 10^{-8}}{18}$$

$$\Rightarrow \text{Rank} = 4 \quad \text{Ans}$$

Q30.

$$\text{Sol: } r = 1.1 \text{ mm}; \quad h = 3.56 \text{ cm}; \quad P = 420 \text{ Pa} \quad \& \quad d(\text{CH}_3\text{COOH}) = 1.0492 \text{ g/cm}^3$$

From Laplace equation

$$y = \frac{r}{2}(P - h d g) = \frac{1.1 \times 10^{-3}}{2} (420 - 3.56 \times 10^{-2} \times 1.0492 \times 10^3 \times 9.8)$$

$$= \frac{1.1 \times 10^{-3}}{2} (420 - 366.045) = \frac{1.1 \times 10^{-3}}{2} \times 53.95 = 29.675 \times 10^{-3} = 2.967 \times 10^{-2} \text{ N/m} \quad \text{Ans}$$

Q31.

$$\text{Sol: } y = \frac{h d r g}{2 \cos \theta}$$

$$\therefore h = \frac{2 y \cos \theta}{d r g}$$

$$\text{For } \theta = 0, \quad y = 0.0284 \text{ N/m}, \quad d = 0.866 \text{ g/cc}, \quad g = 9.8 \text{ m/s}^2, \quad h = 2 \times 10^{-4} \text{ m.}$$

$$2 \times 10^{-4} = \frac{2 \times 2.84 \times 10^{-2}}{866 \times r \times 9.8} \Rightarrow r = 3.346 \times 10^{-2} \text{ m} \quad \text{Ans}$$

Q32.

$$\text{Sol: diameter of tube} = 1.0 \text{ mm}$$

$$\therefore r = 0.5 \text{ mm} = 0.5 \times 10^{-3} \text{ m}$$

$$\theta = 0$$

$$d_{\text{Hg}} = 13.6 \times 10^3 \text{ Kg/m}^3$$

$$\gamma = 4.6 \times 10^{-1} \text{ N/m.}$$

$$h = \frac{2\gamma}{\rho r g} = \frac{2 \times 4.6 \times 10^{-1}}{13.6 \times 10^3 \times 0.5 \times 10^{-3} \times 9.8} = 0.138 \times 10^{-1} = 1.38 \times 10^{-2} \text{ m} \quad \text{Ans}$$

Q33.

$$\text{Sol: } \frac{n_1}{n_2} = \frac{t_1(d_1 - d_0)d_1}{t_2(d_2 - d_0)d_0}$$

d_1 = density of metal ball

$$\frac{n_A}{n_B} = \frac{t_1(-d_1 + d_0)}{t_B(-d_E + d_0)}$$

$$\frac{n_A}{2.5 \text{ cp}} = \frac{5 (7.7 \times 10^3 - 1.5 \times 10^3)}{7.5 (7.8 \times 10^3 - 4.6 \times 10^3)}$$

$$n_A = \frac{2}{3} \times \frac{6.3}{3.2} \times 2.5 \text{ cp} = 3.28 \text{ Cp}$$

Ans

Q34.

Sol: $n = 1 \times 10^4 \text{ poise} = 10^3 \text{ N m}^{-2} \text{ s}$

$$d = 3.2 \text{ g / ml} = 3.2 \times 10^3 \text{ kg / m}^3$$

$$r = 2.5 \text{ mm} = 2.5 \times 10^{-3} \text{ m}$$

$$h = 1.0 \text{ cm} = 1 \times 10^{-2} \text{ m}$$

$$\rho_{\text{PO}} = 21.4 \text{ g / ml} = 21.4 \times 10^3 \text{ kg / m}^3$$

$$\eta = \frac{2r^2(d-d_0)g}{9u} = \frac{2r^2(d-d_0)g}{9x/t}$$

$$\eta = \frac{2r^2(d-d_0)g}{9x} t$$

$$1 \times 10 = \frac{2 \times (2.5 \times 10^{-3})^2 (2.4 \times 10^3 - 3.2 \times 10^3) 9.8 \times t}{9 \times 1 \times 10^2}$$

$$9 \times 10^{-1} = 2 \times (625 \times 10^{-6} \times 18.2 \times 10^3 \times 9.8)$$

$$t = \frac{9 \times 10^{-1}}{2 \times 6.25 \times 10^{-3} \times 9.8 \times 18.2} \Rightarrow t = \frac{9.00 \times 10^4}{2 \times 6.25 \times 9.8 \times 18.2} = 40.5 \text{ sec}$$

Ans

Q 35.

