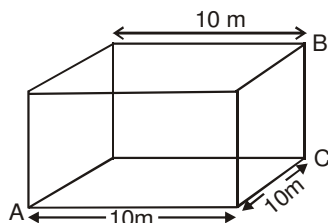


KINEMATICS

EXERCISE – I

SINGLE CORRECT

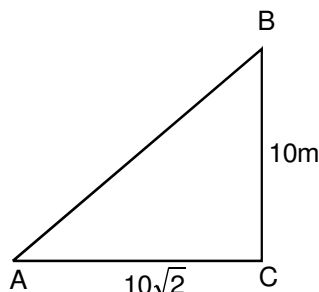
1. B



Fly start from A and reaches at B.

$$\therefore (AB)^2 = (AC)^2 + (BC)^2$$

$$AC = \sqrt{10^2 + 10^2} = 10\sqrt{2}$$

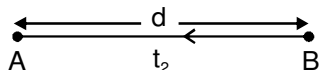
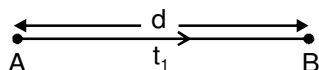


$$\therefore AB = \sqrt{(10\sqrt{2})^2 + 10^2} = 10\sqrt{3} \text{ m}$$

2. B

$$\text{From A to B } t_1 = \frac{d}{20} \text{ hr}$$

$$\text{From B to A } t_2 = \frac{d}{30} \text{ hr}$$



$$\therefore \text{Average Speed} = \frac{\text{Total Distance}}{\text{Total Time}}$$

$$= \frac{2d}{t_1 + t_2} = \frac{2d}{\frac{d}{20} + \frac{d}{30}}$$

$$v = 24 \text{ km/hr}$$

3. A

$$\frac{d/3, t_1}{V_1=2\text{m/s}} \quad \frac{d/3, t_2}{V_2=3\text{m/s}} \quad \frac{d/3, t_3}{V_3=6\text{m/s}}$$

$$\xleftarrow{\hspace{1.5cm}} d \xrightarrow{\hspace{1.5cm}}$$

$$\text{Now } t_1 = \frac{d/3}{v_1} = \frac{d}{6}$$

$$t_2 = \frac{d/3}{3} = \frac{d}{9}$$

$$t_3 = \frac{d/3}{6} = \frac{d}{18}$$

$$\text{Average Velocity} = \frac{d}{\frac{d}{6} + \frac{d}{9} + \frac{d}{18}} = \frac{18}{6} = 3 \text{ m/s}$$

4. B

$$t = 62.8 \text{ sec}$$

in each lap car travel a distance = $2\pi R$

$$= 2 \times 3.14 \times 100 = 628 \text{ m}$$

In each lap displacement of the car = 0

Average speed

$$= \frac{\text{Total Distance}}{\text{Total Time}} = \frac{628}{62.8} = 10 \text{ m/s}$$

$$\text{Average Velocity} = \frac{\text{Total Displacement}}{\text{Total Time}} = 0$$

5. A

$$2s = gt^2$$

$$s = \frac{1}{2}gt^2$$

$$v = \frac{ds}{dt} = gt$$

6. D

7. C

let the accelration of the body is a and $u = 0$

$$\text{then } x_1 = \frac{1}{2}at^2 = \frac{1}{2}a(10)^2$$

$$x_2 = \frac{1}{2}a(20)^2 - x_1$$

$$= \frac{1}{2}a(20)^2 - \frac{1}{2}a(10)^2$$

$$= \frac{1}{2}a(10)(30)$$

$$x_3 = \frac{1}{2}a(30)^2 - \frac{1}{2}a(20)^2$$

$$= \frac{1}{2}a(10)(50)$$

$$\therefore x_1 : x_2 : x_3 = 1 : 3 : 5$$

8. **B**

Stone is dropped

so time taken by stone to reach the bottom of the wall t_1

$$\therefore h = \frac{1}{2}gt_1^2$$

$$= t_1 = \sqrt{\frac{2h}{g}} \quad \text{--- (i)}$$

time taken by sound to comes from bottom to upper

$$\text{end } t_2 = \frac{h}{v} \quad \text{--- (ii)}$$

$$\therefore \text{Total time} = t_1 + t_2 = \sqrt{\frac{2h}{g}} + \frac{h}{v}$$

9. **B**

$$x = 5 \sin 10t$$

$$v_x = \frac{dx}{dt} = 50 \cos 10t$$

$$\text{Similarly } y = 5 \cos 10t$$

$$v_y = \frac{dy}{dt} = -50 \sin 10t$$

$$V_{\text{net}}^2 = V_x^2 + V_y^2$$

$$v_{\text{net}} = \sqrt{(50)^2(\sin^2 10t + \cos^2 10t)} = 50 \text{ m/sec}$$

10. **D**

$$v = \ell n x \text{ m/s} \quad (\text{Given})$$

$$a = v \frac{dv}{dx}$$

$$\Rightarrow a = \ell n x \times \frac{d}{dx}(\ell n x)$$

$$a = \frac{\ell n x}{x}$$

$$F_{\text{net}} = 0$$

$$\Rightarrow a = 0$$

$$\frac{\ell n x}{x} = 0$$

$$x = 1 \text{ m}$$

11. **C**

$$\vec{F} = 2 \sin 3\pi t \hat{i} + 3 \cos 3\pi t \hat{j}$$

$$a = \frac{dv}{dt} = 2 \sin 3\pi t \hat{i} + 3 \cos 3\pi t \hat{j}$$

$$\int_0^v dv = 2 \int_0^t \sin 3\pi t \, dt \hat{i} + 3 \int_0^t \cos 3\pi t \, dt \hat{j}$$

$$v = -\frac{2}{3\pi} [\cos 3\pi t]_0^t \hat{i} + \frac{3}{3\pi} [\sin 3\pi t]_0^t \hat{j}$$

$$\int_0^r dx = \int_0^t \left[-\frac{2}{3\pi} [\cos 3\pi t - 1] \hat{i} + \frac{1}{\pi} \sin 3\pi t \hat{j} \right] \cdot dt$$

$$\vec{r} = -\frac{2}{3\pi} \left[\int_0^t \cos 3\pi t \, dt - \int_0^t dt \right] \hat{i} + \frac{1}{\pi} \int_0^t \sin 3\pi t \, dt \hat{j}$$

$$= -\frac{2}{(3\pi)^2} [\sin 3\pi t]_0^t \hat{i} + \frac{2}{3\pi} t \hat{i} - \frac{1}{3\pi^2} [\cos 3\pi t]_0^t \hat{j}$$

For $t = 1 \text{ sec}$

$$\vec{r} = \frac{2}{3\pi} \hat{i} + \frac{2}{3\pi^2} \hat{j}$$

12. **B**

$$F = Be^{-ct}$$

$$a = \frac{B}{m} e^{-ct}$$

$$\Rightarrow \int_0^v dv = \int_0^t \frac{B}{m} e^{-ct} dt$$

$$v = -\frac{B}{mc} [a^{-ct} - 1]_0^t$$

$$\text{At } t = \infty \quad v = \frac{B}{mc}$$

13. **B**

$$v = t^2 - t$$

$$\therefore a = \frac{dv}{dt} = 2t - 1$$

Motion is consider as Retards
when V & a are in opposite Direction**Case - 1**

If $v > 0$ then $a < 0$
 But $t^2 - t > 0$, $t > 1$
 and $a > 0$ for $t > 1$
 so not Possible

