AIEEE - 2009

Answers

											^	. ^		
	C	OD	ES	CODES				CODES						
Q.No.	Α	В	С	D	Q.No.	Α	В	С	D	Q.No.	A	B	С	D
01	2	1	4	1	31	3	2	1	4	61	3		4	4
02	1	4	4	1	32	4	1	2	3	62	48	\ 4	3	4
03	3	2	4	1	33	3	2	3	4	63 (⊅ 3	\mathbb{Z}	4	1
04	1	3	3	1	34	3	3	4	4	64	3	3	1	1
05	2	3	2	4	35	3	2	3	2	65	22	1	3	2
06	1	1	1	2	36	3	2	3	3	66	38/	1	4	3
07	4	1	4	1	37	4	1	1	3	67		2	3	2
08	3	1	4	1	38	4	4	4	4	68_) 2	1	4	4
09	4	2	4	1	39	3	1	2	3	69	4	1	4	4
10	2	1	3	4	40	4	3	2	$\langle \mathcal{A} ($	70	4	4	4	2
11	4	2	1	4	41	3	4	1	4	73	3	4	3	3
12	2	4	4	4	42	3	1	4	4	72	1	1	4	3
13	2	3	4	4	43	3	2	2	2	73	2	3	1	1
14	3	3	3	1	44	2	2	3/	40	74	3	3	4	4
15	4	2	2	3	45	2	3	4	2))	75	2	3	4	4
16	2	2	4	3	46	4	2	(37)	\\\delta	76	2	2	3	1
17	2	2	3	1	47	2	1))2	77	2	1	4	2
18	2	1	3	1	48	1	4 ((2 0	4	78	2	1	4	1
19	3	1	4	1	49	1	30	3	1	79	2	3	3	1
20	1	2	1	4	50	2	(1	(3)	1	80	4	1	2	3
21	2	2	2	4	51	2	2	3	3	81	1	4	3	1
22	4	2	3	1	52	2 <	2	7 4	3	82	1	3	3	4
23	4	2	3	2	53	37	*	1	1	83	3	3	3	4
24	1	1	3	4	54	2	71)	3	4	84	2	1	4	1
25	4	1	4	2	55	(2)	12	1	4	85	1	4	1	1
26	1	1	1	4	56	/3)) 1	1	4	86	3	1	1	3
27	4	3	3	2	57 2	35	1	1	1	87	3	3	2	4
28	3	2	3	1	58	7 2	1	3	2	88	4	4	3	4
29	2	2	2	2	59	S)	4	3	2	89	3	2	4	1
30	2	2	2	4	Z 60	_3	3	2	2	90	2	2	1	1

Though every care has been taken to provide the answers correctly but the Institute shall not be responsible for error, if any



Dated: 26/04/2009

Solutions of AIEEE 2009

Time: 3 hrs.

CODE - B

Max. Marks: 432

Chemistry, Mathematics & Physics

Important Instructions:

1. Immediately fill in the particulars on this page of the Test Booklet with Blue/Black Ball Point Pen. Use of pencil is strictly prohibited.

- 2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.)
- 3. The test is of 3 hours duration.
- 4. The Test Booklet consists of 90 questions. The maximum marks are 432.
- 5. There are **three** parts in the question paper. The distribution of marks subjectwise in each part is as under for each correct response.
 - Part A CHEMISTRY (144 marks) Question No. 1 to 24 consist FOUR (4) marks each and Question No. 25 to 30 consist EIGHT (8) marks each for each correct response.
 - Part B MATHEMATICS (144 marks) Question No. 31 to 32 and 39 to 60 consist FOUR (4) marks each and Question No. 33 to 38 consist EIGHT (8) marks each for each correct response.
 - Part C PHYSICS (144 marks) Questions No.61 to 84 consist FOUR (4) marks each and Question No. \$5 to 90 consist EIGHT (8) marks each for each correct response
- 6. Candidates will be awarded marks as stated above in instructions No. 5 for correct response of each question. ¼ (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
- 7. Use Blue/Black Ball Point Pen only for writing particulars/marking responses on Side-1 and Side-2 of the Answer Sheet Use of pencil is strictly prohibited.
- 8. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. except the Admit Card inside the examination hall/room.
- 9. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall, however the candidates are allowed to take away this Test Booklet with them.
- 10. The CODE for this Booklet is **B**. Make sure that the **CODE** printed on Side-2 of the Answer Sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet

o not fold or make any stray marks on the Answer Sheet.

PART-A: CHEMISTRY

- The IUPAC name of neopentane is
 - (1) 2, 2-dimethylpropane

(2) 2-methylpropane

(3) 2, 2-dimethylbutane

(4) 2-methylbutane

Answer (1)

$$\begin{array}{ccc} & & & CH_3 \\ & & & 1 & 3 \\ \text{Hints}: & & CH_3 - C - CH_4 \\ & & & & I \\ & & & CH_3 \end{array}$$

IUPAC name: 2, 2-dimethylpropane

- Which one of the following reactions of Xenon compounds is not feasible

(3)
$$XeF_6 + RbF \rightarrow Rb[XeF_7]$$

(4)
$$XeO_3 + \beta FIF \rightarrow XeF_6 + 3H_2O_3$$

Answer (4)

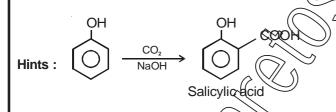
Hints : $XeF_6 + 3H_2O \rightarrow XeO_3 + 6HF$

- The major product obtained on interaction of phenol with socious hydroxide and carbon dioxide is:
 - (1) Salicylaldehyde

Salicylic acid

- (3) Phthalic acid
- Benzoic acid

Answer (2)



- Which of the following statements is incorrect regarding physissorptions?
 - (1) More easily liquefiable gases are adsorbed readily
 - (2) Under high pressure it results into multi molecular layer on adsorbent surface
 - (3) Enthalpy of agracino $(\Delta H_{adsorption})$ is low and positive
 - (4) It occurs because of van der Waal's forces

Answer (3)

Hints: Physisorption is an exothermic process with $\Delta H \simeq -20$ kJ/mol

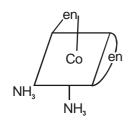
Which of the following has an optical isomer?

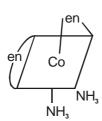
(2) $[Co (H_2O)_4 (en)]^{3+}$

 $(en)_2 (NH_3)_2]^{3+}$

(4) $[Co(NH_3)_3CI]^+$

Answer (3)





- 6. Solid Ba(NO₃)₂ is gradually dissolved in a 1.0 \times 10⁻⁴ M Na₂CO₃ solution. At what concentration of Ba²⁺ will a precipitate begin to form? (K_{sp} for BaCO₃ = 5.1 \times 10⁻⁹)
 - (1) $5.1 \times 10^{-5} \text{ M}$

(2) $8.1 \times 10^{-8} \text{ M}$

(3) $8.1 \times 10^{-7} \text{ M}$

(4) $4.1 \times 10^{-5} \text{ M}$

Answer (1)

Hints: $[CO_3^{2-}] = 10^{-4} \text{ M}$

$$K_{sp} [BaCO_3] = [Ba^{2+}] [CO_3^{2-}]$$

$$\Rightarrow [Ba^{2+}] = \frac{K_{sp}}{[CO_3^{2-}]} = \frac{5.1 \times 10^{-9}}{10^{-4}} = 5.1 \times 10^{-5} \text{ M}$$

7. Calculate the wavelength (in nanometer) associated with a proton moving at 1.0×10^3 ms⁻¹

(Mass of proton = 1.67×10^{-27} kg and h = 6.63×10^{-34} Js)

(1) 0.40 nm

(2) 2.5 nm

(3) 14.0 nm

(4) 0.032 nm

Answer (1)

Hints: $\lambda = \frac{\Pi}{p} = \frac{\Pi}{mv}$

or
$$\lambda = \frac{6.63 \times 10^{-34}}{1.67 \times 10^{-27} \times 10^{3}}$$

- 8. In context with the transition elements, which of the following statements is incorrect?
 - (1) In the highest exidation states, the transition metals show basic character and form cationic complexes
 - (2) In the highest oxidation states of the first five transition elements (Sc to Mn), all the 4s and 3d electrons are used for bonding.
 - (3) Once the o[©] configuration is exceeded, the tendency to involve all the 3d electrons in bonding decreases
 - (4) In addition to the normal oxidation states, the zero oxidation state is also shown by these elements in

Answer (1)

Hints In the highest oxidation states, the transition metals show acidic character.