Sol: $h = \frac{2\gamma}{\rho g} \Rightarrow h_1 = \frac{2\gamma}{\rho r_1 g} \quad \& \quad h_2 = \frac{2\gamma}{\rho r_2 g}$

$$h_1 - h_2 = \frac{2\gamma}{\rho g} \left(\frac{1}{r_1} - \frac{1}{r_2} \right)$$

$$5.50 \times 10^{-2} = \frac{2\gamma}{1.41 \times 10^3 \times 9.8} \left(\frac{-10^{-4}}{2} + \frac{10^{-4}}{1} \right)$$

$$5.5 \times 10^{-2} = \frac{2\gamma}{1.41 \times 9.81 \times 10^3} \times \frac{10^7}{2}$$

$$\gamma = 5.6 \times 10^{-2} \times 1.41 \times 9.81 \times 10^7$$

$$= 7.74 \times 10^{-2} \text{ N/m} \quad \text{Ans}$$

Q 36.

Sol: $\frac{\gamma_1}{\gamma_2} = \frac{m_1}{m_2}$ (Since no. of droplets are same)

$$\frac{\gamma_1}{72.75} = \frac{0.852}{3.64} \Rightarrow \gamma_1 = \frac{0.852}{3.64} \times 72.75 \text{ dyne / cm}$$

$$\gamma_1 = 17.03 \text{ dyne / cm} \quad \text{Ans}$$

Q29.

Sol: $d = \frac{\text{Rank} \times \text{Mol.wt}}{6.023 \times 10^{23} \times \text{volume}}$

$$\Rightarrow 0.92 = \frac{\text{Rank} \times 18}{6.023 \times 10^{23} \times (a^2 \sin 60^\circ \times C)}$$

(angle given should be 60°)

$$\text{rank} = \frac{0.92 \times 6.023 \times 10^{23} \times (4.53 \times 10^{-8})^2 \times \frac{\sqrt{3}}{2} \times 7.41 \times 10^{-8}}{18}$$

$\Rightarrow \text{Rank} = 4$ Ans

Q30.

Sol: $r = 1.1 \text{ mm}$; $h = 3.56 \text{ cm}$; $P = 420 \text{ Pa}$ & $d(\text{CH}_3\text{COOH}) = 1.0492 \text{ g/cm}^3$

From Laplace equation

$$y = \frac{r}{2}(P - h d g) = \frac{1.1 \times 10^{-3}}{2}(420 - 3.56 \times 10^{-2} \times 1.0492 \times 10^3 \times 9.8)$$

$$= \frac{1.1 \times 10^{-3}}{2}(420 - 366.045) = \frac{1.1 \times 10^{-3}}{2} \times 53.95 = 29.675 \times 10^{-3} = 2.967 \times 10^{-2} \text{ N/m} \quad \text{Ans}$$

Q31.

Sol: $y = \frac{h d r g}{2 \cos \theta}$

$\therefore h = \frac{2 y \cos \theta}{d r g}$

For $\theta = 0$, $y = 0.0284 \text{ N/m}$, $d = 0.866 \text{ g/cc}$, $g = 9.8 \text{ m/s}^2$, $h = 2 \times 10^{-4} \text{ m}$.

$$2 \times 10^{-4} = \frac{2 \times 2.84 \times 10^{-2}}{866 \times r \times 9.8} \Rightarrow r = 3.346 \times 10^{-2} \text{ m} \quad \text{Ans}$$

Q32.

