Note: For the benefit of the students, specially the aspiring ones, the question of JEE(Main), 2016 are also given in this booklet. Keeping the interest of students studying in class XI, the questions based on topics from class XI have been marked with '*', which can be attempted as a test.

FIITJEE Solutions to JEE(Main)-2016

PAPER – 1 CHEMISTRY, MATHEMATICS & PHYSICS

Important Instructions:

- 1. Immediately fill in the particular on this page of the Test Booklet with *only Blue / Black Ball Point Pen* provided by the Board.
- 2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
- 3. The test is of **3 hours** duration.
- 4. The Test Booklet consists of 90 questions. The maximum marks are 360.
- 5. There are *three* parts in the question paper A, B, C consisting of **Chemistry**, **Mathematics** and **Physics** having 30 questions in each part of equal weightage. Each question is allotted **4** (four) marks for each correct response.
- 6. Candidates will be awarded marks as started above in instruction No. 5 for correct response of each question. ¼ (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from that total score will be made if no response is indicated for an item in the answer sheet.
- 7. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
- 8. For writing particulars / marking responses on *Side-1* and *Side-2* of the Answer Sheet use *only Blue/Black Ball Point Pen* provided by the Board.
- 9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. except the Admit Card inside the examination room/hall.
- 10. Rough work is to be done on the space provided for this purpose in the Test Booklet only. This space is given at the bottom of each page.
- 11. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room / Hall. *However, the candidates are allowed to take away this Test Booklet with them.*
- 12. The CODE for this Booklet is **F**. Make sure that the CODE printed on **Side-2** of the Answer Sheet and also tally the serial number of the Test Booklet and Answer Sheet are the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
- 13. Do not fold or make any stray mark on the Answer Sheet.

PART A – CHEMISTRY

1*. A stream of electrons from a heated filament was passed between two charged plates kept at a potential difference *V* esu. If *e* and *m* are charge and mass of an electron, respectively, then the value of h/λ (where λ is wavelength associated with electron wave) is given by :

- (1) 2meV (2) \sqrt{meV}
- $(3) \quad \sqrt{2meV} \qquad (4) \quad meV$

Sol.

(3)

 $\lambda = \frac{h}{mv}$ $= \frac{h}{\sqrt{2m(KE)}}$ $\therefore \quad \frac{h}{\lambda} = \sqrt{2meV}$

2.

Sol.

3.

4.

2-chloro-2-methylpentane on reaction with sodium methoxide in methanol yields :

CH₃ $C_2H_5CH_2C \longrightarrow OCH_3 \qquad C_2H_5CH_2C \longrightarrow CH_2 CH_3 \qquad C_3H_5CH_2C \longrightarrow CH_3 CH_3$ CH₃ C₂H₅CH CH₃ (a) (b) (c) (1) (a) and (c) (c) only (3) (a) and (b) (4)All of these (4) via $S_N 1$ and E_2 mechanisms Which of the following compounds is metallic and ferromagnetic ? (1) CrO_2 (2) VO₂ (3) MnO₂ (4) TiO_2

- *Sol.* (1)
 - CrO₂ is metallic and ferromagnetic.
 - Which of the following statements about low density polythene is FALSE ?
 - (1) It is a poor conductor of electricity.
 - (2) Its synthesis requires dioxygen or a peroxide initiator as a catalyst.
 - (3) It is used in the manufacture of buckets, dust-bins etc.
 - (4) Its synthesis requires high pressure.

Sol.

(3)

HDPE is used in making buckets and dustbins

- 5. For a linear plot of log (x/m) versus log p in a Freundlich adsorption isotherm, which of the following statements is correct ? (k and n are constants)
 - (1) 1/n appears as the intercept.
 - (3) $\log(1/n)$ appears as the intercept.
- (2) Only 1/n appears as the slope
- (4) Both k and 1/n appear in the slope term.

Sol. (2) $\frac{x}{m} = kp^{\frac{1}{n}}$ $\log \frac{x}{m} = \log k + \frac{1}{n} \log p$ The heats of combustion of carbon and carbon monoxide are -393.5 and -283.5 kJ mol⁻¹, respectively. The 6*. heat of formation (in kJ) of carbon monoxide per mole is : (1) 676.5 (2) -676.5(3) -110.5(4) 110.5 Sol. (3) $C + O_2 \longrightarrow CO_2 \qquad \dots (1)$ $CO + \frac{1}{2}O_2 \longrightarrow CO_2 \qquad ...(2)$ $\Delta H_1 \Rightarrow -393.5 \text{ kJ} / \text{mole}$ $\Delta H_2 \Rightarrow -283.5 \text{ kJ} / \text{mole}$ $C + \frac{1}{2}O_2 \longrightarrow CO$ $\Delta_{\rm f}\,H_{\rm (CO,\,g)}=\Delta H_1-\Delta H_2$ \Rightarrow -393.5 -(-283.5) = -393.5 + 283.5 \Rightarrow -110 kJ/mole 7. The hottest region of Bunsen flame shown in the figure below is : region 4 region 3 region 2 region 1 (1) region 2 (2) region 3 (3) region 4 (4) region 1 Sol. (1) region 2 Which of the following is an anionic detergent ? 8. (1) Sodium lauryl sulphate (2) Cetyltrimethyl ammonium bromide (3) Glyceryl oleate (4) Sodium stearate Sol. (1) Sodium ⁺(lauryl sulphate)⁻ is an anionic detergent. 9. 18 g glucose (C₆H₁₂O₆) is added to 178.2 g water. The vapour pressure of water (in torr) for this aqueous solution is : (1) 76.0 (2) 752.4 (3) 759.0 (4) 7.6 FIITJEE Ltd., FIITJEE House, 29-A, Kalu Sarai, Sarvapriya Vihar, New Delhi -110016, Ph 46106000, 26569493, Fax 26513942

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Sol.

(2)

 $n_{C_6H_{12}O_6} = 0.1$ $n_{H_2O} = \frac{178.2}{18} = 9.9$ $\frac{p^0 - p}{p^0} \Rightarrow \frac{0.1}{10}$ $p^0 - p \Rightarrow \frac{0.1}{10} \times 760 = 7.6$ $p = p^0 - 7.6$ = 760 - 7.6 = 752.4 torr

10*. The distillation technique most suited for separating glycerol from spent-lye in the soap industry is :

- (1) Fractional distillation
 (3) Distillation under reduced pressure
- (2) Steam distillation(4) Simple distillation

Sol.

(3)

- Glycerol decomposes before its boiling point.
- 11*. The species in which the N atom is in a state of *sp* hybridization is :
 - (1) NO_2^- (2) NO_3^- (3) NO_2 (4) NO_2^+
- *Sol.* (4)

 $O = \overset{\oplus}{N} = O$

- 12. Decomposition of H_2O_2 follows a first order reaction. In fifty minutes the concentration of H_2O_2 decreases from 0.5 to 0.125 M in one such decomposition. When the concentration of H_2O_2 reaches 0.05 M, the rate of formation of O_2 will be :
 - (1) $6.93 \times 10^{-4} \text{ mol min}^{-1}$
 - (3) $1.34 \times 10^{-2} \text{ mol min}^{-1}$