- 9. In an atom, an electron is moving with a speed of 600 m/s with an accuracy of 0.005%. Certainity with which the position of the electron can be located is (h = 6.6×10^{-34} kg m²s⁻¹, mass of electron, $e_m = 9.1 \times 10^{-31}$ kg
 - (1) $5.10 \times 10^{-3} \text{ m}$

(2) $1.92 \times 10^{-3} \text{ m}$

(3) $3.84 \times 10^{-3} \text{ m}$

(4) 1.52×10^{-4} m

Answer (2)

Hints: $\Delta p \cdot \Delta x \ge \frac{h}{4\pi}$

$$\Delta X = \frac{h}{4\pi \cdot m\Delta V}$$

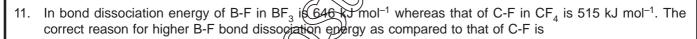
$$= \frac{6.6 \times 10^{-34} \times 100}{4 \times 3.14 \times 9.1 \times 10^{-31} \times 600 \times 0.005}$$

$$= 1.92 \times 10^{-3} \text{ m}$$

- 10. Which of the following pairs represents linkage isomers?
 - (1) $[Pd(P Ph_3)_2 (NCS)_2]$ and $[Pd(P Ph_3)_2 (SCN)_2]$
 - (2) [Co (NH₃)₅ NO₃]SO₄ and <math>[Co(NH₃)₅SO₄] NO₃
 - (3) $[Pt Cl_2(NH_3)_4]Br_2$ and $[PtBr_2(NH_3)_4]Cl_2$
 - (4) $[Cu(NH_3)_4]$ $[PtCl_4]$ and $[Pt(NH_3)_4]$ $[CuCl_4]$

Answer (1)

Hints: SCN⁻ is an ambidentate ligand.



- (1) Stronger σ bond between B and F in BF as compared to that between C and F in CF₄
- (2) Significant $p\pi p\pi$ interaction between B and F in BF₃ whereas there is no possibility of such interaction between C an F in CF₄
- (3) Lower degree of $p\pi$ $p\pi$ interaction between B and F in BF_3 than that between C and F in CF_4
- (4) Smaller size of B-atom as compared to that of C-atom

Answer (2)

Hints: In BF₃, F forms pπ back bonding with B.

- 12. Using MO theory predict which of the following species has the shortest bond length?
 - $(1) O_2^2$

(2) O_2

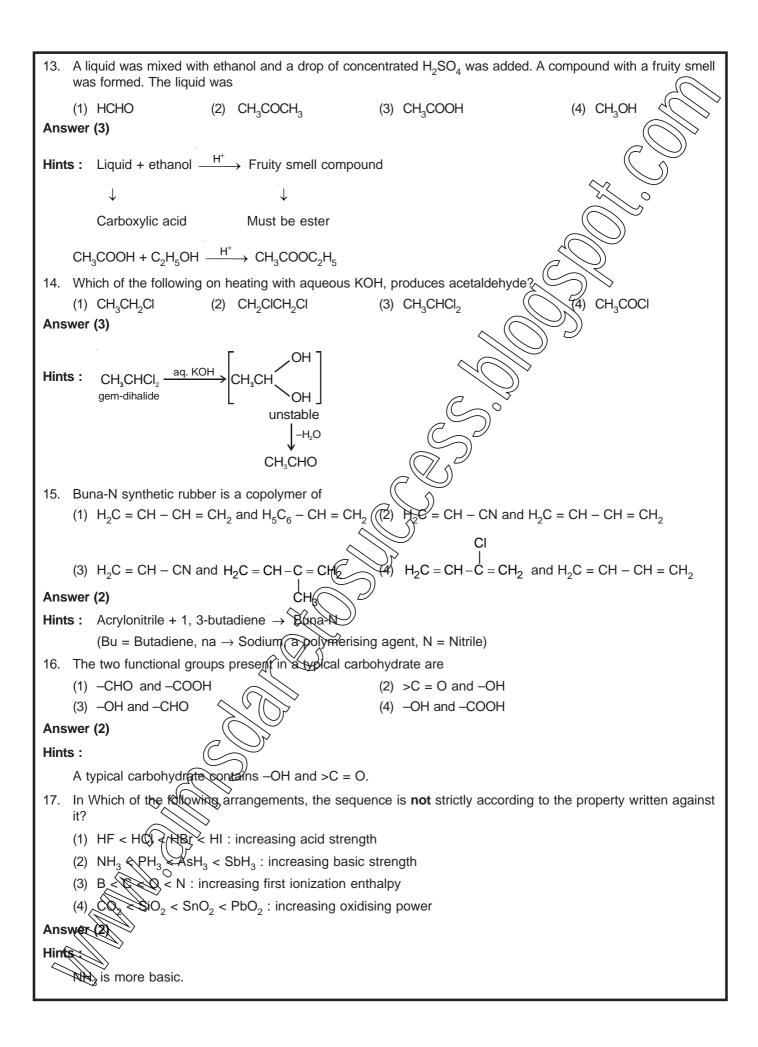
(3) O_{2}^{2}

(4) O_2^2

Answer (4)

Hints: Righer is the bond order, shorter is the bond length.

Bond order of O_2^{2+} is 3.0



- 8. A binary liquid solution is prepared by mixing n-heptane and ethanol. Which one of the following statements is **correct** regarding the behaviour of the solution?
 - (1) The solution is non-ideal, showing +ve deviation from Raoult's Law
 - (2) The solution is non-ideal, showing -ve deviation from Raoult's Law
 - (3) n-heptane shows +ve deviation while ethanol shows -ve deviation from Raoult's Law
 - (4) The solution formed is an ideal solution

Answer (1)

Hints: Ethanol has H-Bonding, n-heptane tries to break the H-bonds of ethanol, hence, increases. Such a solution shows positive deviation from Raoult's Law.

- 19. The set representing the correct order of ionic radius is
 - (1) $Na^+ > Li^+ > Mg^{2+} > Be^{2+}$
 - (2) $Li^+ > Na^+ > Mg^{2+} > Be^{2+}$
 - (3) $Mg^{2+} > Be^{2+} > Li^+ > Na^+$
 - (4) $Li^+ > Be^{2+} > Na^+ > Mg^{2+}$

Answer (1)

Hints:

$$Na^+ > Li^+ > Mg^{2+} > Be^{2+}$$

20. Arrange the carbanions, $(CH_3)_3\bar{C}$, $\bar{C}Cl_3$, $(CH_3)_2\bar{C}H$, $(CH_3)_2\bar{C}H$, in order of their decreasing stability

(1)
$$(CH_3)_2 \overline{C}H > \overline{C}CI_3 > C_6H_5 \overline{C}H_2 > (CH_3)_3 \overline{C}$$

(2)
$$\overline{CCI}_3 > C_6H_5\overline{C}H_2 > (CH_3)_2\overline{C}H > (CH_3)_3\overline{C}$$

(3)
$$(CH_3)_3 \overline{C} > (CH_3)_2 \overline{C}H > C_6H_5 \overline{C}H_2 > \overline{C}C$$

(4)
$$C_6H_5\bar{C}H_2 > \bar{C}CI_3 > (CH_3)_3\bar{C} > (CH_3)_2CH_3$$

Answer (2)

Hints:

$$CCl_3^{\ominus} > C_6H_5CH_2^{\ominus} > (CH_3)_2CH_3(CH_3)_3C$$

- 21. Knowing that the chemistry of anthanoids (Ln) is dominated by its +3 oxidation state, which of the following statements is **incorrect**:
 - (1) The ionic sizes of Ln (NI) decrease in general with increasing atomic number
 - (2) Ln (III) compounds are generally colourless
 - (3) Ln (III) hydroxides are mainly basic in character
 - (4) Because of the large size of the Ln (III) ions the bonding in its compounds is predominently ionic in character.

Answer (2)

Hints

(fl) compounds are generally coloured.

22. The alkene that exhibits geometrical isomerism is

(1) 2 - methyl propene

(2) 2 - butene

(3) 2 - methyl - 2 - butene

(4) Propene

Answer (2)

Hints:

$$CH_3$$
 $C=C$
 CH_3 and CH_3
 $C=C$
 CH_3
 CH_3
 $C=C$
 CH_3
 CH

cis-2-Butene

23. The number of stereoisomers possible for a compound of the molecular formula CH₂, -CH(OH) - Me is

(1) 2

(2) 4

(3) 6

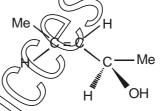
(4) 3

Answer (2)

Hints:

$$CH_3CH = CH - CH(OH)Me$$
 has

$$CH_3$$
 + its enantiomer



$$H$$
 $C = C$ H HO H

$$^{\text{H}}_{\text{CH}_3}$$
c=c $^{\text{H}}_{\text{CH(OH)Me}}$

$$H$$
 $C = C$
 H
 C
 H
 OH

$$H = C = C$$

$$HO H$$

24. In Cannizzaro reaction given bets

the slowest stepos

- (1) The transfer of hydride to the carbonyl group
- (2) The abstraction of proton from the carboxylic group
- (3) The deprotonation of PhCH₂OH
- (4) The attack of : OH at the carboxyl group

Answer (1)

Cannizzaro reaction, the transfer of hydride to the carbonyl group is the rate determining step.