Sol: diameter of tube = 1.0 mm

$\therefore r = 0.5 \text{ mm} = 0.5 \times 10^{-3} \text{ m}$

$\theta = 0$

$d_{\text{Hg}} = 13.6 \times 10^3 \text{ Kg/m}^3$

$\gamma = 4.6 \times 10^{-1} \text{ N/m}$.

$$h = \frac{2\gamma}{\rho r g} = \frac{2 \times 4.6 \times 10^{-1}}{13.6 \times 10^3 \times 0.5 \times 10^{-3} \times 9.8} = 0.138 \times 10^{-1} = 1.38 \times 10^{-2} \text{ m} \quad \text{Ans}$$

Q33.

Sol: $\frac{n_1}{n_2} = \frac{t_1(d_1 - d_0)d_1}{t_2(d_2 - d_0)d_0}$

$d_1 = \text{density of metal ball}$

$$\frac{n_A}{n_B} = \frac{t_1(-d_1 + d_0)}{t_B(-d_E + d_0)}$$

$$\frac{n_A}{2.5 \text{ cp}} = \frac{5 (7.7 \times 10^3 - 1.5 \times 10^3)}{7.5 (7.8 \times 10^3 - 4.6 \times 10^3)}$$

$$n_A = \frac{2}{3} \times \frac{6.3}{3.2} \times 2.5 \text{ cp} = 3.28 \text{ Cp}$$

Ans

Q34.

Sol: $n = 1 \times 10^4 \text{ poise} = 10^3 \text{ N m}^{-2} \text{ s}$

$$d = 3.2 \text{ g / ml} = 3.2 \times 10^3 \text{ kg / m}^3$$

$$r = 2.5 \text{ mm} = 2.5 \times 10^{-3} \text{ m}$$

$$h = 1.0 \text{ cm} = 1 \times 10^{-2} \text{ m}$$

$$\rho_{\text{PO}} = 21.4 \text{ g / ml} = 21.4 \times 10^3 \text{ kg / m}^3$$

$$\eta = \frac{2r^2(d-d_0)g}{9u} = \frac{2r^2(d-d_0)g}{9x/t}$$

$$\eta = \frac{2r^2(d-d_0)g}{2x} t$$

$$1 \times 10 = \frac{2 \times (2.5 \times 10^{-3})^2 (2.4 \times 10^3 - 3.2 \times 10^3) 9.8 \times t}{9 \times 1 \times 10^2}$$

$$9 \times 10^{-1} = 2 \times (625 \times 10^{-6} \times 18.2 \times 10^3 \times 9.8)$$

$$t = \frac{9 \times 10^{-1}}{2 \times 6.25 \times 10^{-3} \times 9.8 \times 18.2} \Rightarrow t = \frac{9.00 \times 10^4}{2 \times 6.25 \times 9.8 \times 18.2} = 40.5 \text{ sec}$$

Ans

Q 35.

Sol: $h = \frac{2\gamma}{\rho g} \Rightarrow h_1 = \frac{2\gamma}{\rho r_1 g} \quad \& \quad h_2 = \frac{2\gamma}{\rho r_2 g}$

$$h_1 - h_2 = \frac{2\gamma}{\rho g} \left(\frac{1}{r_1} - \frac{1}{r_2} \right)$$

$$5.50 \times 10^{-2} = \frac{2\gamma}{1.41 \times 10^3 \times 9.8} \left(\frac{-10^{-4}}{2} + \frac{10^{-4}}{1} \right)$$

$$5.5 \times 10^{-2} = \frac{2\gamma}{1.41 \times 9.81 \times 10^3} \times \frac{10^7}{2}$$

$$\gamma = 5.6 \times 10^{-2} \times 1.41 \times 9.81 \times 10^7$$

$$= 7.74 \times 10^{-2} \text{ N/m} \quad \text{Ans}$$

Q 36.