Case - 2

$v < 0$, $a > 0$
 $t^2 - t < 0$, $2t - 1 > 0$

$$t \in (0, 1), t > \frac{1}{2}$$

$$\frac{1}{2} < t < 1$$

14. A
 distance Travelled by

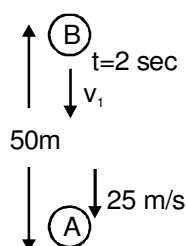
$$\text{ball in 2 sec} = 5 \times 2 + \frac{1}{2} \times 10 \times 2^2$$

$$= 30 \text{ m}$$

$$\text{and } v \text{ at time 2 sec} = 5 + 10 \times 2 = 25 \text{ m/s}$$

Relative Method
 w.r.t. A ball

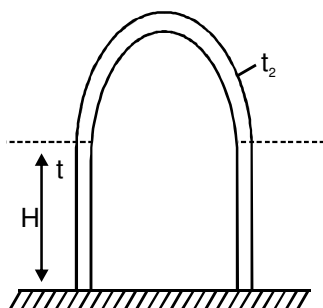
$$t = \frac{30}{v_1 - 25} = 2 \text{ sec}$$



$$30 = 2v_1 - 50$$

$$v_1 = 40 \text{ m/s}$$

15. D



16. C

$$\therefore H_{\max} = \frac{u^2}{2g} \Rightarrow u = \sqrt{2hg}$$

$$\text{Given } H_{\max} = 5 \text{ m}$$

$$t = \frac{u}{g} = \sqrt{\frac{2gh}{g}} = \sqrt{\frac{2H}{g}}$$

$$= \sqrt{\frac{2 \times 5}{10}} = 1 \text{ sec}$$

$$\therefore \text{ in 1 min} = 60 \text{ Balls.}$$

17. B
 Length of groove is L

$$t_1 = \sqrt{\frac{L}{g_{\text{eff}}}} = \sqrt{\frac{L}{g}}$$

$$t_2 = \sqrt{\frac{L}{g \sin 30^\circ}}$$

$$\Rightarrow t_1 : t_2 = 1 : \sqrt{2}$$

18. C

$$V_{\text{inst}} = \frac{dx}{dt} \text{ (slop of } x-t \text{ graph)}$$

At C $\tan \theta = +ve$ At E $\theta > 90^\circ$ ($-ve$ slop)

At D $\theta = 0^\circ$ At F $\theta < 90^\circ$ ($+ve$ slope)

$\therefore$ At E v_{inst} is negative

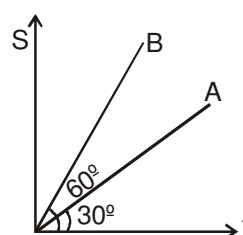
19. C
 From graph it is clear that velocity is always positive during its motion
 so displacement = distance
 displacement = Area under V-t curve

$$= \frac{1}{2} \times 20 \times 1 + 20 \times 1 + \frac{1}{2} \times 1 \times 10$$

$$+ 1 \times 10 + 1 \times 10$$

$$= 55 \text{ m}$$

20. D

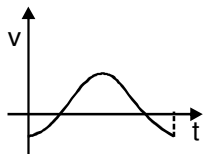


$$\frac{V_A}{V_B} = \frac{\tan 30^\circ}{\tan 60^\circ}$$

$$\therefore \frac{V_A}{V_B} = \frac{1/\sqrt{3}}{\sqrt{3}} = \frac{1}{3}$$

21. C
Equation of given sin curve is
 $x = -A \sin t$

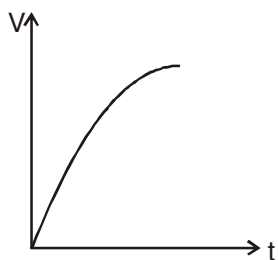
$$V = \frac{dx}{dt} = -A \cos t$$



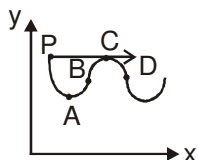
22. D
From graph
 $a = -AV + B$
 $\int \frac{dv}{B - AV} = \int dt$
 $\Rightarrow \frac{-1}{A} \int \frac{dk}{k} = \int dt$ let $(B - AV) = K$
 $-\ln(B - AV) = At + c$
 $c = -\ln B$ (When $t = 0, V = 0$)
 $\therefore -\ln(B - AV) = At - \ln B$
 $t = \frac{1}{A} \ln \left(\frac{B}{B - AV} \right)$

$$e^{At} = \frac{B}{B - AV} \Rightarrow B - AV = Be^{-At}$$

$$\Rightarrow V = \frac{B}{A} (1 - e^{-At})$$



23. B
Point C



24. B
Area = $0.4 \times 0.2 + 0.4 \times 0.2 + 0.4 \times 0.2$
 $+ \frac{1}{2} \times 0.4 \times 0.2 + 0.6 \times 0.2$

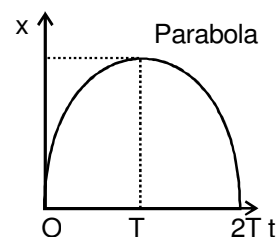
$$\text{Area} = 0.4 \quad \left[\int a \cdot dx = \int v dv \right]$$

$$\text{Now, } v_f^2 - v_i^2 = 2(\text{Area})$$

$$v_f^2 = 0.8 + (0.8)^2$$

$$V_f = 1.2 \text{ m/s}$$

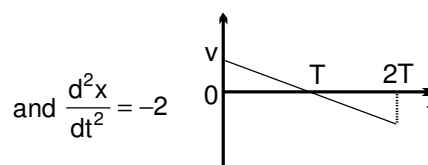
25. B



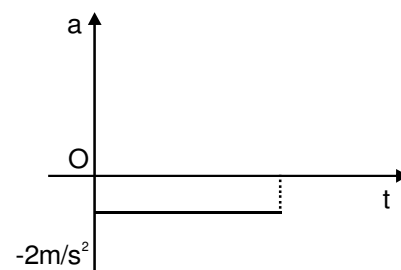
$$x = -t(t - 2T)$$

$$x = -t^2 + 2Tt$$

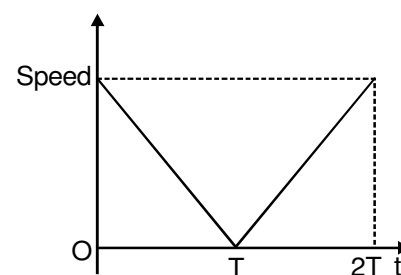
$$\frac{dx}{dt} = -2t + 2T$$



26. C



27. D



28. B
Particle comes to rest when $v=0$
on observing graphs $\rightarrow V=0$ at $t=0, 4.66$ sec, 8 sec
Incorrect $t=5$ sec

29. C
Rate of change of velocity is maximum
 $t = 4$ to 6 sec

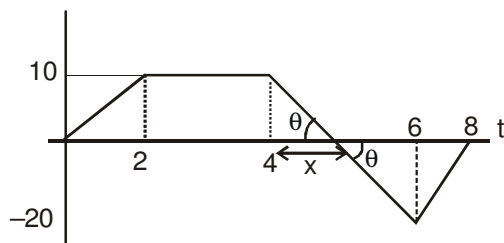
$$a = \frac{-20 - 10}{6 - 4} = \frac{-30}{2} = -15 \text{ m/sec}^2$$

30. A
 $a = 5 \text{ m/s}^2$ (in time 0 to 2 sec)

$$x_f + 15 = \frac{1}{2} \times 5 \times (2)^2$$

$$\therefore x_f + 15 = 10 \Rightarrow x_f = -5 \text{ m}$$

31. A



$$\tan \theta = \frac{10}{x}$$

$$\text{and } \tan \theta = \frac{20}{(2-x)}$$

$$\therefore \frac{10}{x} = \frac{20}{2-x} \Rightarrow x = \frac{2}{3} \text{ sec}$$

Maximum Displacement

$$= \frac{1}{2} \times 2 \times 10 + 2 \times 10 + \frac{1}{2} \times \frac{2}{3} \times 10$$

$$= 33.3 \text{ m}$$

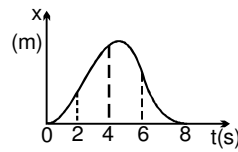
32. A
Total Distance = Upper walla area + Nichewala

$$= 33.3 + \frac{1}{2} \times \left(2 - \frac{2}{3}\right) \times 20 + \frac{1}{2} \times 2 \times 20$$

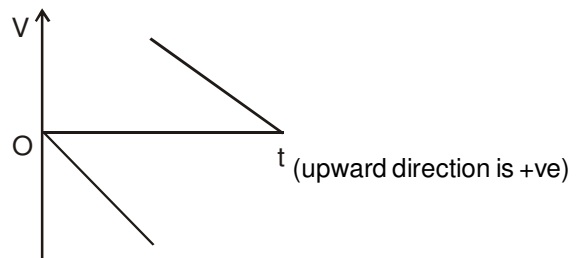
$$= 33.3 + 33.3$$

$$= 66.6 \text{ m}$$

33. C
 $v-t$ Displacement is zero



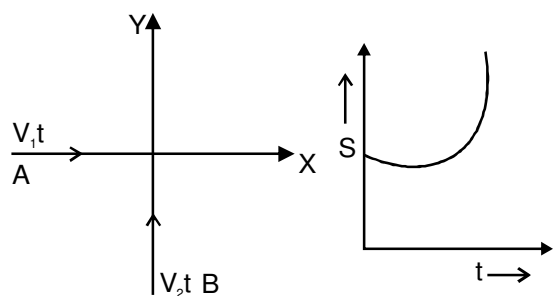
34. A



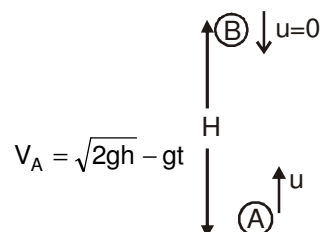
35. D
The slope of curve c_1 and c_2 is constant.
so, their Relative velocity is Non-zero constant not a variable quantity

36. D
 $\therefore$ Slope of $v-t$ curve gives acceleration
Here slope of $P_1 >$ slope of P_2 ($a_{p_1} > a_{p_2}$)
 $\therefore$ Relative velocity in their motion continuously increases.