25. On the basis of the following thermochemical data : $(\sqrt[4]{f}G^0H^+_{(aq)}=0)$

$$H_2O(I) \rightarrow H^+(aq) + OH^-(aq); \Delta H = 57.32 \text{ kJ}$$

$$H_2(g) + \frac{1}{2}O_2(g) \rightarrow H_2O(I); \Delta H = -286.20 \text{ kJ}$$

The value of enthalpy of formation of OH- ion at 25°C is

(1) -228.88 kJ

(2) +228.88 kJ

(3) -343.52 kJ

(4) -22.88 kJ

Answer (1)

Hints:

I.
$$H_2O(I) \rightarrow H^+(aq) + OH^-(aq)$$
; $\Delta H = 57.32 \text{ kJ}$

II.
$$H_2(g) + \frac{1}{2}O_2(g) \rightarrow H_2O(I); \Delta H = -286.20 \text{ kJ}$$

Adding I & II we get,

$$\mathrm{H_2(g)} + \, \frac{1}{2}\,\mathrm{O_2(g)} \rightarrow \mathrm{H^+(aq)} + \mathrm{OH^-(aq)}$$

$$\Delta H = 57.32 - 286.2$$

$$= -228.88 \text{ kJ}$$

- 26. Copper crystallises in fcc with a unit cell length of 36 (pm. What is the radius of copper atom?
 - (1) 127 pm
- (2) 157 pm



(4) 108 pm

Answer (1)

Hints:

$$r = \frac{a}{2\sqrt{2}} = \frac{361}{2\sqrt{2}} = 127.6 \text{ pm}$$

27. In a fuel cell methanol is used as fuel and oxygen gas is used as an oxidizer. The reaction is

$$CH_3OH(I) + \frac{3}{2}O_2(g) \rightarrow CO_2(g) + 2H_2O(I)$$

At 298 K standard Gibb's energies of formation for $CH_3OH(I)$, $H_2O(I)$ and $CO_2(g)$ are -166.2, -237.2 and -394.4 kJ mol⁻¹ respectively. It standard enthalpy of combustion of methanol is -726 kJ mol⁻¹, efficiency of the fuel cell will be

(1) 87%

(2) 90%

(3) 97%

(4) 80%

Answer (3)

Hints:

$$CH_3OH(I) + 2O_2(g) \rightarrow CO_2(g) + 2H_2O(I)$$

$$\Rightarrow \Delta G_{\text{products}} - \Delta G_{\text{reactant}}$$

$$= [-394.4 - 2 \times 237.2] - [-166.2]$$

We know, efficiency of a fuel cell,
$$\eta = \frac{\Delta G}{\Delta H} \times 100$$

$$= \frac{-702.6}{-726} \times 100$$

- 28. Two liquids X and Y from an ideal solution. At 300 K, vapour pressure of the solution containing 1 mol of X and 3 mol of Y is 550 mmHg. At the same temperature, if 1 mol of Y is further added to this solution, vapour pressure of the solution increases by 10 mmHg. Vapour pressure (in mmHg) of X and Y in their pure states will be, respectively
 - (1) 300 and 400
 - (3) 500 and 600

- (2) 400 and 600
- (4) 200 and 300

Answer (2)

Hint:

Let V. P. of pure
$$X = x$$

and V. P. of pure
$$Y = y$$

Then,
$$\frac{1}{4}x + \frac{3}{4}y = 550$$

and
$$\frac{1}{5}x + \frac{4}{5}y = 560$$

Solving (i) and (ii), we get

$$x = 400 \text{ mm}$$

and
$$y = 600 \text{ mm}$$

29. Given
$$E_{Fe^{3+}/Fe}^{0} = -0.036 \text{ V}, E_{Fe^{2+}/Fe}^{0}$$

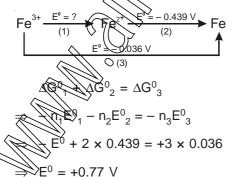
The value of standard electrode potential for the change, $Fe_{(aq)}^{3+}$ + $e^- \rightarrow Fe^{2+}$ (aq) will be

- (1) 0.385 V
- (3) 0.270 V

- (2) 0.770 V
- (4) 0.072 V

Answer (2)

Hint:



- 30. The half life period of a first order chemical reaction is 6.93 minutes. The time required for the completion of 99% of the chemical reaction will be (log 2 = 0.301)
 - (1) 23.03 minutes

(2) 46.06 minutes

(3) 460.6 minutes

(4) 230.3 minutes

Answer (2)

Hint:

$$t_{1/2} = \frac{\ln 2}{k}$$

$$\Rightarrow k = \frac{2.303 \times 0.301}{6.93}$$

Also,
$$t = \frac{2.303}{k} \log \left(\frac{a}{a - 0.99a} \right)$$

$$\Rightarrow t = \frac{2.303}{2.303 \times 0.301} \times 6.93 \log \left(\frac{1}{0.01}\right)$$
$$= 46.05 \text{ minutes}$$



Directions: Questions number **31** to **35** are Assertion-Reason type questions. Each of these questions contains two statements:

Statement -1 (Assertion) and Statement-2 (Reason)

Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select the correct choice.

31. **Statement-1**: $\sim (p \leftrightarrow \sim q)$ is equivalent to p

Statement-2 : $\sim (p \leftrightarrow \sim q)$ is a tautology.

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1
- (2) Statement-1 is true, Statement-2 is false
- (3) Statement-1 is false, Statement 2 is true
- (4) Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1

Answer (2)

Hint :

р	q	~q	p ↔ (~q)	~[p ↔ (~q)]	p ↔ q
T_	T	F	F	Т	Т
	F	Т	Т	F	F
	Т	F	Т	F	F
	F	Т	F	Т	Т

Statement (1) is true and statement (2) is false.

32. Let A be a 2 x 2 matrix

Statement-1: adj (adj A) = A

Statement-2: |adj A| = |A|

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement
- (2) Statement-1 is true, Statement-2 is false
- (3) Statement-1 is false, Statement-2 is true
- (4) Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1

Answer (1)

Hint:

Let
$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

Then adj
$$(A) = \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

$$|A| = |adj A| = ad - bc$$

Also adj[adj
$$A$$
] = $\begin{bmatrix} a & b \\ c & d \end{bmatrix} = A$

.. Both statements are true but (2) is not correct explanation of (1).

33. Let
$$f(x) = (x + 1)^2 - 1$$
, $x \ge -1$.

Statement-1: The set
$$\{x : f(x) = f^{-1}(x)\} = \{0, -1\}$$

Statement-2: *f* is a bijection.

- (1) Statement-1 is true, Statement-2 is true, Statement-2 is not a correct explanation for Statement-1
- (2) Statement-1 is true, Statement-2 is talse
- (3) Statement-1 is false, Statement 2 by true
- (4) Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1

Answer (2)

Hint :

We have,
$$f(x) = (x + 1)^{2} - 1$$

$$\Rightarrow f'(x) = 2(x+1) \ge 0 \text{ for } x \ge -1$$

$$\Rightarrow f(x)$$
 is one one

Since co-domain of the given function is not given, hence it can be considered as R, the set of reals and consequently R is pot onto.

Hence f is not bijective statement-2 is false.

Also
$$(x + 1)^2 - 1 \ge -1$$
 for $x \ge -1$

$$f(x) = f^{-1}(x)$$
 at $x = 0$ and $x = -1$.

stement-1 is true.

34. **Statement-1**: The variance of first *n* even natural numbers is $\frac{n^2-1}{4}$.

Statement-2: The sum of first n natural numbers is $\frac{n(n+1)}{2}$ and the sum of squares of first n natural

numbers is
$$\frac{n(n+1)(2n+1)}{6}$$

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1
- (2) Statement-1 is true, Statement-2 is false
- (3) Statement-1 is false, Statement-2 is true
- (4) Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1

Answer (3)

Hint:

Statement (2) is true.

$$\operatorname{var} x = \frac{\sum x_i^2}{n} - \left(\frac{\sum x_i}{n}\right)^2$$

$$= \frac{4 n (n+1) (2n+1)}{6n} - (n+1)^2$$

$$= \frac{2}{3} (n+1) (2n+1) - (n+1)^2$$

$$= \frac{(n+1)}{3} \{4n+2-3n-3\}$$

$$= \frac{(n+1) (n-1)}{3}$$

$$= \frac{n^2 - 1}{3}$$

:. Statement (1) is false

Statement (2) is true.

35. Let f(x) = x |x| and $g(x) = \sin x$.

Statement-1 Quite differentiable at x = 0 and its derivative is continuous at that point.

Statement-2: pot is twice differentiable at x = 0.