- (2) 2.66 Lmin^{-1} at STP
- (4) $6.93 \times 10^{-2} \text{ mol min}^{-1}$



$$H_2O_2 \longrightarrow H_2O + \frac{1}{2}O_2$$

$$2t_{1/2} = 50 \text{ mins}$$

$$t_{1/2} = 25 \text{ mins}$$

$$\therefore k = \frac{0.693}{25}$$

$$-\frac{d[H_2O_2]}{dt} = \frac{d[O_2]}{dt} \times 2$$

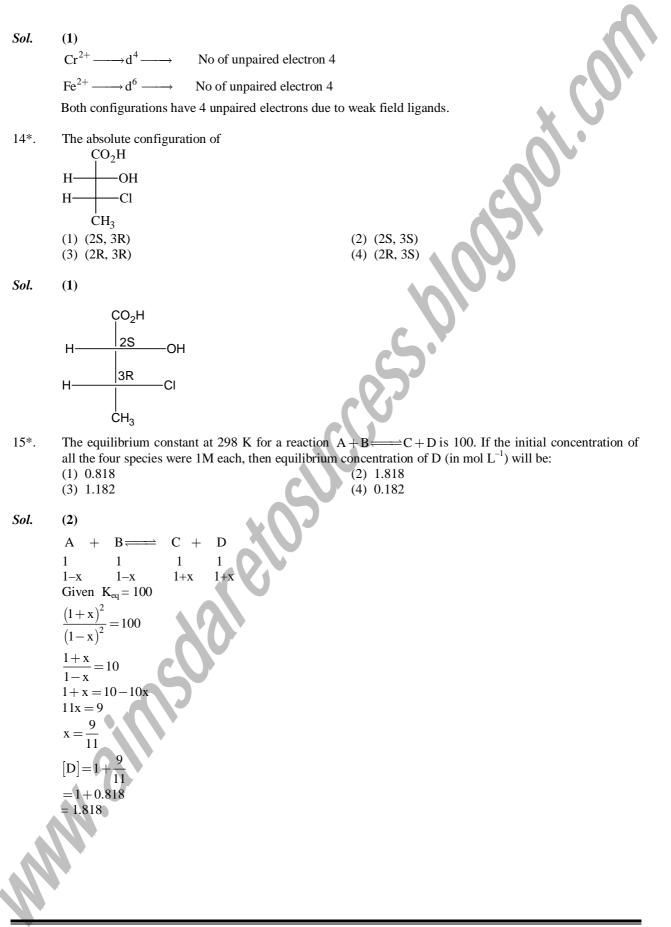
$$\therefore \frac{d[O_2]}{dt} = \frac{1}{2} \times \frac{0.693}{25} \times 0.05$$

$$= 6.93 \times 10^{-4}$$

13. The pair having the same magnetic moment is : [At. No.: Cr = 24, Mn = 25, Fe = 26, Co = 27] (1) $[Cr(H_2O)_6]^{2+}$ and $[Fe(H_2O)_6]^{2+}$ (3) $[CoCl_4]^{2-}$ and $[Fe(H_2O)_6]^{2+}$

 $\begin{array}{ll} (2) & \left[Mn(H_2O)_6\right]^{2+} \text{ and } \left[Cr(H_2O)_6\right]^{2+} \\ (4) & \left[Cr(H_2O)_6\right]^{2+} \text{ and } \left[CoCl_4\right]^{2-} \end{array}$

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- 16. Which one of the following ores is best concentrated by froth floatation method? (1) Siderite (2) Galena
 - (3) Malachite

(4) Magnetite

(4) C₃H₆

- (2) Sol.
 - Galena (PbS) is a sulphide ore.
- At 300 K and 1 atm, 15 mL of a gaseous hydrocarbon requires 375 mL air containing 20% O2 by volume 17*. for complete combustion. After combustion the gases occupy 330 mL. Assuming that the water formed is in liquid form and the volumes were measured at the same temperature and pressure, the formula of the hydrocarbon is: (2) C_4H_8
 - (1) C_3H_8 (3) C₄H₁₀

1

Sol. None

> Volume of $O_2 = 375 \times \frac{20}{100} = 75 \text{ ml}$ Volume of gaseous hydrocarbon = 15 ml

$$C_{x}H_{y} + \left(x + \frac{y}{4}\right)O_{2} \longrightarrow xCO_{2} + \frac{y}{2}H_{2}O(\ell)$$

$$H_{5}\left(x + \frac{y}{4}\right) = 75 \qquad \dots (1)$$

 $x + \frac{y}{-} = 5$

Excess air = 375 - 75 = 300 $300 + volume of CO_2 = 330$ Volume of $CO_2 = 30$ 15 x = 30 $\mathbf{x} = 2$ (Correct option is not given)

$$2 + \frac{y}{4} = 5$$

$$\frac{y}{2} = 3$$

$$4 y = 12$$

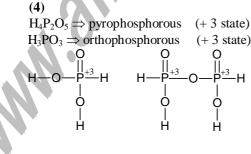
C₂H₁₂ (not possible)

Hence No answer is correct.

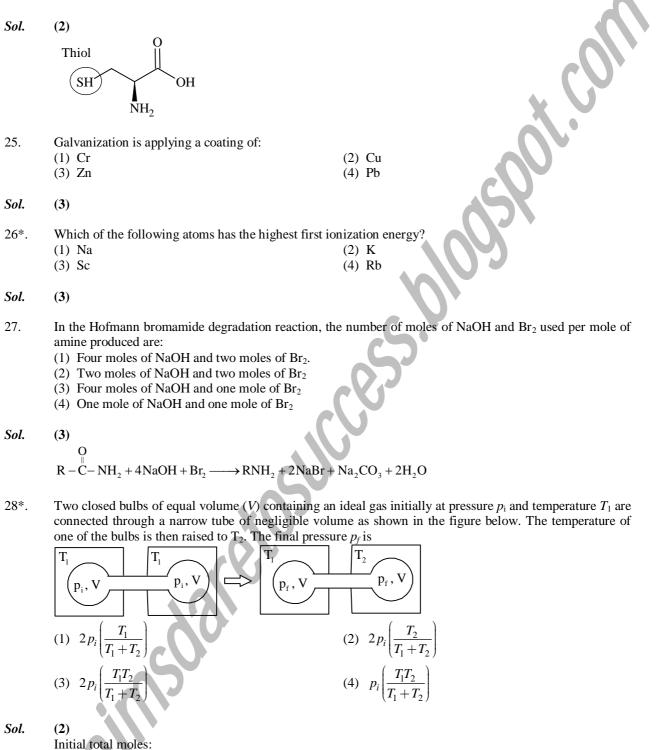
However, considering the equation no. 1 alone, if we put x and y values, 3 and 8 respectively, then equation no. 1 is satisfied and answer will be C₃H₈.

- 18. The pair in which phosphorous atoms have a formal oxidation state of +3 is:
 - (1) Pyrophosphorous and hypophosphoric acids
 - (2) Orthophosphorus and hypophosphoric acids
 - (3) Pyrophosphorous and pyrophosphoric acids
 - (4) Orthophosphorous and pyrophosphorous acids

Sol.



19.		m? s[Co(en) ₂ Cl ₂]Cl NH ₃) ₃ Cl ₃]
Sol.	$ \begin{bmatrix} 1 \\ en \\ Cl \\ C$	
20.	The reaction of zinc with dilute and concentrated nitric acid, re (1) NO ₂ and NO (2) NO a (3) NO ₂ and N ₂ O (4) N ₂ O	
Sol.	(4) $Zn + 4HNO_3 \longrightarrow Zn(NO_3)_2 + 2H_2O + 2NO_2 \uparrow$ $4Zn + 10HNO_3 \longrightarrow 4Zn(NO_3)_2 + N_2O \uparrow + 5H_2O$ dil.	
21*.	 Which one of the following statements about water is FALSE? (1) Water can act both as an acid and as a base. (2) There is extensive intramolecular hydrogen bonding in the (3) Ice formed by heavy water sinks in normal water (4) Water is oxidized to oxygen during photosynthesis 	
Sol.	(2) Ice shows intermolecular H – bonding.	
22*.	The concentration of fluoride, lead, nitrate and iron in a waterto be 1000 ppb, 40 ppb, 100 ppm and 0.2 ppm, respectively.high concentration of :(1) Lead(2) Nitra(3) Iron(4) Fluo	This water is unsuitable for drinking due to ate
Sol.	(2) Maximum limit of nitrate in potable water is 50 ppm.	
23*.		tess of air are, respectively: D_2 , Na_2O_2 and KO_2 D_2 , Na_2O and KO_2
Sol.	(3)	
24.	Thiol group is present in :(2) Cyst(3) Methionine(4) Cyto	



Initial total moles: $n = \frac{p_i V}{RT_1} + \frac{p_i V}{RT_1} = \frac{2p_i V}{RT_1} \qquad \dots (1)$ Final total moles: $n = \frac{p_f V}{RT_1} + \frac{p_f V}{RT_2} \qquad \dots (2)$ Equating the two:

$$\begin{split} &\frac{2p_{i}}{T_{1}} = \frac{p_{f}}{T_{1}} + \frac{p_{f}}{T_{2}} \\ &p_{f} = \frac{2p_{i}}{T_{1}} \times \frac{T_{1}T_{2}}{(T_{1} + T_{2})} \\ &p_{f} = 2p_{i} \times \frac{T_{2}}{T_{1} \times T_{2}} \end{split}$$

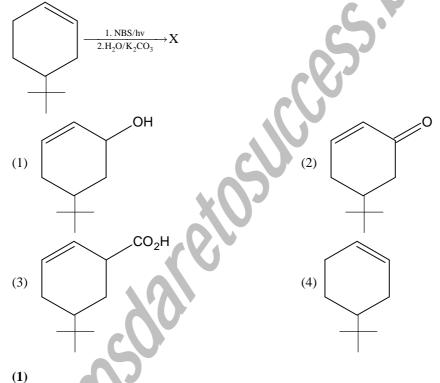
29*. The reaction of propene with HOCl ($Cl_2 + H_2O$) proceeds through the intermediate: (1) $CH_3 - CH^+ - CH_2 - Cl$ (2) $CH_3 - CH(OH) - CH_2^+$ (3) $CH_3 - CHCl - CH_2^+$ (4) $CH_3 - CH^+ - CH_2 - OH$

Sol.