37. D



38. C



$$V_B = -gt$$

$$V_{AB} = V_A - V_B = -gt + \sqrt{2gH} + gt$$

$$= \sqrt{2gh} \left(\text{upto time } \frac{T}{2} \right)$$

where T = Time period

$$\text{After } \frac{T}{2} \quad V_B = 0$$

$$\therefore V_{AB} = V_A - V_B \\ = -gt$$

39. C

$$V_{AB} = 10 - 5 = 5 \text{ m/s}$$

$$\begin{array}{c} 10\text{m/s} \quad 5\text{m/s} \\ \xrightarrow{\quad} \quad \xrightarrow{\quad} \\ \textcircled{A} \quad \quad \textcircled{B} \end{array} \quad t = \frac{100}{5} = 20 \text{ sec}$$

40. B

$$V_E = \frac{H}{60} \text{ m/s and } V_M = \frac{H}{180} \text{ m/s}$$

$$t = \frac{H}{V_E + V_M} = \frac{H}{\frac{H}{60} + \frac{H}{180}} = \frac{180}{4}$$

$$\therefore t = 45 \text{ sec}$$

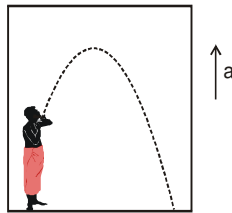
41. B

a = acceleration of lift
u = velocity relative to lift
According to problem
-u = u - (g + a) \times t

$$t = \frac{2u}{g+a}$$

$$\Rightarrow at + gt = 2u$$

$$\therefore \frac{2u - gt}{t}$$



42. D

Horizontal Component of velocity
Because $\rightarrow$ there is no acceleration in horizontal Direction

43. D

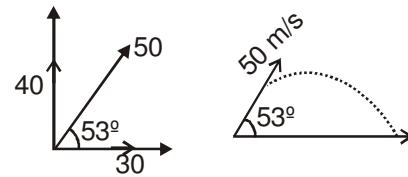
44. B

At maximum height $V_y = 0$

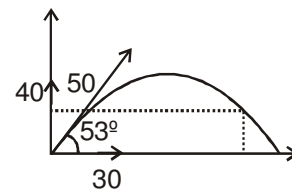
$$\therefore V_x = u_x = \frac{u}{2} = u \cos \theta$$

$$\text{so range} = \frac{u^2 \sin 2\theta}{g} = \frac{\sqrt{3}}{2} \frac{u^2}{g}$$

45. A



46. D



$$H = 40t - \frac{1}{2} \times 10 \times t^2$$

$$5t^2 - 40t + H = 0$$

$$\text{Now, } t_1 + t_2 = \frac{40}{5} = 8 \text{ sec}$$

47. A

By Equation of trajectory

$$y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$

$$\theta = 53^\circ$$

$$\Rightarrow y = \frac{4x}{3} - \frac{10x^2}{1800}$$

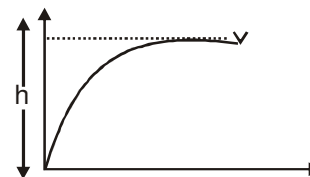
$$\Rightarrow 180y = 240x - x^2$$

48. B

$$\vec{V} = a\hat{i} + (b - ct)\hat{j} = u_x\hat{i} + (u_y - gt)\hat{j}$$

$$R = \frac{2u_x u_y}{g} = \frac{2ab}{c}$$

49. C



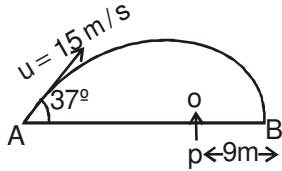
$$h = \frac{U_y^2}{2g}$$

$$U_y = \sqrt{2gh}$$

$$R = U_x T = \frac{U \cdot 2\sqrt{2gh}}{g}$$

$$R = 2U \sqrt{\frac{2h}{g}}$$

50. B

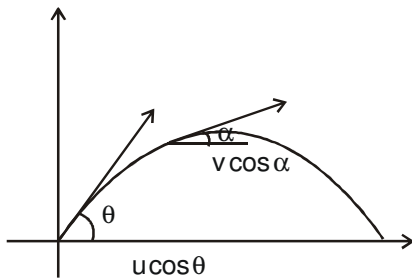


$$T = \frac{2u \sin 37^\circ}{g}$$

$$= \frac{2 \times 15 \times 3}{10 \times 5} = 1.8 \text{ Sec}$$

$$\text{Minimum Velocity} = \frac{9}{1.8} = 5 \text{ m/s}$$

51. C

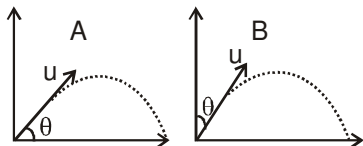


Horizontal Component

$$u \cos \theta = v \cos \alpha$$

$$\therefore v = u \cos \theta \sec \alpha$$

52. D



Both may have same time of flight

$$\therefore T = \frac{2u \sin \theta}{g}$$

53. B

$$\therefore H_{\max} = \frac{u_y^2}{2g}$$

$$\Rightarrow u_y = \sqrt{2gH}$$

$$\therefore T = \frac{2u_y}{g} = \frac{2\sqrt{2gH}}{g} = 2\sqrt{2} \sqrt{\frac{H}{g}}$$

54. B

$$s_y = u_y t - \frac{1}{2} a_y t^2 \quad u_x = 50 \cos 53^\circ = 30 \text{ m/s}$$

$$75 = 40t - \frac{1}{2} \times 10 \times t^2 \quad u_y = 50 \sin 53^\circ = 40 \text{ m/s}$$

$$\Rightarrow t^2 - 8t + 15 = 0$$

$$\Rightarrow t^2 - 5t - 3t + 15 = 0, t_1 = 3 \text{ sec}, t_2 = 5 \text{ sec}$$

$$x_2 = 30 \times 5 = 150 \text{ m}$$

$$x_1 = 30 \times 3 = 90 \text{ m}$$

$$\therefore x_2 - x_1 = 150 - 90 = 60 \text{ m}$$

55. A

$$\text{In } t = 2 \text{ sec}$$

$$x = 30 \times 2 = 60 \text{ m}$$

$$y = 40 \times 2 - \frac{1}{2} \times 10 \times (2)^2$$

$$= 80 - 20 = 60 \text{ m}$$

$$\text{Distance} = 60\sqrt{2} \text{ m}$$

56. C

$$H = 20 \text{ m}, u = 0$$

$$-Sy = ut - \frac{1}{2} gt^2$$

$$T = \sqrt{\frac{2 \times 20}{10}} = 2 \text{ sec}$$

$$\text{Range} = ut + \frac{1}{2} gt^2$$

$$= 0 + \frac{1}{2} \times 10 \times (2)^2 = 20 \text{ m}$$

57. C

$$v_y^2 - (4)^2 = -2 \times 10 \times 0.45$$

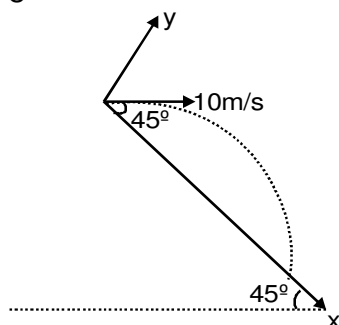
$$v_y^2 = 7 \text{ m}^2/\text{s}^2$$

$$v_x = 5 \cos 53^\circ = 3 \text{ m/s}$$

$$\therefore V_{\text{net}} = \sqrt{(v_x)^2 + (v_y)^2} = \sqrt{9 + 7}$$

$$= 4 \text{ m/s}$$

58. C



$$a_y = -\frac{g}{\sqrt{2}} \text{ m/s}^2$$

$$a_x = \frac{g}{\sqrt{2}} \text{ m/s}^2$$

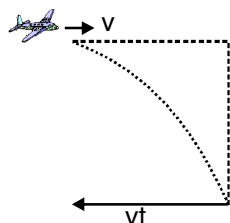
$$T = \frac{2u \sin \theta}{g_{\text{eff}}}$$

$$T = \frac{2 \times (10/\sqrt{2})}{g/\sqrt{2}} = 2 \text{ sec}$$

59. C

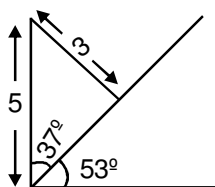
Time is depend only in vertical component V_y
but in both cases $V_y = 0$
 $\therefore$ Both will reach the ground at the same time

60. A



Horizontal velocity of bomb with respect to plane is zero.