- (1) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1
- (2) Statement 1 is true, Statement-2 is false
- (3) Statement-1 is false, Statement-2 is true
- Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1

Answer (2)

$$f(x) = x |x|$$
 and $g(x) = \sin x$

(gof) (x) =
$$\begin{cases} -\sin x^2 & x < 0 \\ 0 & x = 0 \\ \sin x^2 & x > 0 \end{cases}$$

For first derivative

LHD =
$$\lim_{x \to 0} \frac{-\sin x^2}{x} = \lim_{x \to 0^-} \frac{-x \sin x^2}{x^2} = 0$$

= 0

RHD =
$$\lim_{x \to 0^+} \frac{\sin x^2}{x} \times \frac{x}{x} = 0$$

 \therefore gof is differentiable at x = 0.

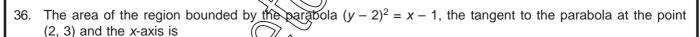
$$(gof)'(x) = \begin{cases} -2x \cos x^2 & x < 0 \\ 0 & x = 0 \\ 2x \cos x^2 & x > 0 \end{cases}$$

For second derivative,

LHD =
$$\lim_{x \to 0^{-}} \frac{-2x \cos x^{2}}{x} = -2$$

$$RHD = \lim_{x \to 0^+} \frac{2x \cos x^2}{x} = 2$$

 \therefore (gof) is not twice differentiable at x = 2



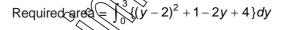
- (1) 6
- (3) 12

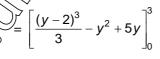
(2) 9

(4) 3

Answer (2)

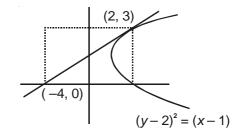
Hints: The equation of tangent at (2, 3) to the given parabola is x = 2y - 4





$$=\frac{1}{3}-9+15+\frac{8}{3}$$

= 9 sq. units.



- 37. Given $P(x) = x^4 + ax^3 + bx^2 + cx + d$ such that x = 0 is the only real root of P(x) = 0. If P(-1) < P(1), then in the interval [-1, 1]
 - (1) P(-1) is not minimum but P(1) is the maximum of P
 - (2) P(-1) is minimum but P(1) is not the maximum of P
 - (3) Neither P(-1) is the minimum nor P(1) is the maximum of P
 - (4) P(-1) is the minimum and P(1) is the maximum of P

Answer (1)

Hints: We have $P(x) = x^4 + ax^3 + bx^2 + cx + d$

$$P'(x) = 4x^3 + 3ax^2 + 2bx + c$$

$$P'(0) = 0 \Rightarrow c = 0$$

Also P'(x) = 0 only at x = 0

P'(x) is a cubic polynomial changing its sign from (-)ve to (+)ve and passing through O.

$$P'(x) < 0 \forall x < 0$$

$$P'(x) > 0 \forall x > 0$$

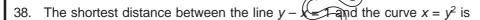
Hence the graph of P(x) is upward concave, where $P'(x) = \emptyset$

Now
$$P(-1) < P(1)$$

 \Rightarrow P(-1) cannot be minimum in [-1, 1] as minima in this interval is at x = 0.

Hence in [-1, 1] maxima is at x = 1

Hence P(-1) is not minimum but P(1) is the maximum of P.





(2)
$$\frac{3\sqrt{2}}{5}$$

(3)
$$\frac{\sqrt{3}}{4}$$

(4)
$$\frac{3\sqrt{2}}{9}$$

Answer (4)

Hints: Let there be a point P(x) on $x = y^2$

Its distance from x - x + 1 = 0 is

$$\left|\frac{t^2-t+1}{\sqrt{2}}\right|$$

$$\frac{3}{4}$$

Shortest distance =
$$\left| \frac{3}{4\sqrt{2}} \right| = \frac{3\sqrt{2}}{8}$$

- 39. Let the line $\frac{x-2}{3} = \frac{y-1}{-5} = \frac{z+2}{2}$ lie in the plane $x + 3y \alpha z + \beta = 0$. Then (α, β) equals
 - (1) (-6, 7)

(2) (5, -15)

(3) (-5, 5)

(4) (6, -17)

Answer (1)

Hints: The point (2, 1, -2) is on the plane $x + 3y - \alpha z + \beta = 0$

$$2 + 3 + 2\alpha + \beta = 0$$

$$2\alpha + \beta = -5$$

Also

$$1(3) + 3(-5) + -\alpha(2) = 0$$

$$3 - 15 - 2\alpha = 0$$

$$2\alpha = -12$$

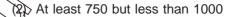
$$\alpha = -6$$

Put
$$\alpha = -6$$
 in (i)

$$\beta = 12 - 5 = 7$$

$$\therefore (\alpha, \beta) \equiv (-6, 7)$$

- 40. From 6 different novels and 3 different dictionaries, and 1 dictionary are to be selected and arranged in a row on a shelf so that the dictionary is always in the middle. Then the number of such arrangements is
 - (1) At least 500 but less than 750



(3) At least 1000

(4) Less than 500

Answer (3)

Hints: The number of ways in which 4 mayels can be selected = 6C_4 = 15

The number of ways in which 1 dictionary can be selected = ${}^{3}C_{1}$ = 3

4 novels can be arranged in 4! ways.

- \therefore The total number of ways = 15 x 4! x 3 = 15 x 24 x 3 = 1080.
- 41. In a binomial distribution (p), $(p) = \frac{1}{4}$, if the probability of at least one success is greater than or equal to
 - $\frac{9}{10}$, then *n* is greater than
 - (1) $\log_{10} 3$

(2) $\frac{9}{\log_{10} 4 - \log_{10} 3}$

 $4 - \log_{10} 3$

(4) $\frac{1}{\log_{10} 4 - \log_{10} 3}$

Answer (4)

Hints: $1 - \left(\frac{3}{4}\right)^n \ge \frac{9}{10}$

$$\Rightarrow \left(\frac{3}{4}\right)^n \le 1 - \frac{9}{10} = \frac{1}{10}$$

$$\Rightarrow \left(\frac{4}{3}\right)^n \ge 10$$

$$\Rightarrow n[\log_4 - \log_3] \ge \log_{10} 10 = 1$$

$$\Rightarrow n \ge \frac{1}{\log 4 - \log 3}$$

- 42. The lines $p(p^2 + 1)x y + q = 0$ and $(p^2 + 1)^2x + (p^2 + 1)y + 2q = 0$ are perpendicular to a common line for
 - (1) Exactly one value of p

(2) Exactly two values of p

(3) More than two values of p

(4) No value of p

Answer (1)

Hints: Lines perpendicular to same line are parallel to each other.

$$-p(p^2 + 1) = p^2 + 1$$

$$\Rightarrow p = -1$$

 \therefore There is exactly one value of p.



(1)
$$A = C$$

(3)
$$A \cap B = \emptyset$$

(2)
$$B = C$$

(4)
$$A = B$$

Answer (2)

Hints: $A \cap B = A \cap C$ and $A \cup B = A \cup C$

$$\Rightarrow B = C$$

44. For real x, let $f(x) = x^3$ then

(1) f is onto R but not one-one

- (2) f is one-one and onto R
- (3) f is neither one-one nor onto R
- (4) f is one-one but not onto R

Answer (2)

Hints: $f(x) = x^3 + 6x + 1$

$$f'(x) = 3x^2 + 5 > 0 \ \forall \ x \in R$$

Hence (x) is monotonic increasing. Therefore it is one-one.

Also it onto on R

tence it one-one and onto R.

45. The differential equation which represents the family of curves $y = c_1 e^{c_2 x}$, where c_1 and c_2 are arbitrary constants,

is

(1) y'' = y' y

(2) vv'' = v'

(3) $yy'' = (y')^2$

(4) $y' = y^2$

Answer (3)

Hints: Put $e^{c_2} = k$

Then
$$y = c_1 . k^x$$

$$\Rightarrow \log_e y = \log_e c_1 + x \log_e k$$

$$\Rightarrow \frac{1}{V}y' = \log_e k$$

$$\Rightarrow \frac{1}{y}y'' - \frac{1}{y^2}(y')^2 = 0$$

$$\Rightarrow yy'' = (y')^2$$

46. Let a, b, c be such that $b(a + c) \neq 0$. If $\begin{vmatrix} a & a+1 & a-1 \\ -b & b+1 & b-1 \\ c & c-1 \end{vmatrix} + \begin{vmatrix} a+1 & b+1 & c-1 \\ a-1 & b-1 & c+1 \\ c & c-1 \end{vmatrix} = 0$, then the value

of n is

- (1) Any even integer
- (3) Any integer

- (2) Any odd integer
-)) (4) Zero

Answer (2)

Hints: Applying D' = D is first determinant and $R_2 \leftrightarrow R_3$ and $R_1 \leftrightarrow R_2$ in second determinant



Then $\begin{vmatrix} a + (-1)^n & a - b & (-1)^{n+1}b & c + (-1)^n c \\ a + 1 & b + 1 & c - 1 \\ b - 1 & c + 1 \end{vmatrix} = 0$ if n is an odd integer.

- 47. The remainder left put when $8^{2n} (62)^{2n+1}$ is divided by 9 is
 - (1) 2

(2) 7

(3) [8

(4) 0

Answer (1)

Hints Rut n = 0

Then when 1 – 62 is divided by 9 then remainder is same as when 63–61 is divided by 9 which is 2.