(1)

$$CH_3 - CH = CH_2 + Cl^{\oplus} \longrightarrow CH_3 - CH_2 - CH_2 Cl$$
 (Markovnikov's addition)

30*. The product of the reaction given below is:





PART B – MATHEMATICS

*31. Two sides of a rhombus are along the lines, x - y + 1 = 0 and 7x - y - 5 = 0. If its diagonals intersect at (-1, -2), then which one of the following is a vertex of this rhombus?

(1)
$$(-3, -8)$$

(2) $\left(\frac{1}{3}, -\frac{8}{3}\right)$
(3) $\left(-\frac{10}{3}, -\frac{7}{3}\right)$
(4) $(-3, -9)$

Sol.

(2)

Remaining two sides of rhombus are x - y - 3 = 0 and 7x - y + 15 = 0. So on solving, we get vertices as $\left(\frac{1}{3}, -\frac{8}{3}\right)$, (1, 2), $\left(-\frac{7}{3}, -\frac{4}{3}\right)$ and $\left(-3, -6\right)$

*32. If the 2nd, 5th and 9th terms of a non-constant A.P. are in G.P., then the common ratio of this G.P. is:

(2)

(1)	$\frac{4}{3}$			
(3)	$\frac{7}{4}$			

Sol.

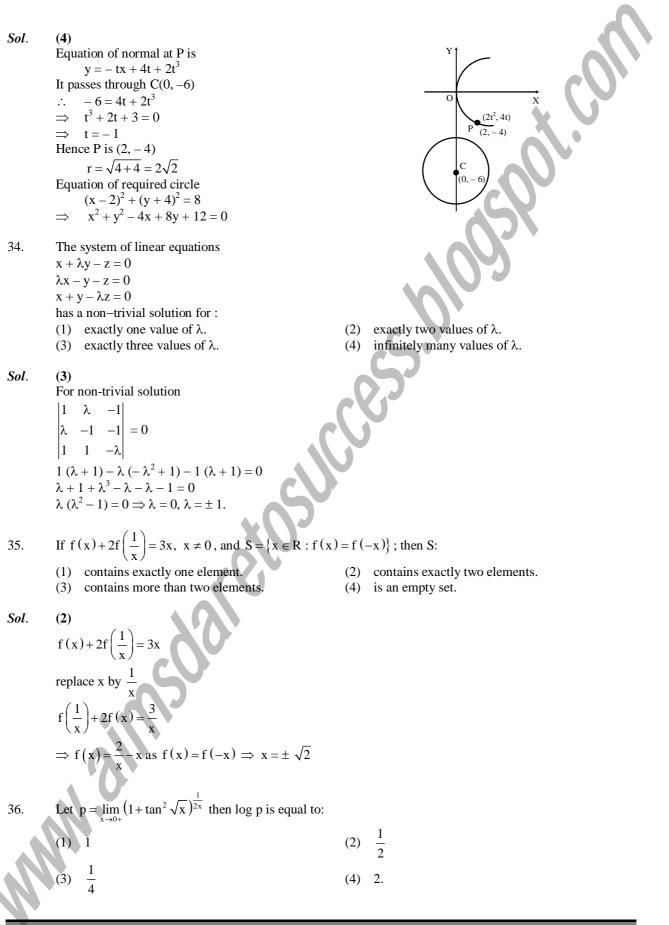
(1)

Let the G.P. be a, ar, ar² and terms of A.P. are A + d, A + 4d, A + 8d then $\frac{ar^2 - ar}{ar - a} = \frac{(A + 8d) - (A + 4d)}{(A + 4d) - (A + d)} = \frac{4}{3}$ $\Rightarrow r = \frac{4}{3}$.

Alternate Solution:

Let AP is a, a + d, a + 2d 2^{nd} , 5^{th} and 9^{th} terms a + d, a + 4d, a + 8d are in GP $\Rightarrow (a + 4d)^2 = (a + d)(a + 8d)$ $\Rightarrow d(8d - a) = 0 \Rightarrow 8d = a \text{ as } d \neq 0$ Hence common ratio of GP $\frac{a+4d}{a+d} = \frac{8d+4d}{8d+d} = \frac{12d}{9d} = \frac{4}{3}$.

- *33. Let P be the point on the parabola, $y^2 = 8x$ which is at a minimum distance from the centre C of the circle, $x^2 + (y + 6)^2 = 1$. Then the equation of the circle, passing through C and having its centre at P is:
 - (1) $x^{2} + y^{2} x + 4y 12 = 0$ (2) $x^{2} + y^{2} - \frac{x}{4} + 2y - 24 = 0$ (3) $x^{2} + y^{2} - 4x + 9y + 18 = 0$ (4) $x^{2} + y^{2} - 4x + 8y + 12 = 0$



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Sol. (2)

$$p = \lim_{x \to 0^{+}} \left(1 + \tan^2 \sqrt{x} \right)^{\frac{1}{2x}}$$
$$= e^{\lim_{x \to 0^{+}} \frac{\tan^2 \sqrt{x}}{2x}}$$
$$= e^{\lim_{x \to 0^{+}} \frac{1}{2} \left(\frac{\tan \sqrt{x}}{\sqrt{x}} \right)^2}$$
$$p = e^{\frac{1}{2}}$$

A value of θ for which $\frac{2+3i\sin\theta}{1-2i\sin\theta}$ is purely imaginary, is: *37.

 \Rightarrow product of slopes taken as in xy plane is – 1

(1)
$$\frac{\pi}{6}$$
 (2)
(3) $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$ (4)

Y (2, 3i sinθ) Ń $(1, -2i \sin \theta)$

(3) $\frac{2+3i\sin\theta}{1-2i\sin\theta} \text{ is purely imaginary } \in \operatorname{Arg} \left($

Sol.

Sol.

Alternate Solution:

 $\Rightarrow \frac{3\sin\theta}{2} \cdot \frac{-2\sin\theta}{1} = -1$

 $\Rightarrow \sin^2 \theta = \frac{1}{3}, \ \theta = \sin^{-1} \left(\frac{1}{\sqrt{3}} \right).$

$$\frac{2+3i\sin\theta}{1-2i\sin\theta} = \frac{2-6\sin^2\theta+7i\sin\theta}{1+4\sin^2\theta}$$
 is purely imaginary
$$\Rightarrow \frac{2-6\sin^2\theta}{1+4\sin^2\theta} = 0 \Rightarrow 6\sin^2\theta = 2.$$

The eccentricity of the hyperbola whose length of the latus rectum is equal to 8 and the length of its *38. conjugate axis is equal half of the distance between its foci, is:

 $\left(\frac{2+3i\sin\theta}{1-2i\sin\theta}\right)$

sin

 $\frac{\pi}{3}$

(1)
$$\frac{4}{\sqrt{3}}$$

(2) $\frac{2}{\sqrt{3}}$
(3) $\sqrt{3}$
(4) $\frac{4}{3}$
(2)
Given, $\frac{2b^2}{a} = 8$ and $2b = \frac{1}{2}(2ae)$
 $2b = ae$
 $4b^2 = a^2 \cdot e^2$
 $3e^2 = 4 \implies e = \frac{2}{\sqrt{3}}$

*39. If the standard deviation of the numbers 2, 3, a and 11 is 3.5, then which of the following is true? (1) $3a^2 - 32a + 84 = 0$ (2) $3a^2 - 34a + 91 = 0$ (3) $3a^2 - 23a + 44 = 0$ (4) $3a^2 - 26a + 55 = 0$

(2)

Sol. (1)

$$\overline{\mathbf{x}} = \frac{2+3+a+11}{4} = \frac{a}{4} + 4$$

$$\sigma = \sqrt{\sum \frac{x_i^2}{n} - (\overline{\mathbf{x}})^2}$$

$$3.5 = \sqrt{\frac{4+9+a^2+121}{4} - \left(\frac{a}{4}+4\right)^2}$$

$$\Rightarrow \frac{49}{4} = \frac{4(134+a^2) - \left(a^2+256+32a\right)}{16}$$

$$\Rightarrow 3a^2 - 32a + 84 = 0$$

40. The integral
$$\int \frac{2x^{12} + 5x^9}{(x^5 + x^3 + 1)^3} dx$$
 is equal to:
(1) $\frac{x^{10}}{2(x^5 + x^3 + 1)^2} + C$
(3) $\frac{-x^{10}}{2(x^5 + x^3 + 1)^2} + C$

where C is an arbitrary constant.