61. A

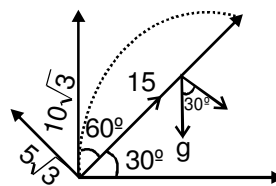


As particle has thrown $\perp$ from ground.

$$\therefore H_{\text{max}} = \frac{u^2}{2g} = 5\text{m}$$

$$\therefore \text{from inclined plane } H_{\text{max}} = 3\text{m}$$

62. C

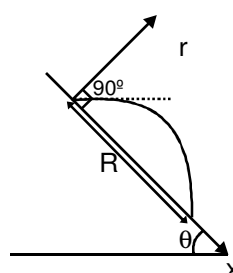


$$T = \frac{2u_y}{g \cos \theta}$$

$$T = \frac{2 \times 5\sqrt{3}}{10 \times \cos 30^\circ}$$

$$T = 2 \text{ sec}$$

63. C



$$a_y = -g \cos \theta$$

$$a_x = g \sin \theta$$

$$u_y = v$$

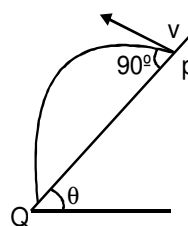
$$u_x = 0$$

$$\text{Range} = \frac{1}{2} a_x T^2$$

$$T = \frac{2.v}{g \cos \theta}$$

$$= \frac{1}{2} g \sin \theta$$

64. D



$$R = u_x t + \frac{1}{2} a_x t^2$$

$$[\therefore u_x = 0, u_y = v]$$

$$\therefore T = \frac{2u_y}{g \cos \theta} = \frac{2v}{g \cos \theta}$$

$$R = \frac{1}{2} \times g \sin \theta \times \frac{4v^2}{g^2 \cos^2 \theta}$$

$$= \frac{2v^2}{g} \tan \theta \sec \theta = Tv \tan \theta$$

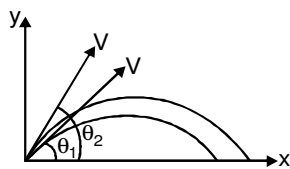
65. B
 $a_{AB} = 0$
 $\therefore$ Straight line

66. C
 Given $V_1 \cos \theta_1 = v_2 \cos \theta_2 \Rightarrow v_{xA} = v_{xB}$
 $\vec{v}_A = v_{xA} \hat{i} + v_{yA} \hat{j}$; $\vec{v}_B = v_{xB} \hat{i} + v_{yB} \hat{j}$
 $\therefore \vec{v}_{AB} = v_{yA} \hat{j} - v_{yB} \hat{j}$ (Verticle Line)
 $R = \frac{2u_x u_y}{g}$

67. D
 $T = \frac{2u_y}{g} \quad \therefore \text{same}$

$$H = \frac{u_y^2}{2g}$$

$$\vec{v}_{AB} = v_{xA} \hat{i} - v_{xB} \hat{i}$$

68. B
- 
- $$R = \frac{2u_x u_y}{g} = \frac{u^2 \sin 2\theta}{g}$$

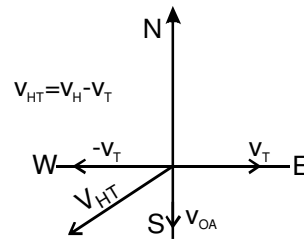
when angle in θ and $90 - \theta$ Range is Same

$$v_{21} = v_{2x} \hat{i} - v_{2y} \hat{j} - v_{1x} \hat{i} - v_{1y} \hat{j}$$

$$\tan \theta = \left(\frac{v_{2y} - v_{1y}}{v_{2x} - v_{1x}} \right) \begin{matrix} v_{2y} < v_{1y} \\ v_{2x} > v_{1x} \end{matrix}$$

$$\tan \theta = -ve$$

69. D



South - West

70. D

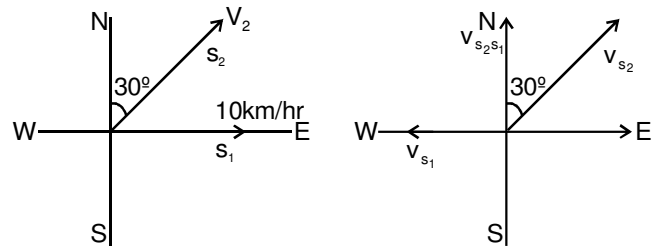
$$\vec{v}_r = \vec{v}_1 - \vec{v}_2$$

$$|\vec{v}_r| = \sqrt{v_1^2 + v_2^2 - 2v_1 v_2 \cos \theta}$$

$$|\vec{v}_r| \text{ max when } \cos \theta = -1 \quad \theta = \pi$$

$$\Rightarrow v_r = v_1 + v_2$$

71. C

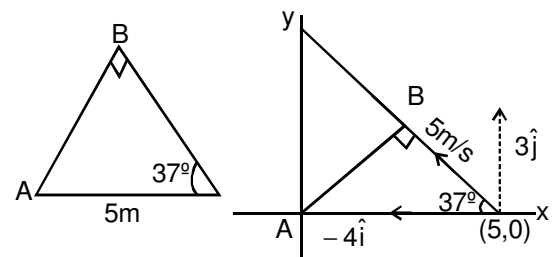


East component of both ship must be same.

from fig : $-v_2 \sin 30^\circ = v_{s1}$

$$v_{s2} = \frac{10}{1/2} = 20 \text{ km/hr}$$

72. A



Draw a perpendicular from A on the line of a velocity of the particle B.

$$\sin 37^\circ = \frac{AB}{5}$$

$$AB = 3m$$

73. A
Each particle move perpendicular with the neighbour particle so no component of v along the line of motion of neighbour velocity so vel. of approach = v

$$\Rightarrow t = \frac{a}{v}$$

74. A
Given $v_r + v_{br} = v_b$

$$\Rightarrow v_r + v_{br} = 16 \quad -(1)$$

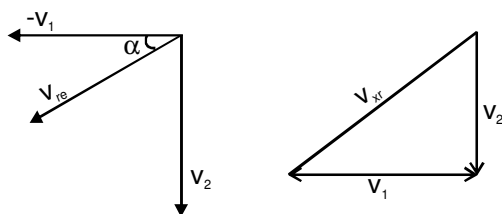
$$v_{br} - v_r = 8 \quad -(2)$$

from equation (1) and (2)

$$v_{br} = 12 \text{ km/h}$$

$$v_r = 4 \text{ km/h}$$

75. A
Drops of rain move parallel to the walls if v_{rp} makes α angle with the horizontal.



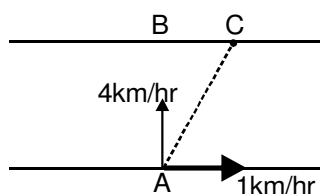
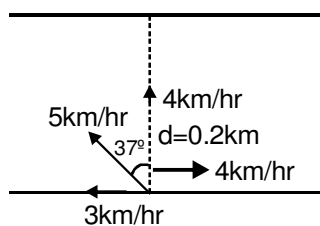
$$\vec{V}_{RC} = \vec{V}_R - \vec{V}_C$$

$$= \vec{V}_R \hat{j} - \vec{V}_C \hat{i}$$

$$\tan \alpha = \frac{v_2}{v_1} = \frac{6}{2}$$

$$\alpha = \tan^{-1}(3)$$

76. B



$$\text{Given : } V_{br} = 5 \text{ km/hr}$$

$$v_r = 4 \text{ km/hr} \quad d = 0.2 \text{ km}$$

$$t = \frac{0.2}{4}$$

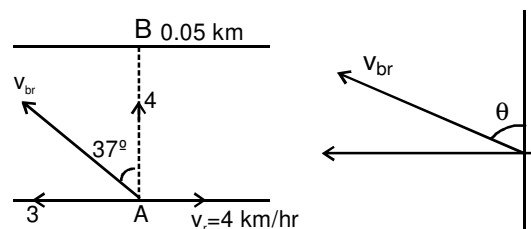
$$= 0.05 \text{ hr} = 3 \text{ min}$$

$$t_2 = \frac{0.05}{3} \times 60$$

$$= 1 \text{ min}$$

$$t_1 + t_2 = 4 \text{ min}$$

77. B



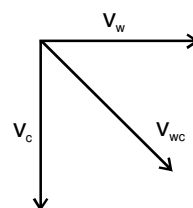
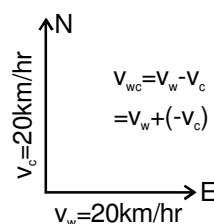
$$V_{br} = 5 \text{ km/hr}$$

$$\sin \theta = \frac{v_r}{5}$$

$$t = \frac{d}{v_{br} \cos \theta} \Rightarrow \cos \theta = \frac{4}{5} \Rightarrow \theta = 37^\circ$$