- 48. Let y be an implict function of x defined by $x^{2x} 2x^x \cot y 1 = 0$. Then y'(1) equals
 - (1) 1

(2) log 2

(3) -log 2

(4) -1

Answer (4)

Hints:
$$(x^x)^2 - 2 \cdot x^x \cot y = 1$$
, \therefore when $x = 1$, $y = \frac{\pi}{2}$

Differentiating, $2.x^x.x^x(1 + \log_e x) - 2\left[-x^x \csc^2 y \frac{dy}{dx} + \cot y.x^x(1 + \log x)\right] = 0$

Put
$$x = 1$$
 and $y = \frac{\pi}{2}$

$$2+2.\frac{dy}{dx}-2\times 0=0$$

$$\frac{dy}{dx} = -1$$

- 49. If the roots of the equation $bx^2 + cx + a = 0$ be imaginary, then for all real values of x, the expression $3b^2x^2 + 6bcx + 2c^2$ is
 - (1) Less than 4ab

(2) Greater than -4ab

(3) Less than -4ab

(4) Greater than 4ab

Answer (2)

Hints:
$$bx^2 + cx + a = 0$$

Roots are imaginary $c^2 - 4ab < 0$

$$f(x) = 3b^2x^2 + 6bcx + 2c^2$$

$$D = 36b^2c^2 - 24b^2c^2 = 12b^2c^2$$

$$3b^2 > 0$$

$$\therefore f(x) \ge \left(-\frac{D}{4a}\right)$$

$$f(x) \geq -c^2$$

Now $c^2 - 4ab$

$$c^2 < 4ab$$

- 50. The sum to infinity of the series $1 + \frac{2}{3} + \frac{6}{3^2} + \frac{10}{3^3} + \frac{14}{3^4} + \dots$ is
 - (2) 4

(3) 6

(4) 2

Hints: Let $S = 1 + \frac{2}{3} + \frac{6}{3^2} + \frac{10}{3^3} + \frac{14}{3^4} + \dots$

$$S-1=\frac{2}{3}+\frac{6}{3^2}+\frac{10}{3^3}+\frac{14}{3^4}+\dots$$

$$\frac{S-1}{3} = \frac{2}{3^2} + \frac{6}{3^3} + \frac{10}{3^4} + \frac{14}{3^5} + \dots$$

$$\Rightarrow \frac{2}{3}(S-1) = \frac{2}{3} + \frac{4}{3^2} + \frac{4}{3^3} + \frac{4}{3^4} + \dots$$

$$\Rightarrow$$
 S-1=1+ $\frac{2}{3}$ + $\frac{2}{3^2}$ + $\frac{2}{3^3}$ +.....

$$\Rightarrow S = 2 + \frac{\frac{2}{3}}{1 - \frac{1}{3}}$$

51. The projections of a vector on the three coordinate axis are respectively. The direction cosines of the vector are

(1)
$$\frac{6}{5}, \frac{-3}{5}, \frac{2}{5}$$

(3)
$$\frac{-6}{7}, \frac{-3}{7}, \frac{2}{7}$$

Answer (2)

Hints: Direction ratios are a = 6, b = -3 and c = 6

Then direction cosines are $\frac{6}{\sqrt{36+9+4}}$, $\frac{-3}{\sqrt{36+9+4}}$, $\frac{2}{\sqrt{36+9+4}}$

$$=\frac{6}{7},\frac{-3}{7},\frac{2}{7}$$

52. Let A and B denote the statements:

A:
$$\cos\alpha + \cos\beta + \cos\gamma = 0$$

B:
$$\sin\alpha + \sin\beta + \sin\gamma = 0$$

If
$$cos(\beta - \gamma)$$
 $+ cos(\alpha - \beta) = -\frac{3}{2}$, then

- (1) A is talse and B is true
- (2) Both a and B are true
- (a) Both A and B are false
 - A is true and B is false

Answer (2)

Hints: $2(\cos\beta \cos\gamma + \sin\beta \sin\gamma) + 2(\cos\gamma \cos\alpha + \sin\gamma \sin\alpha) + 2(\cos\alpha \cos\beta + \sin\alpha \sin\beta)$

 $+\sin^2\alpha + \cos^2\alpha + \sin^2\beta + \cos^2\beta + \sin^2\gamma + \cos^2\beta$

 \Rightarrow $(\sin\alpha + \sin\beta + \sin\gamma)^2 + (\cos\alpha + \cos\beta + \cos\gamma)^2 = 0$

 \Rightarrow $\sin \alpha + \sin \beta + \sin \gamma = 0 = \cos \alpha + \cos \beta + \cos \gamma$

.. Both A and B are true.

53. One ticket is selected at random from 50 tickets numbered 00, 01, 02, ..., 49. Then the probability that the sum of the digits on the selected ticket is 8, given that the product of these digits is zero equals

 $(1) \frac{1}{7}$

(2) $\frac{5}{14}$

(3) $\frac{1}{50}$

Answer (4)

Hints: Restricting sample space as $S = \{00, 01, 02, 03, 04, 05, 06, 07, 08, 09, 10, 20, 30, 40\}.$

 $\therefore P(\text{sum of digits is 8}) = \frac{1}{14}.$

54. Three distinct points A, B and C are given in the 2 - dimensional coordinate plane such that the ratio of the distance of any one of them from the point (1, 0) to the distance from the point (-1, 0) is equal to $\frac{1}{3}$. Then the circumcentre of the triangle ABC is at the point

 $(1) \quad \left(\frac{5}{4}, 0\right)$

 $(2) \quad \left(\frac{5}{2}, 0\right)$

(3)

(4) (0, 0)

Answer (1)

Hints: Let (x, y) denote the coordinates of A, B and

Then, $\frac{(x-1)^2 + y^2}{(x+1)^2 + y^2} = \frac{1}{9}$

 \Rightarrow 9x² + 9y² - 18x + 9 = x² + y² +

 $\Rightarrow 8x^2 + 8y^2 - 20x + 8 = 0$

 $x^2 + y^2 - \frac{5}{2}x + 1 = 0$

 \therefore A, B, C lie on a circle with $C(\frac{5}{4},0)$.

55. If the mean deviation at the numbers 1, 1 + d, 1 + 2d,, 1 + 100d from their mean is 255, then the d is equal to

(1) 20.0

(2) 10.1

(3) 20.2

(4) 10.0

Answer (2)

Hints: $\overline{x} = \frac{1 + (0 + d) + (1 + 2d) + \dots + (1 + 100d)}{101}$

101 (1+2+3+.....100)

$$\frac{101 + d \times \frac{100 \times 101}{2}}{101}$$

 $\bar{x} = 1 + 50d$

Mean deviation =
$$\frac{|1+50d-1|+|1+50d-1-d|+.....|1+50d-1-100d|}{101}$$

$$= \frac{50d + 49d + 48d + \dots + d + 0 + d + 2d + \dots + 50d}{101}$$

$$= \frac{2 \times d \times \left(\frac{50 \times 51}{2}\right)}{101}$$

$$\Rightarrow \frac{50 \times 51 \times d}{101} = 255$$

$$\Rightarrow$$
 $d = 10.1$

56. The ellipse $x^2 + 4y^2 = 4$ is inscribed in a rectangle aligned with the coordinate axes, which in turn is inscribed in another ellipse that passes through the point (4, 0). Then the equation of the ellipse is

(1)
$$x^2 + 12y^2 = 16$$

$$(2) 4x^2 + 48y^2 = 48$$

(3)
$$4x^2 + 64y^2 = 48$$

(4)
$$x^2 + 16y^2 = 16$$

Answer (1)

Hints: Let the equation of the required ellipse is

$$\frac{x^2}{16} + \frac{y^2}{b^2} = 1$$

But the ellipse passes through (2, 1)

$$\Rightarrow \frac{1}{4} + \frac{1}{b^2} = 1$$

$$\Rightarrow \frac{1}{b^2} = \frac{3}{4}$$

$$\Rightarrow b^2 = \frac{4}{3}$$

Hence equation is

$$\frac{x^2}{16} + \frac{y^2 \times 3}{4}$$

$$\Rightarrow x^2 + 12x^2 = 16$$

57. If $|Z - \frac{4}{Z}| \approx 2$, then the maximum value of |Z| is equal to



(4)
$$\sqrt{3} + 1$$

Answer (1



(0, 1)

(2, 0)

Hints: $\left|Z - \frac{4}{Z}\right| = 2$

$$\Rightarrow \left| Z - \frac{4}{Z} \right| \ge \left| |Z| - \frac{4}{|Z|} \right|$$

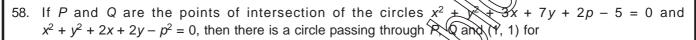
$$\Rightarrow |Z| - \frac{4}{|z|} \le 2$$

$$\Rightarrow |Z|^2 - 4 - 2|Z| \le 0$$

$$\Rightarrow |Z|^2 - 2|Z| - 4 \le 0$$

$$1 - \sqrt{5} \le |Z| \le 1 + \sqrt{5}$$

Hence maximum value = $1+\sqrt{5}$



- (1) All except one value of p
- (2) All except two values of p
- (3) Exactly one value of p
- (4) All values of p

Answer (1)

Hints: $x^2 + y^2 + 3x + 7y + 2p - 5 + \lambda(x^2 + y^2 + 2x + 2y - y^2) = 0$, $\lambda \neq -1$ passes through point of intersection of given circles.