Sol.

(1)

$$I = \int \frac{\left(\frac{2}{x^{3}} + \frac{5}{x^{6}}\right)}{\left(1 + \frac{1}{x^{2}} + \frac{1}{x^{5}}\right)^{3}} dx, \quad \text{let } 1 + \frac{1}{x^{2}} + \frac{1}{x^{5}}$$

Hence $I = \frac{x^{10}}{2\left(x^{5} + x^{3} + 1\right)^{2}} + c.$

41. If the line, $\frac{x-3}{2} = \frac{y+2}{-1} = \frac{z+4}{3}$ lies in the plane, lx + my - z = 9, then $l^2 + m^2$ is equal to: (1) 18 (3) 2 (4) 26

Sol.

(3) As line $\frac{x-3}{2} = \frac{y+2}{-1} = \frac{z+4}{3}$ lies in plane $\ell x + my - z = 9$ So $2\ell - m - 3 = 0$ (as line is perpendicular to normal of the plane) (1) Also point (3, -2, -4) lies in plane So $3\ell - 2m - 5 = 0$ (2) From equation (1) and (2), we get $\ell = 1$, m = -1So $\ell^2 + m^2 = 2$

Q (2, -2)

*42. If
$$0 \le x < 2\pi$$
, then the number of real values of x, which satisfy the equation
 $\cos x + \cos 2x + \cos 3x + \cos 4x = 0$ is:
(1) 5 (2) 7
(3) 9 (4) 3
Sol. (2)
 $2\cos \frac{5x}{2} \cdot \cos \frac{3x}{2} + 2\cos \frac{5x}{2} \cdot \cos \frac{x}{2} = 0$
 $\Rightarrow \cos \frac{5x}{2} \cdot \left(2 \cdot \cos x \cdot \cos \frac{x}{2}\right) = 0$
 $\Rightarrow \frac{x}{2} = (2n+1)\frac{\pi}{2}, x = (2m+1)\frac{\pi}{2}, \frac{5x}{2} = (2k+1)\frac{\pi}{2}, \text{ (where n, m, k \in Z)}$
 $\Rightarrow x = (2n+1)\pi, x = (2m+1)\frac{\pi}{2}, x = (2k+1)\frac{\pi}{5}$
 $\Rightarrow x = \pi, \frac{\pi}{2}, \frac{3\pi}{2}, \frac{\pi}{5}, \frac{3\pi}{5}, \frac{7\pi}{5}, \frac{9\pi}{5}.$
43. The area (in sq. units) of the region $\{(x, y): y^2 \ge 2x \text{ and } x^2 + y^2 \le 4x, x \ge 0, y \ge 0\}$ is:
(1) $\pi - \frac{8}{3}$ (2) $\pi - \frac{4\sqrt{2}}{3}$
(3) $\frac{\pi}{2} - \frac{2\sqrt{2}}{3}$ (4) $\pi - \frac{4}{3}$
Sol. (1)
The point of intersection of the curve $x^2 + y^2 = 4x$
 $y^2 = 2x \text{ are } (0, 0) \text{ and } (2, 2) \text{ for } x \ge 0 \text{ and } y \ge 0$
So required area $= \frac{1}{4}\pi \times 4 - \int_{0}^{2}\sqrt{2x} dx$
 $= \pi - \sqrt{2} \cdot \frac{2}{3} [x^{3/2}]_{0}^{2}$
 $= \pi - \frac{8}{3}$

Let \vec{a} , \vec{b} and \vec{c} be three unit vectors such that $\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\sqrt{3}}{2} (\vec{b} + \vec{c})$. If \vec{b} is not parallel to \vec{c} , then the 44. angle between \vec{a} and \vec{b} is:

(1)
$$\frac{\pi}{2}$$

(3) $\frac{5\pi}{6}$
(2) $\frac{2\pi}{3}$
(4) $\frac{3\pi}{4}$

Sol. (3)

$$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\sqrt{3}}{2} (\vec{b} + \vec{c})$$

 $\Rightarrow (\vec{a} \cdot \vec{c}) \vec{b} - (\vec{a} \cdot \vec{b}) \vec{c} = \frac{\sqrt{3}}{2} (\vec{b} + \vec{c})$

$$\Rightarrow \vec{a} \cdot \vec{c} = \frac{\sqrt{3}}{2} \text{ and } \vec{a} \cdot \vec{b} = -\frac{\sqrt{3}}{2}$$
$$\Rightarrow \cos \theta = -\frac{\sqrt{3}}{2} \quad \text{where } \theta \text{ is angle between } \vec{a} \& \vec{b}$$
$$\therefore \theta = \frac{5\pi}{6}.$$

45. A wire of length 2 units is cut into two parts which are bent respectively to form a square of side = x units and a circle of radius = r units. If the sum of the areas of the square and the circle so formed is minimum, then:

(1)
$$(4 - \pi)x = \pi r$$

(3) $2x = r$

(2) x = 2r(4) $2x = (\pi + 4)r$

Sol.

(2)

$$f(x) = x^{2} + \frac{(1-2x)^{2}}{\pi} (As r = \frac{1-2x}{\pi})$$

$$f'(x) = 2x - \frac{4(1-2x)}{\pi}$$

$$f''(x) = 2 + \frac{8}{\pi} > 0$$
For minimum value of sum of area f'(x) = 0

$$x = \frac{2}{\pi + 4} \implies r = \frac{1}{\pi + 4}$$
$$\implies x = 2r.$$

The distance of the point (1, -5, 9) from the plane x - y + z = 5 measured along the line x = y = z is: 46.

(1) $10\sqrt{3}$

(3)
$$\frac{20}{3}$$

 $\frac{10}{\sqrt{3}}$ (2) $3\sqrt{10}$ (4)



47.

Sol.

If a curve y = f(x) passes through the point (1, -1) and satisfies the differential equation, y(1 + xy) dx = xdy, then is equal to: $\frac{2}{5}$ (2) $\frac{2}{5}$

(4)

Sol. (3)

$$y (1 + xy) dx = xdy$$

$$\frac{xdy - ydx}{y^{2}} = xdx$$

$$\int -d\left(\frac{x}{y}\right) = \int xdx$$

$$-\frac{x}{y} = \frac{x^{2}}{2} + c \text{ as } y(1) = -1 \Rightarrow c =$$
Hence $y = \frac{-2x}{x^{2} + 1} \Rightarrow f\left(-\frac{1}{2}\right) = \frac{4}{5}$

*48. If the number of terms in the expansion of $\left(1-\frac{2}{x}+\frac{4}{x^2}\right)^n$, $x \neq 0$, is 28, then the sum of the coefficients of all the terms in this expansion, is:

	<i>'</i>	243 64	
--	----------	-----------	--

 $\frac{1}{2}$

```
Sol.
```

(3)

Total number of terms $=^{n+2} C_2 = 28$

$$(n+2)(n+1) = 56$$

 $n = 6$

Sum of coefficients = $(1 - 2 + 4)^n$

$$=3^6 = 729$$

[*Note: In the solution it is considered that different terms in the expansion having same powers are not merged, as such it should be a bonus question.]

49. Consider

Sol.