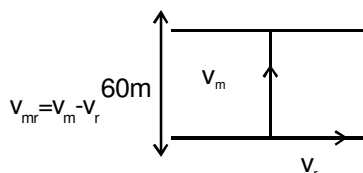
$$\sin 37^\circ = \frac{v_r}{5} \Rightarrow v_r = 3 \text{ km/hr}$$

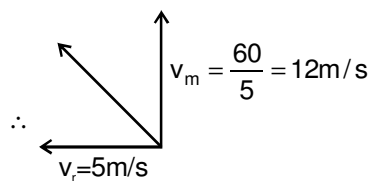
78. C



79. B

$$v_r = 5 \text{ m/s}$$





$$v_{mr} = \sqrt{(12)^2 + (5)^2} = 13 \text{ m/s}$$

80. B

81. A
 $-5 - 5 - 5 + v_B = 0$
 $v_B = 15 \text{ m/s} \downarrow$

82. A
 $+2 - v_B - v_B + 1 = 0$

$$v_B = \frac{3}{2} \text{ m/s} \uparrow$$

83. A
 $-a - a_B - a_B + f = 0$

$$a_B = \left(\frac{f}{2} - \frac{a}{2} \right) = \frac{1}{2}(f - a) \uparrow$$

84. A
 $-a_c + 2 + 2 - 1 - 1 - a_c = 0$
 $a_c = 1 \text{ m/s}^2 \uparrow$

EXERCISE – II

MULTIPLE CHOICE QUESTIONS

1. A, B, C, D

$$X = \alpha t^2 - \beta t^3$$

$$(A) \quad 0 = \alpha t^2 - \beta t^3$$

$$\Rightarrow t = \frac{\alpha}{\beta}$$

$$(B) \quad v = \frac{dx}{dt} = 2\alpha t - 3\beta t^2$$

$$v = 0 \Rightarrow t = \frac{2\alpha}{3\beta}$$

$$(C) \quad a = \frac{d^2x}{dt^2} = 2\alpha - 6\beta t$$

when $t=0$

$$a = 2\alpha ; v = 0$$

$$(D) \quad \text{Acceleration at } t = \frac{\alpha}{3\beta} ; a = 0$$

$$\therefore \text{net force} = 0$$

2. A, C

$$v = 10 - 5t \quad \text{---} \quad t=2$$

When $v = 0$ at $t = 2$ sec.

$$\text{Max displacement} = 10t - \frac{5t^2}{2}$$

$$\text{put } t=2 \Rightarrow 20 - 10 = 10\text{m}$$

Distance traveled in first 3 seconds

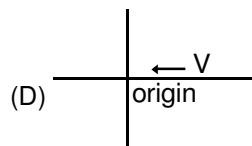
$$= 10 + \left(0 + \frac{1}{2} \times 5 \times (1)^2\right)$$

$$= 12.5 \text{ m}$$

3. B, C, D

$$a = \frac{dv}{dt}$$

$$(C) \quad \frac{\vec{v}}{a} \quad \text{Object is slowing down.}$$



(D)

the particle is moving towards origin.

4. B, D

$$F_{\text{net}} = f - kv$$

$$\Rightarrow a = \frac{f}{m} - \frac{kv}{m}$$

As $v \uparrow, a \downarrow$ and when $a=0$, velocity remains constant

5. C, D

$$\xrightarrow{+}$$

$$\xleftarrow{-}$$

$$\frac{\vec{v}}{a} \cdot (v) \uparrow$$

$$\frac{\vec{v}}{a} \cdot (v) \uparrow$$

$$\frac{\vec{v}}{a} \cdot (v) \downarrow$$

$$\frac{\vec{v}}{a} \cdot (v) \downarrow$$

(C) Moving with constant velocity

(D) No

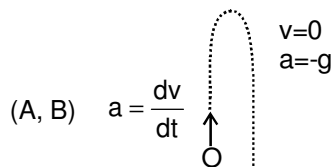
6. A, C

$$|\vec{V}| \uparrow, \vec{V} \uparrow$$

$$\vec{a} = \frac{d\vec{V}}{dt}$$

(C) In circular motion speed may be constant but velocity will not be constant and particle has some acceleration.

7. A, C

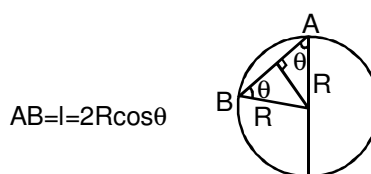
(A) At the top of the motion $v = 0$ but $a = -g$.

$$(A, B) \quad a = \frac{dv}{dt}$$

(C) If particle is moving with constant velocity

(D) No

8. A, D



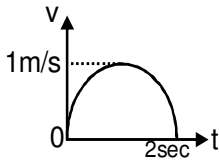
$$a = g \cos \theta$$

$$v^2 = 2 \times g \cos \theta \times 2R \cos \theta$$

$$v \propto \cos \theta \quad \text{and} \quad 2R \cos \theta = \frac{1}{2} g \cos \theta t^2$$

$$t^2 = \frac{4R}{g}$$

9. C



$$\text{Area} = \frac{\pi(1)^2}{2} = \frac{\pi}{2} \text{ m}$$

$$\text{Av velocity} = \frac{\pi}{2 \times 2} = \frac{\pi}{4} \text{ m/s}$$

10. A, B, C, D

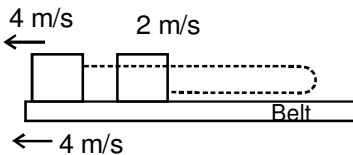
- (a) At T (velocity changes its direction)
 (b) slope constant
 (c) Upper wala area = Niche wala area
 (d) Initial speed = final speed.

11. B, C, D

$$s = ut - \frac{1}{2}at^2$$

$$\therefore -4 = 2 + a \times 4$$

$$a = -\frac{3}{2} \text{ m/s}^2$$



- (B) Now $s = 2 \times 4 - \frac{1}{2} \times \frac{3}{2} \times (4)^2$
 $= 8 - 12 = -4 \text{ m}$ (w.r.t. ground)
 w.r.t. Belt

- (C) $u_i = 6 \text{ m/s}$ and $v = 0$

$$s = 6 \times 4 - \frac{1}{2} \times \frac{3}{2} \times (4)^2$$

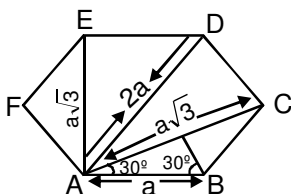
$$= 24 - 12 = 12 \text{ m}$$

- (D) Displacement w.r.t. ground is zero

$$0 = 2 \times t - \frac{1}{2} \times \frac{3}{2} \times t^2$$

$$t = \frac{8}{3} \text{ sec}$$

12. A, C, D



- (A) A to F

$$\text{Average velocity} = \frac{\text{Total Displacement}}{\text{Total time}}$$