Since it passes through (1, 1), hence

$$7 - 2p + \lambda(6 - p^2) = 0$$

$$\Rightarrow 7 - 2p + 6\lambda - \lambda p^2 = 0$$

If
$$\lambda = -1$$
, then $7 - 2p - 6 \approx 0$

$$p^2-2p+1=0$$

$$\therefore \lambda \neq -1 \text{ hence } p \neq 1$$

$$\therefore$$
 All values of pare possible except $p = 1$

59. If
$$\overrightarrow{u}, \overrightarrow{v}, \overrightarrow{w}$$
 are non-coplanar vectors and \overrightarrow{p} , \overrightarrow{q} are real numbers, then the equality $[3\overrightarrow{u}, \overrightarrow{pv}, \overrightarrow{pw}]$ $[2\overrightarrow{w}, \overrightarrow{qv}, \overrightarrow{qu}] = 0$ holds for

- (1) Exactly two values of (p, q)
- (2) More than two but not all values of (p, q)
- (3) All values of (p, q)
- (4) Exactly one value of (p, q)

Answer (4)

Hints: $[3\overrightarrow{u} \ p\overrightarrow{v} \ p\overrightarrow{w}] - [p\overrightarrow{v} \ \overrightarrow{w} \ q\overrightarrow{u}] - [2\overrightarrow{w} \ q\overrightarrow{v} \ q\overrightarrow{u}]$

$$= 3p^{2}[\overrightarrow{u}.(\overrightarrow{v}\times\overrightarrow{w})] - pq[\overrightarrow{v}.(\overrightarrow{w}\times\overrightarrow{u})] - 2q^{2}[\overrightarrow{w}.(\overrightarrow{v}\times\overrightarrow{u})]$$

$$\Rightarrow (3p^2 - pq + 2q^2)[\overrightarrow{u}.(\overrightarrow{v} \times \overrightarrow{w})] = 0$$

But
$$\overrightarrow{u} \cdot (\overrightarrow{v} \times \overrightarrow{w}) \neq 0$$

$$\Rightarrow 3p^2 - pq + 2q^2 = 0$$

$$\Rightarrow p = q = 0$$

60. $\int_{0}^{\pi} [\cot x] dx$, where [.] denotes the greatest integer function, is equal to

- (1) 1
- (2) -1

(3) $-\frac{\pi}{2}$

Answer (3)

Hints: $I = \int_{0}^{\pi} [\cot x] dx$

$$I = \int_{0}^{\pi} [\cot(\pi - x)] dx$$

$$2I = \int_{0}^{\pi} ([\cot x] + [-\cot x]) dx$$

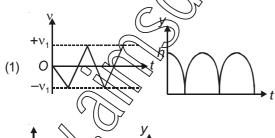
$$2I=\int\limits_{0}^{\pi}(-1)dx=-\pi$$

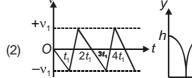
$$I=-\frac{\pi}{2}$$

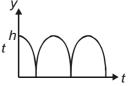
52

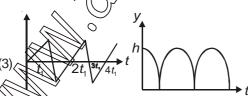
61. Consider a rubber ball freely falling from a height h = 4.9 m onto a horizontal elastic plate. Assume that the duration of collision is negligible and the collision with the plate is totally elastic.

Then the velocity as a function of time and the height as a function of time will be

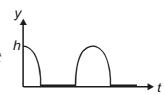












Answer (2)

From v = u + at

$$v = 0 - g \times t$$

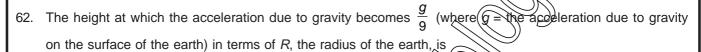
$$\Rightarrow v = -gt$$

And just after collision velocity is upwarded then after some time it becomes zero and then regative. Same process repeats.

From
$$S = ut + \frac{1}{2}at^2$$

$$h = 4.9 - \frac{1}{2}gt^2$$

So, graph will be downward parabola.



- (1) $\frac{R}{\sqrt{2}}$
- (2) $\frac{R}{2}$

(3) $\sqrt{2}R$

(4) 2R

Answer (4)

Hints:

As,

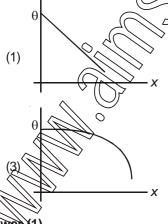
$$g(h) = \frac{g}{\left(1 + \frac{h}{R}\right)^2}$$

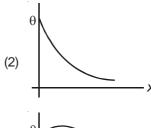
$$\Rightarrow \frac{g}{9} = \frac{g}{\left(1 + \frac{h}{R}\right)^2}$$

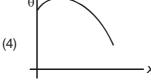
$$\Rightarrow \left(1 + \frac{h}{R}\right) = 3$$

$$\Rightarrow \frac{h}{R} = 2 \Rightarrow \boxed{h = 2R}$$

63. A long metallic bar is carrying heat from one of its ends to the other end under steady state. The variation of temperature θ along the length hof the bar from its hot end is best described by which of the following figures?







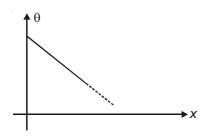
Answer (1)

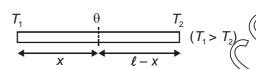
As rate of heat flow through the rod is constant through each section.

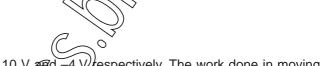
$$\frac{T_1 - \theta}{\frac{x}{k_0 A}} = \frac{\theta - T_2}{\frac{\ell - x}{k_0 A}}$$

$$\Rightarrow \theta = -\frac{(T_1 - T_2)x}{\ell} + T_1$$

So, graph is







64. Two point P and Q are maintained at the potentials of 10 V and -4 V respectively. The work done in moving 100 electrons from P to Q is

(1)
$$9.60 \times 10^{-17} \text{ J}$$
 (2) $-2.24 \times 10^{-16} \text{ J}$

(2)
$$-2.24 \times 10^{-16}$$

(3)
$$2.24 \times 10^{-16} \text{ J}$$

$$(4) - 9.60 \times 10^{-17} \text{ J}$$

Answer (3)

Hints:

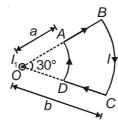
$$Q = 100e = -100 \times 1.6 \times 10^{-19} = -1.6 \times 10^{-17}$$

$$\Delta V = -14 \text{ V}$$

$$W = Q\Delta V = 14 \times 1.6 \times 10^{-17} = 2.24 \times 10^{-16}$$

Directions: Question numbers 65 and 66 are based on the following paragraph.

A current loop ABCD is held fixed on the paper as shown in the figure. The arcs BC (radius = b) and DA (radius = a) of the loop are joined by two straight wires AB and CD. A steady current I is flowing in the loop. Angle made by AB and CD at the origin Q is 30°. Another straight thin wire with steady current I_1 flowing out of the plane of the paper is kept at the origin.



65. The magnitude of the magnetic field (B) due to the loop ABCD at the origin (O) is



(2)
$$\frac{\mu_0 I}{4\pi} \left[\frac{b-a}{ab} \right]$$

$$2(b-a)+\frac{\pi}{3}(a+b)$$

(4) Zero

Magnetic field due to AB and CD is zero

$$\vec{B}_{net} = \frac{\mu_0}{4\pi} \times \frac{I}{a} \times \frac{\pi}{6} \hat{k} + \frac{\mu_0}{4\pi} \times \frac{I}{b} \times \frac{\pi}{6} (-\hat{k})$$

$$= \frac{\mu_0}{24} \times I \left\{ \frac{1}{a} - \frac{1}{b} \right\} \hat{k}$$

$$=\frac{\mu_0 I(b-a)}{24ab}\hat{k}$$

- 66. Due to the presence of the current I_1 at the origin
 - (1) The forces on AD and BC are zero
 - (2) The magnitude of the net force on the loop is given by $\frac{l_1 l}{4\pi} \mu_0 \left[2(b-a) + \frac{l_2 l}{3} (a+b) \right]$
 - (3) The magnitude of the net force on the loop is given by $\frac{\mu_0 II_1}{24ab}$
 - (4) The forces on AB and DC are zero

Answer (1)

Hints:

In wire DA

$$\vec{B} \uparrow \uparrow d\vec{\ell}$$

$$F_{DA} = 0$$

In wire AB, $d\vec{\ell} \times \vec{B}$ is upwards

In wire BC,
$$\vec{B} \uparrow \downarrow d\vec{\ell}$$
 $\therefore F_{BC} = 0$

In wire *CD*, $d\vec{\ell} \times \vec{B}$ is downwards.