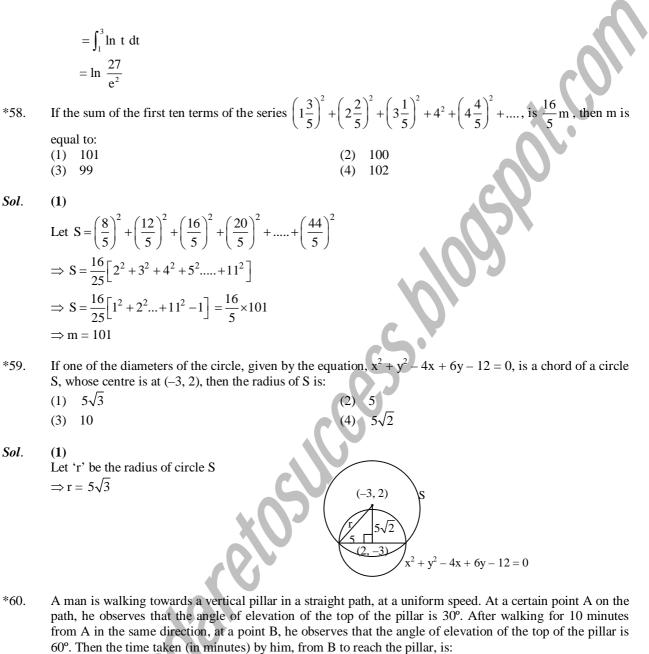
Formula
f (x) =
$$\tan^{-1}\left(\sqrt{\frac{1+\sin x}{1-\sin x}}\right)$$
, $x \in \left(0, \frac{\pi}{2}\right)$. A normal to $y = f(x)$ at $x = \frac{\pi}{6}$ also passes through the point:
(1) $\left(0, \frac{2\pi}{3}\right)$ (2) $\left(\frac{\pi}{6}, 0\right)$
(3) $\left(\frac{\pi}{4}, 0\right)$ (4) $(0, 0)$
(1)
f (x) = $\tan^{-1}\sqrt{\frac{1+\sin x}{1-\sin x}}$, where $x \in \left(0, \frac{\pi}{2}\right)$
= $\tan^{-1}\left(\left|\tan\left(\frac{\pi}{4}+\frac{x}{2}\right)\right|\right)$
 $\Rightarrow f(x) = \frac{\pi}{4}+\frac{x}{2}$, $f\left(\frac{\pi}{6}\right)=\frac{\pi}{3}$
f'(x) = $\frac{1}{2}$
Equation of normal is
 $y - \frac{\pi}{3} = -2\left(x - \frac{\pi}{6}\right)$
It passes through $\left(0, \frac{2\pi}{3}\right)$.

For $x \in \mathbf{R}$, $f(x) = |\log 2 - \sin x|$ and g(x) = f(f(x)), then:

50.

(1) $g'(0) = \cos(\log 2)$ (2) $g'(0) = -\cos(\log 2)$ (3) g is differentiable at x = 0 and $g'(0) = -\sin(\log 2)$ (4) g is not differentiable at x = 0Sol. (1) At x = 0, f is differential and $f'(0) = -\cos 0 = -1$ $g'(0) = f'(f(0)) \cdot f'(0)$ $= -\cos(\log 2) \times -1$ (at x = 0, f(0) = log 2) $= \cos(\log 2)$ Let two fair six-faced dice A and B be thrown simultaneously. If E_1 is the event that die A shows up four, 51. E_2 is the event that die B shows up two and E_3 is the event that the sum of numbers on both dice is odd, then which of the following statements is NOT true? (2) E_1 and E_3 are independent. (1) E_2 and E_3 are independent. (3) E_1 , E_2 and E_3 are independent. (4) E_1 and E_2 are independent. Sol. (3) $P(E_1) = \frac{1}{6}, P(E_2) = \frac{1}{6}, P(E_3) = \frac{1}{2}$ Also $P(E_1 \cap E_2) = \frac{1}{36}$, $P(E_2 \cap E_3) = \frac{1}{12}$, $P(E_1 \cap E_3)$ And $P(E_1 \cap E_2 \cap E_3) = 0 \neq P(E_1) \cdot P(E_2) \cdot P(E_3)$ Hence, E_1 , E_2 , E_3 are not independent. If $A = \begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix}$ and A adj $A = A A^{T}$, then 5a + b is equal to: 52. (1) 5 (2)4 (3) 13 (4) - 1(1) Sol. A adj A = |A| I_n = $\begin{bmatrix} 5a & -b \\ 3 & 2 \end{bmatrix} \begin{bmatrix} 5a & 3 \\ -b & 2 \end{bmatrix}$ $\Rightarrow (10a+3b) \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 25a^2+b^2 & 15a-2b \\ 15a-2b & 13 \end{bmatrix}$ \Rightarrow 15a - 2b = 0 and 10a + 3b = 13 $\Rightarrow 5a + b = 5 \times \frac{2}{5} + 3 = 5.$ The Boolean Expression $(p \land q) \lor (\neg p \land q)$ is equivalent to: *53. (1) $p \wedge q$ (2) $p \lor q$ (3) $p \vee \sim q$ (4) $\sim p \wedge q$ (2) Sol. $(p \land \neg q) \lor q \lor (\neg p \land q)$ $\equiv \{ (p \lor q) \land (\neg q \lor q) \} \lor (\neg p \land q)$ $\equiv \{(p \lor q) \land T\} \lor (\sim p \land q)$ $\equiv (\mathbf{p} \lor \mathbf{q}) \lor (\mathbf{\sim} \mathbf{p} \land \mathbf{q})$ $= \{ (p \lor q) \lor \sim p \} \land (p \lor q \lor q) \}$ $\equiv T \land (p \lor q)$ $\equiv p \lor q$

*54. The sum of all real values of x satisfying the equation $(x^2 - 5x + 5)^{x^2 + 4x - 60} = 1$ is (1) -4 (2) 6 (3) 5 (4) 3 Sol. (4) Either $x^2 - 5x + 5 = 1$ or $x^2 + 4x - 60 = 0$ x = 1, 4 or x = -10, 6Also $x^2 - 5x + 5 = -1$ and $x^2 + 4x - 60 \in$ even number x = 2, 3 For $x = 3 x^2 + 4x - 60$ is odd Total solutions are x = 1, 4, -10, 6, 2 \Rightarrow Sum = 3 The centres of those circles which touch the circle, $x^2 + y^2 - 8x - 8y - 4 = 0$, externally and also touch the *55. x-axis, lie on: (1) an ellipse which is not a circle. (2) a hyperbola. (4) a circle. (3) a parabola. Sol. (3) Let (h, k) be the centre of the circle which touch x-axis and $x^2 + y^2 - 8x - 8y - 4 = 0$ externally. Radius of that circle is $|\mathbf{k}|$ \Rightarrow $(h-4)^{2} + (k-4)^{2} = (|k|+6)^{2}$ \Rightarrow $\Rightarrow \quad x^2 - 8x - 20y - 4 = 0 \text{ if } y \ge 0$ and $x^2 - 8x + 4y - 4 = 0$ if y < 0 \Rightarrow The curve is parabola. *56. If all the words (with or without meaning) having five letters, formed using the letters of the word SMALL and arranged as in a dictionary; then the position of the word SMALL is: (2) 52nd (1) 59^{th} (3) 58th (4) 46th (3) Sol. Words starting with A, L, M = = 48 Words starting with SA, SI 3! = 9 \Rightarrow Rank of the word SMALL = 58 (n+1)(n+2)...3n57. lim is equal to: $\frac{9}{e^2}$ (1)(2) $\frac{18}{2^4}$ 3 log3 -(3)Sol. (1) $= \lim_{n \to \infty} \frac{1}{n} \cdot \log\left(1 + \frac{1}{n}\right) \left(1 + \frac{2}{n}\right) \dots \left(1 + \frac{2n}{n}\right)$ $\frac{1}{n} \cdot \sum_{r=1}^{2n} \ln\left(1 + \frac{r}{n}\right)$ $\ln y = \int_{0}^{2} \ln(1+x) dx$, let t = 1 + x



(1) 10 (3) 5 (2) 20

Sol.

(4) 6

(3) $\tan 60^\circ = \frac{h}{x} \implies h = \sqrt{3}x$ $\tan 30^\circ = \frac{h}{x+y} \implies \sqrt{3}h = x+y$ 3x = x+y $\implies 2x = y$ Time taken from A to B is 10 min So time taken from B to pillar is 5 min

P h 60° 30° A A

PART C – PHYSICS

*61. A uniform string of length 20 m is suspended from a rigid support. A short wave pulse is introduced at its lowest end. It starts moving up the string. The time taken to reach the support is : (take $g = 10 \text{ ms}^{-2}$) (1) 2s (2) $2\sqrt{2} \text{ s}$

(3) $\sqrt{2}$ s

11.....

(4) $2\pi\sqrt{2}$ s

Sol.