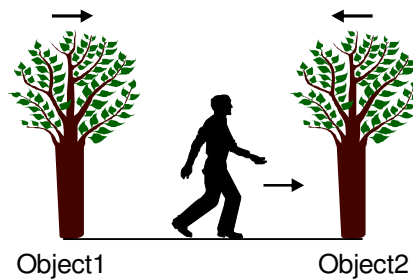
$$= \frac{a}{5a/v} = \frac{v}{5}$$

$$(B) \text{ A to D} = \frac{2a}{3a/v} = \frac{2}{3}v$$

$$(C) \text{ A to C} = \frac{a\sqrt{3}}{2a/v} = \frac{v\sqrt{3}}{2}$$

$$(D) \text{ A to B} = \frac{a}{a/v} = v$$

13. A, B, C



14. C, D
 From theory.

15. C, D

$$R = \frac{u^2 \sin 2\theta}{g}$$

$$\sqrt{3} = \frac{20 \sin^2 \theta}{10} \Rightarrow \sin 2\theta = \frac{\sqrt{3}}{2}$$

$$\therefore \theta = 30^\circ$$

$$(A) H_{\max} = \frac{u^2 \sin 2\theta}{2g} = \frac{(\sqrt{20})^2 \times \frac{1}{4}}{2 \times 10} = 0.25 \text{ m}$$

$$(B) \text{ Minimum Velocity } u \cos \theta$$

$$= \sqrt{20} \times \cos 30^\circ$$

$$= \sqrt{20} \times \frac{\sqrt{3}}{2} = \sqrt{15} \text{ m/s}$$

16. A, B, C, D

$$h = \frac{u^2}{2g} \Rightarrow u = \sqrt{2gh}$$

$$(a) R_{\max} = \frac{u^2}{g} = 2h$$

$$(b) R = nH_{\max}$$

$$\frac{u^2 \sin 2\theta}{g} = n \frac{u^2 \sin^2 \theta}{2g}$$

$$4 = n \tan \theta$$

$$\theta = \tan^{-1} \left(\frac{4}{n} \right)$$

$$(c) \quad gT^2 = g \times \frac{4u^2 \sin^2 \theta}{g^2} = \frac{2 \times u^2 \sin 2\theta}{g} \times \tan \theta$$

$$gT^2 = 2R \tan \theta$$

$$(d) \quad T = \frac{2u_y}{g}, H_{\max} = \frac{u_y^2}{2g}$$

$$\therefore \text{Ratio } 1:1$$

17. A,B

Put the value of T, R, H, in the given equation and solve each option.

18. A,B,C,D

$$y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$

$$\text{Given } y = ax - bx^2$$

$$\text{on comparing } \tan \theta = a \quad b = \frac{g}{2u^2 \cos^2 \theta}$$

$$\therefore 1 + \tan^2 \theta = \sec^2 \theta = 1 + a^2$$

$$b = \frac{g}{2u^2} (1 + a^2) \Rightarrow u = \left(\frac{g}{2b} (1 + a^2) \right)^{1/2}$$

$$\therefore u_x = u \cos \theta = u \cdot \frac{1}{\sqrt{1 + a^2}}$$

$$\text{and } \theta = \tan^{-1}(a)$$

19. A,C,D

$$T = \sqrt{\frac{2H}{g}} \Rightarrow 0.4 = \sqrt{\frac{2H}{g}}$$

$$\Rightarrow H = 0.8\text{m}$$

$$R = 0.4 \times 4 = 1.6\text{m}$$

$$\text{and } U_y = \sqrt{2gH} = \sqrt{2 \times 10 \times 0.8} = 4\text{m/s}$$

$$\theta = 45^\circ$$

20. B

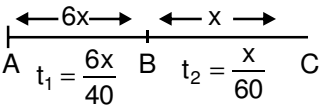
As $\theta \uparrow$, H and T both increases

But R $\uparrow$ from 0° to 45° & at $\theta = 45^\circ$ Max then decreases

Ans (B) R $\uparrow$ then $\downarrow$ [θ from 30° to 60°]

while H $\uparrow$ and T $\uparrow$.

EXERCISE – III**SUBJECTIVE PROBLEMS**

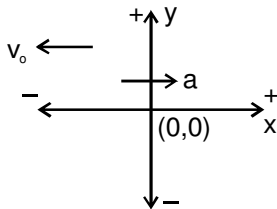
1. 

$$\text{Average speed} = \frac{\text{Total distance travelled}}{\text{Total time taken}}$$

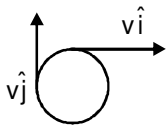
$$= \frac{7x}{\frac{6x}{40} + \frac{x}{60}}$$

$$= 42 \text{ km/hr}$$

2. As the particle is left



3.



$$\text{Change in velocity} = v_j - v_i$$

$$v = \frac{2\pi R}{60} = \frac{2\pi \times 10}{60} = \frac{\pi}{3} \text{ cm/min}$$

$$|\Delta v| = \sqrt{2}v = \sqrt{2} \times \frac{\pi}{3} = \frac{\sqrt{2}\pi}{3} \text{ cm/min}$$

4.

$$v_i = 54 \text{ km/hr} = 15 \text{ m/s}$$

$$v_f = 0 \therefore 0 = 15 - 0.3t$$

$$\Rightarrow t = 50 \text{ sec}$$

Distance travelled by the locomotive

$$s = ut - \frac{1}{2}at^2$$

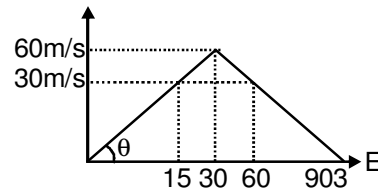
$$s = 15(50) - \frac{1}{2}(0.3)(50)^2$$

$$= 375 \text{ m}$$

$$\text{Position of the locomotive} = 400 - 375$$

$$= 25 \text{ m}$$

5.



$$\tan \theta = \frac{v_{\max}}{30}$$

$$v_{\max} = 30 \times 2$$

$$= 60 \text{ m/s}$$

(a) Total Distance

$$= \frac{1}{2} \times 30 \times 60 + \frac{1}{2} \times 60 \times 60$$

$$= 2700 \text{ m}$$

$$= 2.7 \text{ km}$$

(b) Max Speed

$$2 = \tan \theta = \frac{v_{\max}}{30}$$

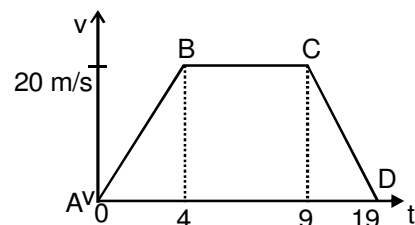
$$v_{\max} = 60 \text{ m/s}$$

(c) Positions of the train

$$\text{I}^{\text{st}} \text{ Position} = \frac{1}{2} \times 15 \times 30 = 225 \text{ m}$$

$$\text{II}^{\text{nd}} \text{ Position} = 2700 - \frac{1}{2} \times 30 \times 30 = 2250 \text{ m}$$

6.



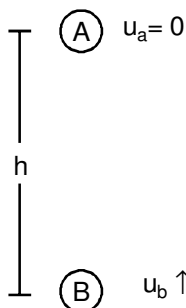
$$\text{for AB } 20 = 0 + 5t \Rightarrow t = 4 \text{ sec}$$

$$\text{for CD } 0 = 20 - 2t \Rightarrow t = 10 \text{ sec}$$

$$\text{Area covered} = \frac{1}{2} \times 20 \times 4 + 5 \times 20 + \frac{1}{2} \times 10 \times 20$$

$$= 240 \text{ m}$$

7. Max height of B

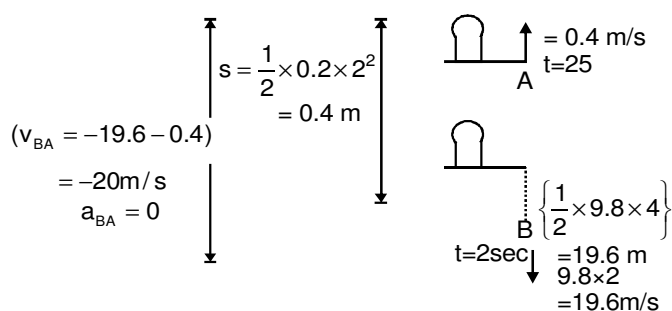


$$\frac{u^2}{2g} = 4h \Rightarrow u_B = \sqrt{8gh}$$

$$\text{Relative velocity } V_{AB} = 0 - \sqrt{8gh} = -\sqrt{8gh}$$

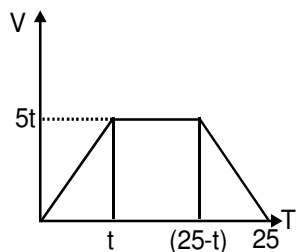
$$t = \frac{h}{\sqrt{8gh}} = \sqrt{\frac{h}{8g}}$$

8.



for next 1.5 sec
 $= 20 \times 1.5 = 30 \text{ m}$
 Total Distnace = $20 + 30 = 50 \text{ m}$

9. Area of V-T curve give displacement.
 Distnace travelled by the particle
 $= 50 + 50 = 100 \text{ m}$
 Av. velocity = zero



10.

$$\tan \theta = \frac{v_{\max}}{t} = 5$$

$$v_{\max} = 5t$$

$$\text{Displacement} = \frac{1}{2} \times t \times 5t + (25 - 2t) \times 5t + \frac{1}{2} \times t \times 5t = 125t - 5t^2$$