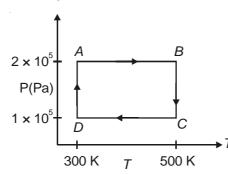
Since, AB and CD are symmetrical to I_1

So,
$$\overrightarrow{F_{AB}} + \overrightarrow{F_{CD}} = 0$$
.

Directions: Question numbers 67, 68 and 69 are based on the following paragraph

Two moles of helium gas are taken over the cycle ABCDA, as shown in the P-T diagram





67.	Assuming	the gas	s to be ide	al the work	done on	the gas in	taking it form	A to B is

- (1) 300 R
- (2) 400 R
- (3) 500 R

(4) 200 R

Answer (2)

Hints:

Since process is isobaric

$$W_{AB} = 2 \times R \times 200 = 400R$$

68. The work done on the gas in taking it from *D* to *A* is

- (1) +414R
- (2) -690R
- (3) +690R

Answer (1)

Hints:

Since process is isothermal

$$W_{DA} = 2.303 \times 2 \times R \times 300 \log \left(\frac{1}{2}\right)$$
$$= -415.8R \text{ J}$$

So, work done on the gas = 415.8R J

Remarks: The exact answer is 415.8R J but the option given in the question is approximate.

69. The net work done on the gas in the cycle ABCDA is

- (1) 276R
- (2) 1076R
- (3) 1904R

(4) Zero

Answer (1)

Hints:

$$W_{\text{total}} = W_{DA} + W_{BC}$$
, since $W_{AB} + W_{CD} = 0$
= 2.303 × 2 × R × 300 log $\left(\frac{1}{2}\right)$ + 2.303 × 2 × R × 500 log(2)
= 2.303 × 2R × 200 log(2)
= 277.2R

Remarks: The exact answer is 277.2 R but the option given in the question is approximate.

- 70. In an experiment the angles are required to be measured using an instrument. 29 divisions of the main scale exactly coincide with the 30 divisions of the vernier scale. If the smallest division of the main scale is half-a-degree (= 0.5°), then the least count of the instrument is
 - (1) Half minute



- (3) Half degree
- (4) One minute

Answer (4)

Hints:

29 Div of M.S = 30 Div of V.S

1 Div of $\Re S = \frac{29}{80}$ Div of M.S

Least count ≥ 1 Div of M.S - 1 Div V.S



$$\frac{1}{30} \times \frac{1}{2} = \frac{1}{60^{\circ}} = 1 \text{ minute}$$

71. A charge Q is placed at each of the opposite corners of a square. A charge q is placed at each of the other

two corners. If the net electrical force on Q is zero, then

- (1) -1
- (2) 1

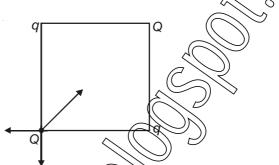
Answer (4)

Hints:

Either of Q or q must be negative for equilibrium.

$$\sqrt{2} \frac{kQq}{l^2} = \frac{kQ^2}{2l^2}$$

$$\frac{|Q|}{|q|} = 2\sqrt{2}$$



- 72. One kg of diatomic gas is at a pressure of 8×10^4 N/m². The density of the gas is 4 kg/m³. What is the energy of the gas due to its thermal motion?
 - (1) $5 \times 10^4 \text{ J}$

(3) $7 \times 10^4 \text{ J}$

Answer (1)

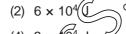
Hints:

$$E = \frac{f}{2}PV$$

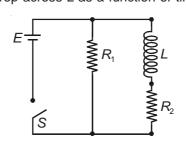
$$E = \frac{5}{2}PV$$

$$=\frac{5}{2}\times P\times \frac{m}{\rho}$$

$$=\frac{5\times8\times10^4\times1}{2\times4}=5\times10^4$$



73. An inductor of inductance $R_1 = 2 \Omega$ and $R_2 = 2 \Omega$ are connected to a battery of emf 12 V as shown in the figure. The internal resistance of the battery is negligible. The switch S is closed at t = 0. The potential drop across L as a function of time is

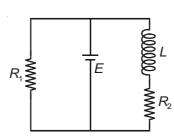


- (2) $6(1 e^{-t/0.2})$ V
- (4) $6e^{-5t}$ V

Answer (3)

Hints:

Given circuit is

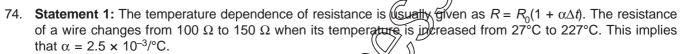


I through inductor as a function of time is

$$I = \frac{E}{R_2} \left\{ 1 - e^{-t/L/R_2} \right\}$$

$$V_L = L \frac{dI}{dt} = Ee^{-\frac{R_2 t}{L}}$$





Statement 2: $R = R_0(1 + \alpha \Delta t)$ is valid only when the change in the temperature ΔT is small and $\Delta R = (R - R_0) << R_0$.

- (1) Statement 1 is true, statement 2 is true; Statement 2 is the correct explanation of Statement 1
- (2) Statement 1 is true, Statement 2 is true; Statement 2 is not the correct explanation of Statement 1
- (3) Statement 1 is false, Statement 2 is true
- (4) Statement 1 is true, Statement 2 isofalse

Answer (3)

Hints:

As relation $R = R_0(1 + \alpha \Delta t)$ is valid only when $\Delta R < < R_0$.

Hence statement 1 is false and statement 2 is true.

- 75. The transition from the state $n \neq 4$ to n = 3 in a hydrogen like atom results in ultraviolet radiation. Infrared radiation will be obtained in the transition from
 - (1) $3 \to 2$

(2)
$$4 \to 2$$

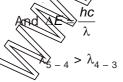
 $(3) \quad 5 \rightarrow 4$

(4)
$$2 \to 1$$

Answer (3)

Hints:

Energy gap between 4th and 3rd state is more than the gap between 5th and 4th state,



- 76. A mixture of light, consisting of wavelength 590 nm and an unknown wavelength, illuminates Young's double slit and gives rise to two overlapping interference patterns on the screen. The central maximum of both lights coincide. Further, it is observed that the third bright fringe of known light coincides with the 4th bright tringe of the unknown light. From this data, the wavelength of the unknown light is
 - (1) 885.0 nm

(2) 442.5 nm

(3) 776.8 nm

(4) 393.4 nm

Answer (2)

Hints:

As 4th bright fringe of unknown wavelength coincides with 3rd bright fringe of known wavelength

$$\Rightarrow \frac{4\lambda D}{d} = 3\frac{(590 \text{ nm})D}{d}$$

$$\Rightarrow \quad \lambda = \frac{3 \times 590}{4} = 442.5 \text{ nm}$$

- 77. A particle has an initial velocity of $3\hat{i} + 4\hat{j}$ and an acceleration of $0.4 \div 0.3\hat{j}$. Its speed after 10 s is
 - (1) $7\sqrt{2}$ units

(2) 7 units

(3) 8.5 units

(1) 10 unite

Answer (1)

Hints:

$$\vec{v} = \vec{u} + \vec{a}t$$

= $(3\hat{i} + 4\hat{j}) + 10(0.4\hat{i} + 0.3\hat{j})$

$$= (3\hat{i} + 4\hat{j}) + (4\hat{i} + 3\hat{j})$$

$$=7\hat{i}+7\hat{j}$$

$$|\vec{v}| = 7\sqrt{2}$$
 units

- 78. The surface of a metal is itterbinated with the light of 400 nm. The kinetic energy of the ejected photoelectrons was found to be 1.68 eV. The work function of the metal is
 - (1) 1.41 eV

(2) 1.51 eV

(3) 1.68 eV

(4) 3.09 eV

Answer (1)

Hints:

According to enstein photo electric equation



$$K_{\text{max}} = 1.42 \text{ ev}$$

- Three sound waves of equal amplitudes have frequencies (v 1), v, (v + 1). They superpose to give beats. The number of beats produced per second will be
 - (1) 3
- (2) 2

(3) 1

(4) 4

Answer (3)

If we assume that all the three waves are in same phase at t=0 they will be again in same (hase a

- 80. A motor cycle starts from rest and accelerates along a straight path at 2 m/s². At the starting point of the motor cycle there is a stationary electric siren. How far has the motor cycle gone when the driver hears the frequency of the siren at 94% of its value when the motor cycle was at rest? (Speed of sound = (330 m)s⁻³)
 - (1) 98 m
 - (2) 147 m
 - (3) 196 m
 - (4) 49 m

Answer (1)

Hints:

$$f' = f\left(\frac{v - v_0}{v}\right)$$

 $f = f\left(\frac{v - v_0}{v}\right)$ $\left(\begin{array}{c} v = \text{speed of sound} \\ v_0 = \text{speed of observer} \end{array}\right)$

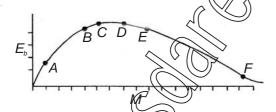
$$\Rightarrow$$
 0.94 = $1 - \frac{v_0}{v}$

$$\Rightarrow \frac{V_0}{V} = 0.06$$

$$\Rightarrow$$
 $v_0 = 19.8 \text{ m/s}$

⇒ Distance covered =
$$\frac{v_0^2}{2a}$$
 = 98 m

81.