(2)

$$T(x) = \frac{Mgx}{L}$$

$$\Rightarrow v(x) = \sqrt{\frac{T}{\mu}} = \sqrt{gx}$$

$$\Rightarrow \frac{dx}{dt} = \sqrt{gx} \Rightarrow \text{ time taken} = 2\sqrt{2} \text{ s}.$$

*62. A person trying to lose weight by burning fat lifts a mass of 10 kg upto a height of 1 m 1000 times. Assume that the potential energy lost each time he lowers the mass is dissipated. How much fat will he use up considering the work done only when the weight is lifted up? Fat supplies 3.8×10^7 J of energy per kg which is converted to mechanical energy with a 20 % efficiency rate. Take g = 9.8 ms⁻² : (1) 6.45×10^{-3} kg (2) 9.89×10^{-3} kg

(1)
$$0.45 \times 10^{-3}$$
 kg (2) 9.39×10^{-3} kg (4) 2.45×10^{-3} kg

Sol. (3)

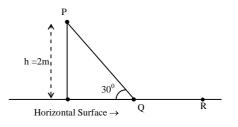
Let fat used be 'x' kg

 \Rightarrow Mechanical energy available = x × 3.8 × 10⁷ × -

Work done in lifting up = $10 \times 9.8 \times 1000$

$$\Rightarrow \mathbf{x} \times 3.8 \times 10^7 \times \frac{20}{100} = 9.8 \times 10^4$$
$$\Rightarrow \mathbf{x} \approx 12.89 \times 10^{-3} \text{ kg.}$$

*63. A point particle of mass m, moves along the uniformly rough track PQR as shown in the figure. The coefficient of friction, between the particle and the rough track equals μ. The particle is released, from rest, from the point P and it comes to rest at a point R. The energies, lost by the ball, over the parts, PQ and QR, of the track, are equal to each other, and no energy is lost when particle changes direction from PQ to QR.



The values of the coefficient of friction μ and the distance x(=QR), are, respectively close to : (1) 0.2 and 3.5 m (2) 0.29 and 3.5 m (3) 0.29 and 6.5 m (4) 0.2 and 6.5 m

Sol.

(2)

Since work done by friction on parts PQ and QR are equal

$$-\mu mg \times \frac{\sqrt{3}}{2} \times 4 = -\mu mgx$$

 $\Rightarrow x = 2\sqrt{3} \text{ m} \approx 3.5 \text{ m}$ Applying work energy theorem from P to R

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(QR = x)

mg sin
$$30^0 \times 4 - \mu$$
mg $\frac{\sqrt{3}}{2} \times 4 - \mu$ mg $x = 0$
 $\Rightarrow \mu = \frac{1}{2\sqrt{3}} \approx 0.29.$

64.

Two identical wires A and B, each of length ' ℓ ', carry the same current I. Wire A is bent into a circle of radius R and wire B is bent to form a square of side 'a'. If BA and BB are the values of magnetic field at the $\frac{B_A}{B_B}$ is : centres of the circle and square respectively, then the ratio

> $\frac{\pi^2}{16}$ (2)

(1)
$$\frac{\pi^2}{16\sqrt{2}}$$

(3)
$$\frac{\pi^2}{8\sqrt{2}}$$

Sol.

(3)

$$B_{A} = \frac{\mu_{0}}{4\pi} \frac{2\pi i}{(\ell/2\pi)}$$

$$B_{B} = \left[\frac{\mu_{0}}{4\pi} \frac{i}{\ell/8} (\sin 45^{0} + \sin 45^{0})\right] \times 4$$

$$\frac{B_{A}}{B_{B}} = \frac{\pi^{2}}{8\sqrt{2}}$$

A galvanometer having a coil resistance of 100 Ω gives a full scale deflection, when a current of 1 mA is 65. passed through it. The value of the resistance, which can convert this galvanometer into ammeter giving a full scale deflection for a current of 10 A is : $(1) 2\Omega$ $(2) 0.1 \Omega$

(4) 0.01 Ω

(3) 3 Ω

Sol.

(4) For full scale deflection $100 \times i_g = (i - i_g)S$ where 'S' is the required resistance $S = \frac{100 \times 1 \times 10^{-3}}{(10 - 10^{-3})}$

 $S\approx 0.01~\Omega$

- 66. An observer looks at a distant tree of height 10 m with a telescope of magnifying power of 20. To the observer the tree appears :
 - (1) 10 times nearer. (2) 20 times taller. (3) 20 times nearer. (4) 10 times taller.

Sol. (3)

- 67. The temperature dependence of resistances of Cu and undoped Si in the temperature range 300 - 400 K, is best described by :
 - (1) Linear increase for Cu, exponential increase for Si.
 - (2) Linear increase for Cu, exponential decrease for Si.
 - (3) Linear decrease for Cu, linear decrease for Si.
 - (4) Linear increase for Cu, linear increase for Si.

Sol. (2)

The electric resistance of a typical intrinsic (undoped) semiconductor decreases exponentially with temperature

 $\rho=\rho_0 e^{-aT}$ where a is a constant.

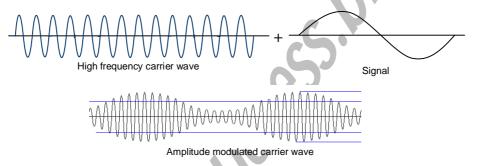
68. Choose the correct statement :

- (1) In amplitude modulation the frequency of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.
- (2) In frequency modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.
- (3) In frequency modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the frequency of the audio signal.
- (4) In amplitude modulation the amplitude of the high frequency carrier wave is made to vary in proportion to the amplitude of the audio signal.

Sol.

(4)

In amplitude modulation amplitude of carrier wave varies in proportion to applied signal.



69. Half-lives of two radioactive elements A and B are 20 minutes and 40 minutes, respectively. Initially, the samples have equal number of nuclei. After 80 minutes, the ratio of decayed numbers of A and B nuclei will be :

(2) 1 : 4

(4) 1 : 16

(1) 4:1

(3) 5:4

for A : N

(3)

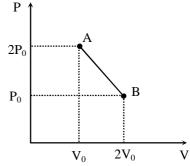
Sol.

for \mathbf{B} : \mathbf{N}_0 -

The required ratio is

15N

- 'n' moles of an ideal gas undergoes a process $A \rightarrow B$ as *70. shown in the figure. The maximum temperature of the gas during the process will be :
 - 2nR9P_\ nR $9P_0V_0$ 4nR



Sol. (4) Equation of line is $PV_0 + P_0V = 3P_0V_0$...(i) Also PV = nRT...(ii) for T_{max} , $\frac{dT}{dV} = 0$ \Rightarrow V = $\frac{3V_0}{2}$, P = $\frac{3P_0}{2}$ $\Rightarrow T_{max} = \frac{9P_0V_0}{4nR}$ An arc lamp requires a direct current of 10 A and 80 V to function. If it is connected to a 220 V (rms), 50 71. Hz AC supply, the series inductor needed for it to work is close to : (1) 0.08 H (2) 0.044 H (3) 0.065 H (4) 80 H Sol. (3) For the lamp with direct current, V = IR \Rightarrow R = 8 Ω and P = 80 × 10 = 800 W For ac supply $P = I_{rms}^2 R = \frac{\varepsilon_{rms}^2}{Z^2} R$ $\Rightarrow Z^2 = \frac{(220)^2 \times 8}{800}$ \Rightarrow Z = 22 Ω $\Rightarrow R^2 + \omega^2 L^2 = (22)^2$ $\Rightarrow \omega L = \sqrt{420}$ \Rightarrow L = 0.065 H *72. A pipe open at both ends has a fundamental frequency f in air. The pipe is dipped vertically in water so that half of it is in water. The fundamental frequency of the air column is now :

(1) $\frac{3f}{4}$		(2) 2f
(3) f	XO	(4) $\frac{f}{2}$

Sol.

For open pipe in air, fundamental frequency:

 2ℓ

$$f = \frac{V}{2\ell}$$

(3)

For the pipe closed at one end (dipped in water), fundamental frequency:

73. The box of pin hole camera, of length L, has a hole of radius *a*. It is assumed that when the hole is illuminated by a parallel beam of light of wavelength λ the spread of the spot (obtained on the opposite wall of the camera) is the sum of its geometrical spread and the spread due to diffraction. The spot would then have its minimum size (say b_{min}) when :

(1)
$$a = \sqrt{\lambda L}$$
 and $b_{\min} = \left(\frac{2\lambda^2}{L}\right)$
(3) $a = \frac{\lambda^2}{L}$ and $b_{\min} = \sqrt{4\lambda L}$

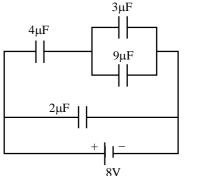
Sol.