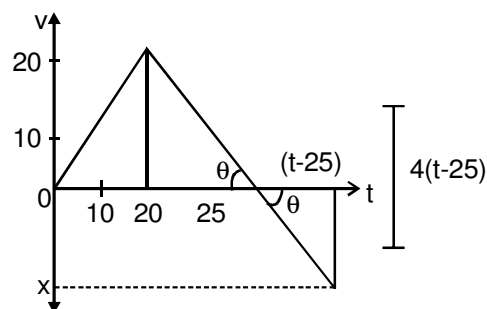
$$\text{Average velocity} = \frac{125t - 5t^2}{25}$$

$$125t - 5t^2 = 500$$

$$t = 20, 5$$

ans $t = 5 \text{ sec}$

11. Particle return to starting point
 it means displacement = 0
 $\therefore$ upper wala area = Niche wala area



$$\tan \theta = \frac{20}{5}$$

$$\tan \theta = \frac{x}{(t-25)} \Rightarrow x = 4(t-25)$$

Now, $\frac{1}{2} \times 20 \times 20 + \frac{1}{2} \times 5 \times 20 = \frac{1}{2} (t-25) \times 4(t-25)$
 On solving $t = 36.2 \text{ sec}$

12.

$$\text{At } t = 2 \text{ sec } \therefore \theta = 45^\circ$$

$$\therefore v_y = v_x$$

 for $t = 4 \text{ sec}$, $u_y = 0$

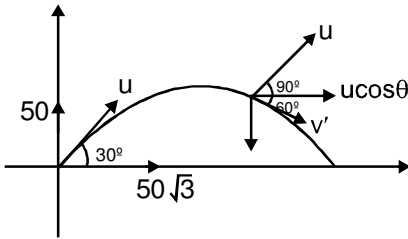
$$T = \frac{u_y}{g} \Rightarrow u_y = 40 \text{ m/s}$$

$$\text{st } t = 2 \text{ sec } v_y = 40 - 20 = 20$$

 $\therefore v_y = v_x = 20$

$$v = \sqrt{(20)^2 + (40)^2} = 20\sqrt{5}$$

13.



$$u_x = 50\sqrt{3} \text{ m/s}$$

$$u_y = 50 \text{ m/s}$$

$$V_x = u_x = 50\sqrt{3}$$

$$V_y = u_y - gt = 50 - 10t$$

$$\tan(-60) = \frac{50 - 10t}{50\sqrt{3}}$$

$$t = 20 \text{ sec}$$

14.

$$y = \sqrt{3}x - \frac{gx^2}{2}$$

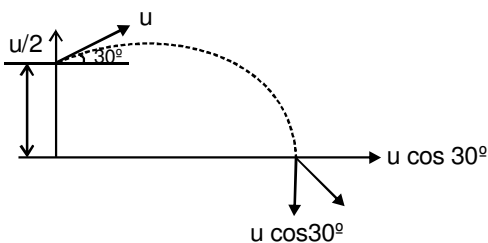
$$y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$

$$\text{on comparing } \tan \theta = \sqrt{3} \quad \theta = 60^\circ$$

$$\text{and } u^2 \cos^2 \theta = 1$$

$$u = 2 \text{ m/s}$$

15.



$$-\frac{u\sqrt{3}}{2} = \frac{u}{2} - 10 \times 5$$

$$u = \frac{100}{\sqrt{3} + 1} = 50(\sqrt{3} - 1) \text{ m/sec}$$

16.

$$s = 100 \times 3 + \frac{1}{2} \times 30 \times 3^2$$

$$= 435 \text{ m}$$

$$H_{\max} = \frac{(190)^2}{2 \times 10} \times \sin^2 53^\circ = 1155.2$$

(a)

$$\text{Total} = 348 + H_{\max}$$

$$= 348 + 1155.2$$

$$= 1503.2 \text{ m} = \text{maximum altitude}$$

(b)

$$u = 190 \sin 53^\circ; -a_y = 10; s_y = -348$$

$$-348 = 152t - \frac{1}{2} \times 10 \times t^2$$

$$5t^2 - 152t - 348 = 0$$

$$t = 32.54 \text{ sec}$$

$$\text{Total} = 35.54 \text{ sec}$$

(c)

$$R = 435 \cos 53^\circ + 190 \cos 53^\circ \times 32.54$$

$$= 435 \times \frac{3}{5} + 190 \times \frac{2}{5} \times 32.54$$

$$= 3970.56 \text{ m}$$

17.

$$\sqrt{\frac{2h}{g}} = 5 \text{ sec } (h = y)$$

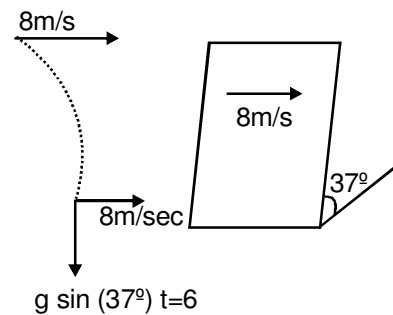
$$y = 125 \text{ m}$$

$$\text{Now, } \tan 37^\circ = \frac{125}{x} \Rightarrow \frac{3}{4} = \frac{125}{x}$$

$$x = 500/3$$

$$\therefore x = u \times 5 \Rightarrow u = \frac{100}{3} \text{ m/s}$$

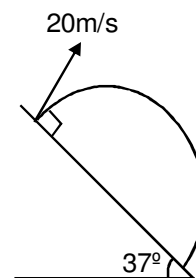
18.



$$g \sin(37^\circ) t = 6$$

$$V = \sqrt{6^2 + 8^2} = 10 \text{ m/s}$$

19.



$$T = \frac{2u}{g \cos 37^\circ} = \frac{2 \times 20}{10 \times 4/5}$$

$$R = \frac{1}{2} a_x T^2$$

$$R = \frac{1}{2} \times 10 \sin 37^\circ \times T^2$$

$$= \frac{1}{2} \times 10 \times \frac{3}{5} \times (5)^2 = 75\text{m}$$

20.

$$R = \frac{u^2 \sin 2\theta}{g}; H = \frac{u^2 \sin^2 \theta}{2g}$$

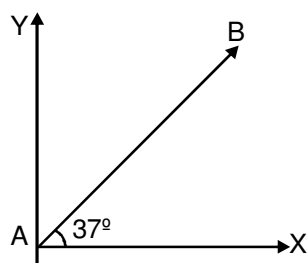
$$T = \frac{2u \sin \theta}{g}; a_x = g/2$$

Due to acceleration in x-direction range will increase.

Now,
$$R' = u \cos \left(\frac{2u \sin \theta}{g} \right) + \frac{1}{2} \times \frac{g}{2} \times \left(\frac{2u \sin \theta}{g} \right)^2$$

$$R' = \frac{u^2 \sin 2\theta}{g} + \frac{u^2 \sin^2 \theta}{g} = R + 2H$$

21.



$$\vec{v}_{bw} = \vec{v}_b - \vec{v}_w$$

$$\vec{v}_b = \vec{v}_{bw} + \vec{v}_w$$

$$= 10\hat{i} + 12\hat{j} + u\hat{i}$$

$$= (10+u)\hat{i} + 12\hat{j}$$

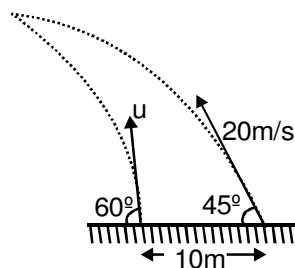
$$\tan 37^\circ = \frac{12}{10+u} \Rightarrow \frac{3}{4} = \frac{12}{10+u}$$

$$10+u = 16$$

$$u = 6\text{m/s}$$

22.

Vertical component of both particle be same for collision of particle.

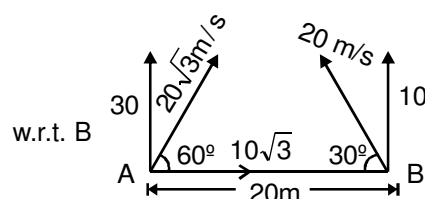


$$\frac{u\sqrt{3}}{2} = \frac{20}{\sqrt{2}}$$

$$u = \frac{40}{\sqrt{6}}$$

$$u = 20\sqrt{\frac{2}{3}}$$

23.