Sol: $\frac{\gamma_1}{\gamma_2} = \frac{m_1}{m_2}$ (Since no. of droplets are same)

$$\frac{\gamma_1}{72.75} = \frac{0.852}{3.64} \Rightarrow \gamma_1 = \frac{0.852}{3.64} \times 72.75 \text{ dyne / cm}$$

$$\gamma_1 = 17.03 \text{ dyne / cm} \quad \text{Ans}$$

Q 37.

Sol: $n_w = 100$

$$n_0 = 280$$

$$\gamma_0 = ? \text{ If } Y_w = 0.07275 \text{ N/m}$$

$$d_w = 0.998 \times 10^3 \text{ kg/m}^3$$

$$d_0 = 0.755 \times 10^3 \text{ kg/m}^3$$

$$\frac{\gamma_0}{\gamma_w} = \frac{d_0}{d_w} \cdot \frac{n_w}{n_1}$$

$$\frac{\gamma_0}{0.07275} = \frac{0.755 \times 10^3}{0.998 \times 10^3} \times \frac{100}{280} \Rightarrow \gamma_0 = 0.019656 \text{ N/m} \quad \text{Ans}$$

Q38.

Sol: $n_0 = 0.084 \text{ N/m}^2$

$$d_0 = 1.1 \times 10^3 \text{ kg/m}^3$$

$$n_{H_2O} = 0.001101 \text{ N/m}^2$$

$$d_{H_2O} = 0.998 \times 10^3 \text{ kg/m}^3$$

$$\frac{n_1}{n_2} = \frac{t_1}{t_2} \times \frac{d_1}{d_2} \Rightarrow \frac{0.084}{0.00101} = \frac{t_0}{305} \times \frac{1.1 \times 10^3}{0.998 \times 10^3}$$

$$\frac{0.084}{0.00101} \times \frac{0.998}{1.1} \times 30 = t_0 \Rightarrow t_0 = 37 \text{ min } 43.7 \text{ sec} \quad \text{Ans}$$

Q39

Sol: $h = 1.0 \text{ cm}$

$$r = ?$$

If x- section is halved then r will be before $\frac{r}{\sqrt{2}}$

$$\therefore h = \frac{2\gamma}{\rho r g} \quad \therefore h \propto \frac{1}{r}$$

$$\therefore \frac{h_1}{h_2} = \frac{r_2}{r_1} = \frac{r/\sqrt{2}}{r}$$

$$\Rightarrow \frac{1.0}{h_2} = \frac{1}{\sqrt{2}} \Rightarrow h_2 = 1.0 \times \sqrt{2} \text{ cm} = 1.414 \text{ cm}$$

Objective Problems

Q1. Ans - (c)

Q2. Ans - (a) Crystalline solid has diffⁿ properties in different dirⁿ, so it is an anisotropic material.

Q3. Ans - (c)

Q4. Ans - (a)

Q5. Ans - (b) Total element of symmetry = $9 + 13 + 1 = 23$

Q6. Ans - (a) Primitive cubic unit cell

Body centred cubic unit cell

Face centred cubic unit cell

Q7. Ans - (a) Each Cl⁻ ion is surrounded by 6 octahedral voids in which Na⁺ ions are present

Q8. Ans - (a)

Q9. Ans - (b)

Q10. Ans - (b)

Q11. Ans - (c) In FCC, Rank = $8 \times \frac{1}{8} + \frac{1}{2} \times 6 = 1 + 3 = 4$

Q12. Ans - (c)

Q13. Ans - (b)

Q14. Ans (a) Rank of A = 1, Rank of B = $\frac{1}{8} \times 8 = 1$

Q15: Ans - (a)

Q16. Ans - (c) $\therefore 4r = \sqrt{3}a \Rightarrow r = \frac{\sqrt{3}a}{4}$ (in BCC)