(2) We know that Geometrical spread = a and diffraction spread = $\frac{\lambda L}{a}$ so spot size(b) = $a + \frac{\lambda L}{a}$ for minimum spot size $a = \frac{\lambda L}{a}$ $\Rightarrow a = \sqrt{\lambda L}$ and $b_{min} = \sqrt{\lambda L} + \sqrt{\lambda L} = \sqrt{4\lambda L}$ (2) $a = \sqrt{\lambda L}$ and $b_{\min} = \sqrt{4\lambda L}$

(4)
$$a = \frac{\lambda^2}{L}$$
 and $b_{\min} = \left(\frac{2\lambda^2}{L}\right)$

74. A combination of capacitors is set up as shown in the figure. The magnitude of the electric field, due to a point charge Q (having a charge equal to the sum of the charges on the 4 μ F and 9 μ F capacitors), at a point distant 30 m from it, would equal :

- (1) 360 N/C (2) 420 N/C
- (3) 480 N/C (4) 240 N/C



Sol.

(2)

Charge on 9 μ F capacitor = 18 μ C Charge on 4 μ F capacitor = 24 μ C \therefore Q = 24 + 18 = 42 μ C

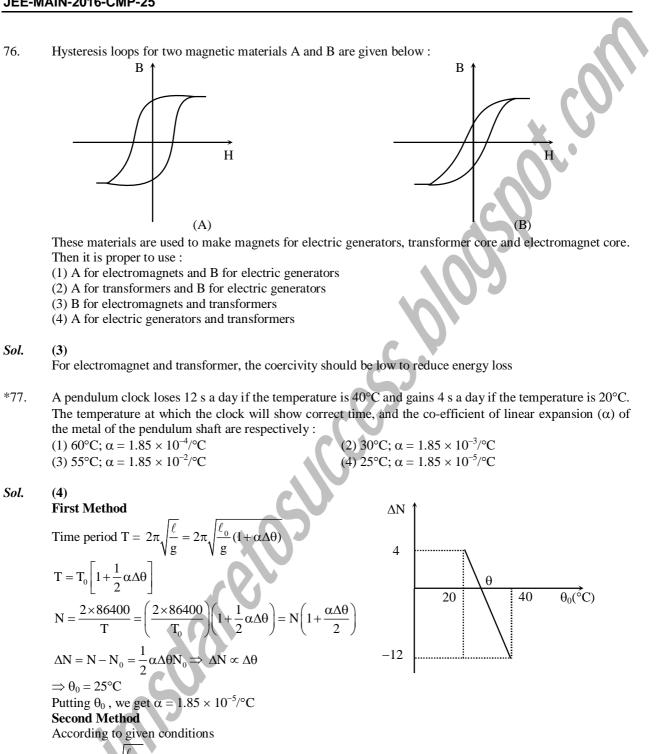
 $\therefore \quad \frac{KQ}{r^2} = \frac{9 \times 10^9 \times 42 \times 10^{-6}}{(30)^2} = 420 \text{ N/C}$

75. Arrange the following electromagnetic radiations per quantum in the order of increasing energy :
A : Blue light B : Yellow light
C : X-ray D : Radiowave
(1) A, B, D, C
(2) C, A, B, D
(3) B, A, D, C
(4) D, B, A, C

Sol.

(4)

Radiation energy per quantum is E = hvAs per EM spectrum, the increasing order of frequency and hence energy is Radio wave < Yellow light < Blue light < X Ray



$$86412 = 2\pi \sqrt{\frac{\ell_{40}}{g}} \qquad \dots(i)$$

$$86396 = 2\pi \sqrt{\frac{\ell_{20}}{g}} \qquad \dots(ii)$$

$$86400 = 2\pi \sqrt{\frac{\ell}{g}} \qquad \dots(iii)$$

From equation (i) and (iii)

$$12 = \frac{2\pi}{\sqrt{g}} \left[\sqrt{\ell_{40}} - \sqrt{\ell} \right] \qquad \dots (iv)$$

and $4 = \frac{2\pi}{\sqrt{g}} \left[\sqrt{\ell} - \sqrt{\ell_{20}} \right] \qquad \dots (v)$
on dividing (iv) and (v)
 $3 = \frac{\sqrt{1 + \alpha(40 - \theta)} - 1}{1 - \sqrt{1 + \alpha(20 - \theta)}}$
 $\Rightarrow 3 = \frac{40 - \theta}{\theta - 20}$ (by Binomial theorem)
 $\Rightarrow \theta = 25^{\circ}$
on using θ in (i) and (iii)
 $\frac{86412}{86400} = \sqrt{1 + \alpha 15} \Rightarrow \alpha = 1.85 \times 10^{-5/\circ}C$

78.

The region between two concentric spheres of radii 'a' and 'b', respectively (see figure), has volume charge density $\rho = \frac{A}{r}$, where A is a constant and r is the distance from the centre. At the centre of the spheres is a point charge Q. The value of A such that the electric field in the region between the spheres will be constant, is :

(1)
$$\frac{Q}{2\pi(b^2 - a^2)}$$

(3) $\frac{2Q}{\pi a^2}$
(2) $\frac{2Q}{\pi(a^2 - b^2)}$
(4) $\frac{Q}{2\pi a^2}$

Sol.

(4)

According Gauss's law, we can write

$$E \times 4\pi r^{2} = \frac{1}{\varepsilon_{0}} \left[Q + \int_{a}^{r} \left(\frac{A}{r} \right) (4\pi r^{2} dr) \right] = \frac{1}{\varepsilon_{0}} \left[Q + 2\pi A (r^{2} - a^{2}) \right]$$

For E to be independent of r

F

$$Q - 2\pi Aa^2 = 0 \implies a = \frac{Q}{2\pi a^2}$$

79. In an experiment for determination of refractive index of glass of a prism by $i - \delta$, plot, it was found that a ray incident at angle 35°, suffers a deviation of 40° and that it emerges at angle 79°. In that case which of the following is closest to the maximum possible value of the refractive index ? (2) 1.7

(4) 1.5

$$(1)$$
 1.6
 (3) 1.8

Sol.

(4)

$$\delta = i + e - A \Rightarrow A = 74^{\circ}$$

$$\mu = \frac{\sin\left(\frac{A + \delta_{\min}}{2}\right)}{\sin\left(\frac{A}{2}\right)} = \frac{5}{3}\sin\left(37^{\circ} + \frac{\delta_{\min}}{2}\right)$$

$$\mu_{\max} \text{ can be } \frac{5}{3}, \text{ so } \mu \text{ will be less than } \frac{5}{3}$$

Since δ_{\min} will be less than 40°, so $\mu < \frac{5}{3} \sin 57^{\circ} < \frac{5}{3} \sin 60^{\circ} \Rightarrow \mu < 1.446$ So the nearest possible value of μ should be 1.5

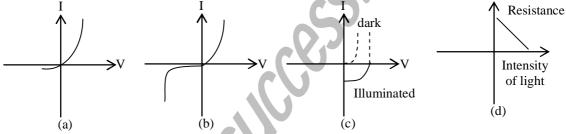
80. A student measures the time period of 100 oscillations of a simple pendulum four times. The data set is 90s, 91s, 95s and 92s. If the minimum division in the measuring clock is 1s, then the reported mean time should be:
(1) 02 + 5.0

(1) $92 \pm 5.0s$ (2) $92 \pm 1.8s$ (3) $92 \pm 3s$ (4) $92 \pm 2s$

Sol.

 $t = \frac{t_1 + t_2 + t_3 + t_4}{4} = \frac{90 + 91 + 95 + 92}{4} = 92$ Now mean deviation is equal to $\left(\frac{2 + 1 + 3 + 0}{4}\right) = 1.5$ Since least count of clock is one second, so $\Delta t = 2 \sec t$

81. Identify the semiconductor devices whose characteristics are given below, in the order (a), (b), (c), (d) :



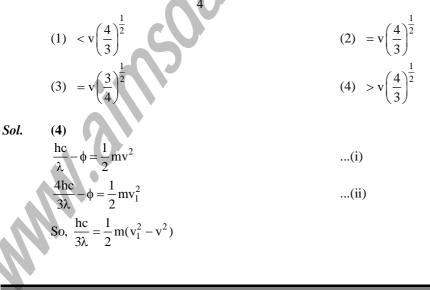
(1) Zener diode, Simple diode, Light dependent resistance, Solar cell

(2) Solar cell, Light dependent resistance, Zener diode, Simple diode

(3) Zener diode, Solar cell, Simple diode, Light dependent resistance

(4) Simple diode, Zener diode, Solar cell, Light dependent resistance

82. Radiation of wavelength λ , is incident on a photocell. The fastest emitted electron has speed v. If the wavelength is changed to $\frac{3\lambda}{4}$, the speed of the fastest emitted electron will be :



$$\frac{1}{3}\left(\frac{1}{2}mv^2 + \phi\right) = \frac{1}{2}m(v_1^2 - v^2)$$

$$\therefore \quad v_1 > v\left(\frac{4}{3}\right)^{\frac{1}{2}}$$

*83.