The above is a plot of binding energy per nucleon E_b , against the nuclear mass M; A, B, C, D, E, F correspond to different nucled Consider four reactions :

- (ii) $C \rightarrow A + B + \varepsilon$
- (iii) $D + E \rightarrow F + \varepsilon$ (iv) $F \rightarrow D + E + \varepsilon$

where ε is the energy released? In which reactions is ε positive?

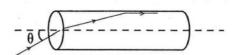
(2) (ii) and (iv)

(4) (i) and (iv)

Answer (4)

to reactions (i) & (iv), The B.E per nucleon increases. This makes nuclei more stable so energy will be Hints released in these reactions.

82. A transparent solid cylindrical rod has a refractive index of $\frac{2}{\sqrt{3}}$. It is surrounded by air. A light ray is incident at the mid-point of one end of the rod as shown in the figure.

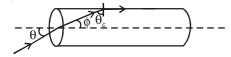


The incident angle θ for which the light ray grazes along the wall of the rod is

- (1) $\sin^{-1}\left(\frac{\sqrt{3}}{2}\right)$ (2) $\sin^{-1}\left(\frac{2}{\sqrt{3}}\right)$ (3) $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$

Answer (3)

Hints:



$$f + \theta_C = 90^\circ$$

$$\theta_C = \sin^-\left(\frac{1}{\mu}\right)$$

Using snell's law

$$\frac{\sin\theta}{\sin\phi} = \mu$$

$$\Rightarrow \sin\theta = \mu \cos\theta_C$$

$$\Rightarrow \sin\theta = \mu \sqrt{1 - \frac{1}{\mu^2}} = \sqrt{\mu^2 - 1}$$

$$\Rightarrow \theta = \sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

- 83. Two wires are made of the same material and have the same volume. However wire 1 has cross-sectional area A and wire 2 has cross-sectional area 3A. If the length of wire 1 increases by Δx on applying force F, how much force is needed to stretch wire 2 by the same amount?
 - (1) 4F



(3) 9F

(4) F

Answer (3)

Hints:

$$\frac{F}{A} = Y \frac{\Delta I}{I}$$

$$\Rightarrow F = X \frac{\Delta IA^2}{V} = Y \frac{\Delta IA^2}{V}$$



This question contains Statement-1 and statement-2. Of the four choices given after the statements, choose the one that best describes the two statements. **Statement 1:** For a charged particle moving from point P to point Q, the net work done by an electrostatic field on the particle is independent of the path connecting point P to point Q. Statement 2: The net work done by a conservative force on an object moving along a close (Too) is zero. (1) Statement-1 is true, Statement-2 is true; Statement-2 is the correct explanation of Statement-(2) Statment-1 is true, Statement-2 is true; Statement-2 is not the correct explanation of Statement-1. (3) Statement-1 is false, Statement-2 is true. (4) Statement-1 is true, Statement-2 is false. Answer (1) Hints: $W_e = -q (V_f - V_i)$ It depends on initial and final point only, because rectionation field is a conservative field. 85. The logic circuit shown below has the input waveforms 'A' and 'B' as shown. Pick out the correct output waveform. Input A Input B Output is: (2)(3)

Hint

$$y = \left(\overline{\overline{A} + \overline{B}}\right) = A \cdot B$$

The combination represents AND Gate Truth table.

Α	В	Υ
0	0	0
0	1	0
1	0	0
1	1	1

- If x, v and a denote the displacement, the velocity and the acceleration of a particle executing simple harmonic motion of time period T, then, which of the following does not change with time
 - (1) aT/x
 - (3) aT/v

- (2) $aT + 2\pi v$
- (4) $a^2T^2 + 4\pi$

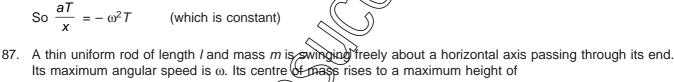
Answer (1)

Hint

$$x = A \sin(\omega t + \phi)$$

$$a = -A\omega^2 \sin(\omega t + \phi)$$

So
$$\frac{aT}{V} = -\omega^2 T$$



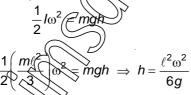
- $(3) \quad \frac{1}{6} \frac{I^2 \omega^2}{\sigma}$

 $(4) \quad \frac{1}{3} \frac{I^2 \omega^2}{\sigma}$

Answer (3)

Hints:

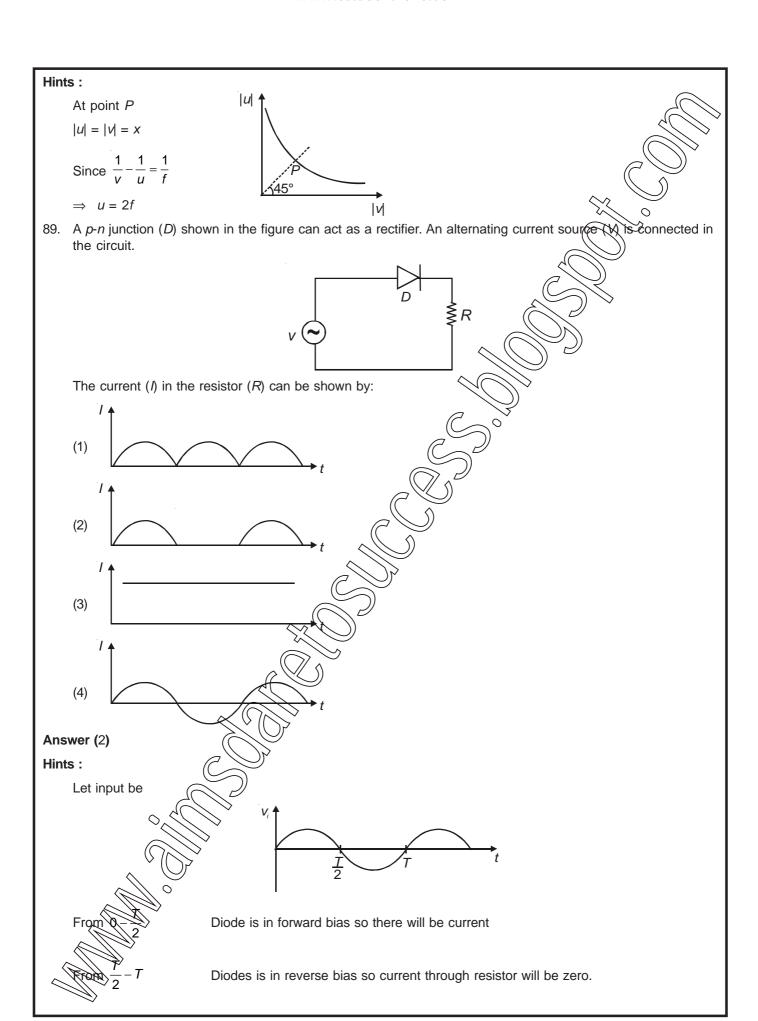
Loss in kinetic energy = Gain in potential energy



- In an optics (experiment, with the position of the object fixed, a student varies the position of a convex lens and for each position, the screen is adjusted to get a clear image of the object. A graph between the object distance u and the image distance v, from the lens, is plotted using the same scale for the two axes. A straight line passing through the origin and making an angle of 45° with the x-axis meets the experimental curve at The coordinates of P will be:
- (2) (f, f)
- (3) (4f, 4f)

(4) (2f, 2f)

Answer (4)



- 90. Let $\rho(r) = \frac{Q}{\pi R^4} r$ be the charge density distribution for a solid sphere of radius R and total charge Q for a point 'p' inside the sphere at distance r_1 from the centre of the sphere, the magnitude of electric field is:
 - $(1) \quad \frac{Q}{4\pi\varepsilon_0 r_1^2}$
- (2) $\frac{Q r_1^2}{4\pi\epsilon_0 R^4}$
- $(3) \quad \frac{Q r_1^2}{3\pi\varepsilon_0 R^4}$

(4) (

Answer (2)

Hints:

Consider a gaussian surface of radius r_1

$$\oint \vec{E}. \ \vec{dA} = \frac{Q_{en}}{\varepsilon_0}$$

$$E4\pi r_1^2 = \frac{1}{\varepsilon_0} \int \rho \ dV$$

$$=\frac{1}{\varepsilon_0}\int_0^{r_1}\frac{Q\ r}{\pi R^4}\ 4\pi r^2\ dr$$

$$E = \frac{Qr_1^4}{4\pi\epsilon_0 R^4 r_1^2} = \frac{Qr_1^2}{4\pi\epsilon_0 R^4}$$