Q17. Ans - (c) Volume of an atom = $\frac{4}{3}\pi r^3$

In simple cubic unit cell, no of atoms = 1

Also $a = 2r \Rightarrow r = \frac{a}{2}$

\Rightarrow volume of atoms in simple cubic unit cell = $\frac{4}{3}\pi \left(\frac{a}{2}\right)^3 - \frac{4}{3}\pi \times \frac{a^3}{8} = \frac{\pi}{6}a^3$ Ans

Q18. Ans - (a)

Q19. Ans - (d)

Q20. Ans - (c)

Q21. Ans - (b)

Q22. Ans - (d)

Q23. Ans - (a)

Q24. Ans - (d)

Q25. Ans - (b)

If h, k, l is the miller indices of the plane then the plane is passing through points.

(1) (0,0,0), (2) (0,0,1) (3) (1,1,0) & (4) (1,1,1)

$hx + ky + lz = e$

(1) $\Rightarrow ho + Ko + lo = 3 \Rightarrow e = 0$

$h \times 0 + k \times 0 + l \times 1 = 0 \Rightarrow l = 0$

(2) $\Rightarrow h \times 1 + K \times 1 + l \times 0 = 0 \Rightarrow h + k = 0$

(3) $\Rightarrow h + k + l = 0 \quad h + k = 0 \Rightarrow h = -K$

\therefore Miller indices = $(h, -h, 0) = h(1, -1, 0)$.

Q 26. Ans - (b)

Q27. Ans - (d) Since twice the no. of atoms can be present as there are no. of atoms present in FCC unit cell.

Q28. Ans - (b)

Q29. Ans - (a) In BCC only one ion pair will be present in unit cell

$$d = \frac{2 \times 168.4}{6.023 \times 10^{23} \times a^3} = 3.988 \text{ g/cc}$$

$$a^3 = \frac{1 \times 168.4}{6.023 \times 3.988 \times 10^{23}} = 70.011 \times 10^{-23} \text{ cc}$$

Q30. Ans - (d) For Cs^+ ion to be present in bcc void

radius ratio, $\frac{r^+}{r^-} = 0.732$ in limiting case when cation & anions just touches each other.

Q31. Ans - (a) $x = 8 \times \frac{1}{8} = 1$

$$y = 6 \times \frac{1}{2} = 3$$

$\therefore \text{A}_x\text{B}_y$ is AB_3

Q32. Ans - (c) A_3B_4 , because at face centre it will remain so effective no. of A new = 3

Q33. Ans - (b) Q34. Ans - (a), (c)

Q35. Ans - (a) Q36. Ans - (b)

Q37. Ans - (d)

$$h = \frac{2\gamma \cos \theta}{\rho r g}$$

If x-section is doubled new radius becomes $\sqrt{2}$ times the initial radius.

$$\text{Height raised becomes} = \frac{1}{\sqrt{2}} \text{ times} = \frac{1}{\sqrt{2}} \times 2.0 \text{ cm} = 1.414 \text{ cm}$$

Q38. Ans - (b)

$$\therefore \eta = A c \frac{E}{RT} \quad \text{As } T \uparrow, \eta \downarrow$$

Q39. Ans - (d)

Q40. Ans - (a)

Q41. Ans - (b)

Q42. Ans - (b)

Q43. Ans - (a)

Q44. Ans - (c)

$$\begin{aligned} \gamma(\text{n-C}_3\text{H}_7\text{OH}) &= 23.78 \text{ mJ m}^{-2} \\ &= 23.78 \times 10^{-3} \text{ N-m} \end{aligned}$$

$$\gamma(\text{CH}_3\text{OH}) = 22.61 \text{ dyne-cm}^{-1} = 22.61 \times 10^{-3} \text{ N/m}$$

$$\gamma(\text{C}_2\text{H}_5\text{OH}) = 2.275 \times 10^{-2} \text{ N/m}$$

$$\therefore \gamma(\text{n-C}_3\text{H}_7\text{OH}) > \gamma(\text{CH}_3\text{OH}) > \gamma(\text{C}_2\text{H}_5\text{OH})$$

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