A particle performs simple harmonic motion with amplitude A. Its speed is trebled at the instant that it is at a distance $\frac{2A}{3}$ from equilibrium position. The new amplitude of the motion is :

 $A\sqrt{3}$

 $\frac{A}{3}\sqrt{41}$

(1)
$$3A$$
 (2)
(3) $\frac{7A}{3}$ (4)

Sol.

(3)

$$3\omega \sqrt{A^2 - \left(\frac{2A}{3}\right)^2} = \omega \sqrt{A_1^2 - \left(\frac{2A}{3}\right)^2}$$

$$\therefore \quad A_1 = \frac{7A}{3}$$

*84. A particle of mass m is moving along the side of a square of side 'a', with a uniform speed v in the x-y plane as shown in the figure : Which of the following statements is **false** for the angular momentum \vec{L} about the origin ?

(1) $\vec{L} = mv \left[\frac{R}{\sqrt{2}} - a \right] \hat{k}$ when the particle is moving from C to D.

(2)
$$\vec{L} = mv \left[\frac{R}{\sqrt{2}} + a \right] \hat{k}$$
 when the particle is moving from B to C.

(3) $\vec{L} = \frac{mv}{\sqrt{2}} R \hat{k}$ when the particle is moving from D to A.

(4)
$$\vec{L} = -\frac{mv}{\sqrt{2}} R \hat{k}$$
 when the particle is moving from A to B.

Sol. (1, 3)

$$\vec{L}_{O} = mv \frac{R}{\sqrt{2}} (-\hat{k}) \text{ [D to A]}$$

 $\vec{L}_{O} = mv \left[\frac{R}{\sqrt{2}} + a \right] \hat{k} \text{ [C to D]}$

 $\begin{array}{c} a & v & v \\ A & v & v & a \\ A & a & B \\ \hline A & A & A \\ \hline A & A & B \\ \hline A & A & A \\ \hline A & A &$

*85. An ideal gas undergoes a quasi static, reversible process in which its molar heat capacity C remains constant. If during this process the relation of pressure P and volume V is given by PV^n = constant, then n is given by (Here C_P and C_V are molar specific heat at constant pressure and constant volume, respectively):

(1)
$$n = \frac{C - C_p}{C - C_v}$$

(2) $n = \frac{C_p - C}{C - C_v}$
(3) $n = \frac{C - C_v}{C - C_p}$
(4) $n = \frac{C_p}{C_v}$

Sol. (1)

$$C = C_v - \frac{R}{n-1}$$
$$\frac{R}{n-1} = C_v - C_v$$
$$n = \frac{C - C_p}{C - C_v}$$

- 86. A screw gauge with a pitch of 0.5 mm and a circular scale with 50 divisions is used to measure the thickness of a thin sheet of Aluminium. Before starting the measurement, it is found that when the two jaws of the screw gauge are brought in contact, the 45th division coincides with the main scale line and that the zero of the main scale is barely visible. What is the thickness of the sheet if the main scale reading is 0.5 mm and the 25th division coincides with the main scale line?
 - (1) 0.80 mm

(2) 0.70 mm (4) 0.75 mm

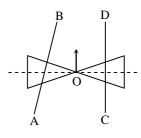
(4) turn left

(3) Sol. (1)

Reading = $0.5 + 25\left(\frac{0.5}{50}\right) + 5\left(\frac{0.5}{50}\right) = 0.8 \,\mathrm{mm}$

*87. A roller is made by joining together two cones at their vertices O. It is kept on two rails AB and CD which are placed asymmetrically (see figure), with its axis perpendicular to CD and its centre O at the centre of line joining AB and CD (see figure). It is given a light push so that it starts rolling with its centre O moving parallel to CD in the direction shown. As it moves, the roller will tend to :

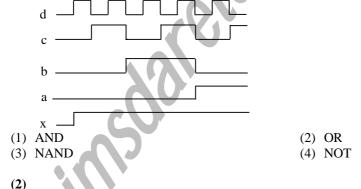
(1) turn right
(2) go straight



Sol. (4)

From normal reactions of roller, we can conclude it moves towards left.

88. If a, b, c, d are inputs to a gate and x is its output, then, as per the following time graph, the gate is :



Sol.

From truth Table, it is OR gate.

(3) turn left and right alternately

89. For a common emitter configuration, if α and β have their usual meanings, the incorrect relationship between α and β is :

(1) $\alpha = \frac{\beta}{1-\beta}$	(2)	$\alpha = \frac{\beta}{1+\beta}$
(1) $\alpha = \frac{\beta}{1-\beta}$ (3) $\alpha = \frac{\beta^2}{1+\beta^2}$	(4)	$\frac{1}{\alpha} = \frac{1}{\beta} + 1$

Sol. (1, 3)

 $\beta = \frac{\alpha}{1 - \alpha}$, is not satisfied by option (1, 3)

*90. A satellite is revolving in a circular orbit at a height 'h' from the earth's surface (radius of earth R; h<<R). The minimum increase in its orbital velocity required, so that the satellite could escape from the earth's gravitational field, is close to : (Neglect the effect of atmosphere.)

(1) \sqrt{gR} (3) $\sqrt{gR}(\sqrt{2}-1)$ (2) $\sqrt{gR/2}$ (4) $\sqrt{2gR}$

Sol.

(3)

At height h escape velocity

$$V_{e} = \sqrt{\frac{2GM}{h+h}}$$

Orbital velocity $V_0 = \sqrt{\frac{GM}{R+h}}$

: Increase in orbital velocity required to escape gravitational field

$$\Rightarrow V_{e} - V_{0}$$
$$\Rightarrow \sqrt{gR} \left(\sqrt{2} - 1\right)$$

Read the following instructions carefully:

- 1. The candidates should fill in the required particulars on the Test Booklet and Answer Sheet (*Side–I*) with *Blue/Black Ball Point Pen*.
- 2. For writing/marking particulars on *Side-2* of the Answer Sheet, use *Blue/Black Ball Point Pen only*.
- 3. The candidates should not write their Roll Numbers anywhere else (except in the specified space) on the Test Booklet/Answer Sheet.
- 4. Out of the four options given for each question, only one option is the correct answer.
- 5. For each *incorrect response, one-fourth* (¹/₄) of the total marks allotted to the **question** would be deducted from the total score. *No deduction* from the total score, however, will be made *if no response* is indicated for an item in the Answer Sheet.
- 6. Handle the Test Booklet and Answer Sheet with care, as under no circumstances (except for discrepancy in *Test Booklet Code and Answer Sheet Code*), another set will be provided.
- 7. The candidates are not allowed to do any rough work or writing work on the Answer sheet. All calculations/writing work are to be done in the space provided for this purpose in the Test Booklet itself, marked 'Space for Rough Work'. This space is given at the bottom of each page and in **three** pages (Pages 21 23) at the end of the booklet.
- 8. On completion of the test, the candidates must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall. **However, the candidates are allowed to take away this Test Booklet with them.**
- 9. Each candidate must show on demand his/her Admit Card to the Invigilator.
- 10. No candidate, without special permission of the Superintendent or Invigilator, should leave his/her seat.
- 11. The candidates should not leave the Examination Hall without handing over their Answer Sheet to the Invigilator on duty and sign the Attendance Sheet again. Cases where a candidate has not signed the Attendance Sheet a second time will be deemed not to have handed over the Answer Sheet and dealt with as an unfair means case. The candidates are also required to put their left hand THUMB impression in the space provided in the Attendance Sheet.
- 12. Use of Electronic/Manual Calculator and any Electronic device like mobile phone, pager etc. is prohibited.
- 13. The candidates are governed by all Rules and Regulations of the JAB/Board with regard to their conduct in the Examination Hall. All cases of unfair means will be dealt with as per Rules and Regulations of the JAB/Board.
- 14. No part of the Test Booklet and Answer Sheet shall be detached under any circumstance.
- 15. Candidates are not allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, electronic device or any other material except the Admit Card inside the examination room/hall.