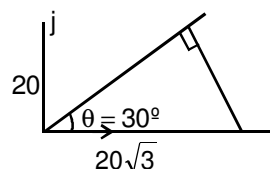


$$v_{ABx} = 10\sqrt{3} - (-10\sqrt{3}) = 20\sqrt{3}\text{m/s}$$

$$v_{AB_y} = 30 - 10 = 20\text{m/s}$$

$$\vec{V}_{AB} = 20\sqrt{3}\hat{i} + 20\hat{j}$$

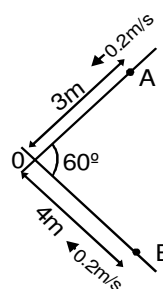
$$\tan \theta = \frac{20}{20\sqrt{3}}$$



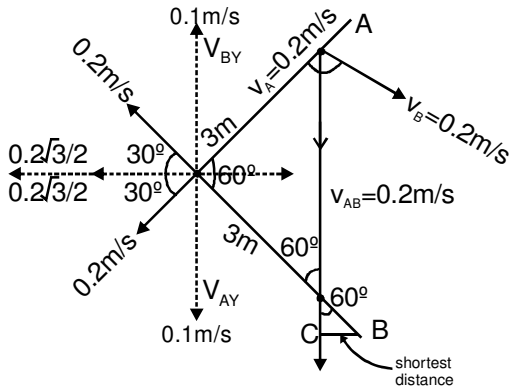
$$\tan \theta = \frac{1}{\sqrt{3}} \Rightarrow \theta = 30^\circ$$

$$x = 20 \sin 30^\circ \Rightarrow x = 10\text{m}$$

24.



Now, we solve the problem w.r.t. B then



shortest Distance $BC = 1 \sin 60^\circ$
 $= \frac{\sqrt{3}}{2} \text{ m} = 50\sqrt{3} \text{ cm}$

25.

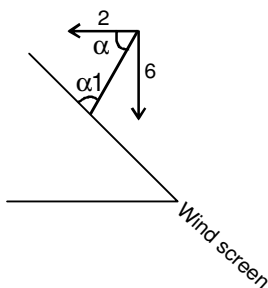
$$\vec{v}_{rw} = \vec{v}_r - \vec{v}_w$$

$$\vec{v}_r = \vec{v}_{rw} + \vec{v}_w = -20\hat{j} + 15\hat{i}$$

$$\vec{v}_{rm} = \vec{v}_r - \vec{v}_m = -20\hat{j} + 15\hat{i} - 5\hat{i} = 10\hat{i} - 20\hat{j}$$

$$\tan \theta = \frac{10}{20} \Rightarrow \theta = \tan^{-1}\left(\frac{1}{2}\right)$$

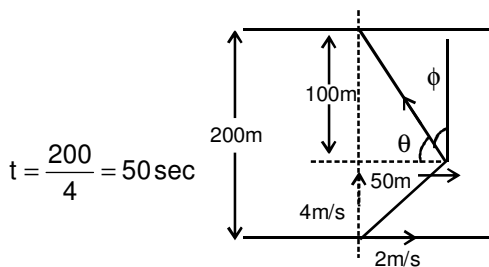
26.



$$\vec{v}_{rc} = \vec{v}_r - \vec{v}_c$$

$$\tan \alpha = \frac{6}{2} \Rightarrow \alpha = \tan^{-1}(3)$$

27.

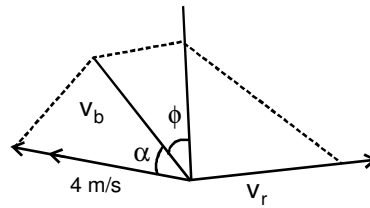


$$t = \frac{200}{4} = 50 \text{ sec}$$

$$\tan \theta = 2$$

$$\tan \phi = \frac{1}{2}$$

$$4 \sin \alpha = 2 \sin (90 + \phi)$$



$$4 \sin \alpha = 2 \cos \phi$$

$$\sin \alpha = \frac{2 \cos \phi}{4} = \frac{2}{4} \times \frac{2}{\sqrt{5}} = \frac{1}{\sqrt{5}}$$

$$t = \frac{100}{4 \cos(\alpha + \phi)} = \frac{100}{4(\cos \alpha \cos \phi - \sin \alpha \sin \phi)}$$

$$t = \frac{100}{4 \times \frac{3}{5}} = \frac{125}{3}$$

28.

$$t_{\min} = \frac{d}{v_{br}} = 10 \times 60 \text{ sec}$$

$$t_{\min} = 600 \text{ sec}$$

$$120 = v_r \times 600$$

$$v_r = \frac{1}{5} \text{ m/s}$$

$$\sin \theta = \frac{v_r}{v_{br}} = \frac{1}{v_{br} \times 5}$$

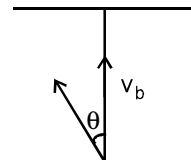
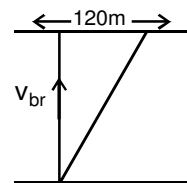
$$12.5 \times 60 = \frac{d}{v_{br} \cos \theta}$$

$$12.5 \times 60 = \frac{10 \times 60}{\cos \theta}$$

$$\cos \theta = \frac{4}{5} \Rightarrow \theta = 37^\circ$$

$$\text{Now, } \frac{3}{5} = \frac{1}{v_{br} 5}$$

$$v_{br} = \frac{1}{3} \text{ m/s}$$



EXERCISE – IV

TOUGH SUBJECTIVE PROBLEMS

1

Bill board
t = 0

t = 2 sec t = 14 sec

← 2U → ← 12U → ← Ut →

← $\frac{1}{2} \times \left[\frac{150 \times 5}{18} \times \frac{1}{12} \right] \times 12^2$ → ← $\frac{150 \times 5}{18} \times t$ →

← 1500 m →

$$14U + Ut = 1500 \text{ m} \quad \dots(1)$$

$$\frac{1}{2} \times \frac{150 \times 5}{18} \times \frac{1}{12} \times 12^2 + \frac{150 \times 5}{18} \times t = 1500 \text{ m}$$

$$\Rightarrow t = 30 \text{ sec}$$

$$U(30 + 14) = 1500 \text{ m} \Rightarrow U = 122.7 \text{ km/hr}$$

2 Bullets will spread in a area of radius equal to the range of bullets. Therefore for area to be maximum. Range

should be maximum. i.e. $\frac{v^2}{g}$

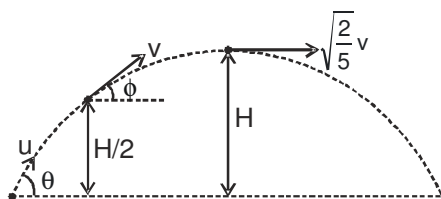
$$A = \frac{\pi v^4}{g^2}$$

3

$$v^2 - u^2 = 2\vec{a} \cdot \vec{S}_y$$

$$\frac{2}{5}v^2 - u^2 = -2gH \Rightarrow v^2 - u^2 = -\frac{2gH}{2}$$

$$\frac{3}{5}v^2 = g \times \frac{(U \sin \theta)^2}{2g} \Rightarrow U \sin \theta = \sqrt{\frac{6}{5}} v$$



$$U \cos \theta = \sqrt{\frac{2}{5}} v$$

$$\tan \theta = \sqrt{3} \Rightarrow \theta = 60^\circ$$

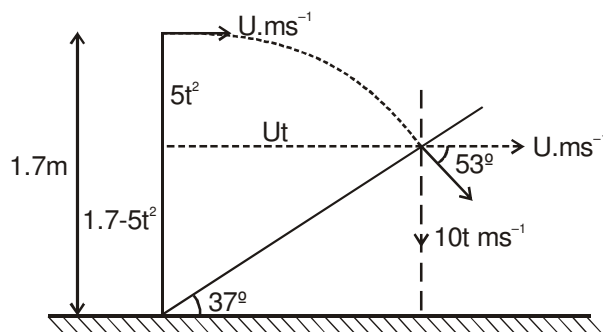
$$v \cos \phi = \sqrt{\frac{2}{5}} v \Rightarrow \phi = \cos^{-1} \sqrt{\frac{2}{5}}$$

4

$$\tan 53^\circ = \frac{10t}{U}$$

$$\Rightarrow \frac{4}{3} = \frac{10t}{U} \quad \dots(1)$$

$$\tan 53^\circ = \frac{Ut}{1.7 - 5t^2} \quad \dots(2)$$



from (1) & (2) : $t = \frac{2}{5} \text{ sec}$

from (1) : $U = \frac{3}{4} \times 10 \times \frac{2}{5}$

$$U = 3 \text{ ms}^{-1}$$

5

Let us choose the x and y directions along OB and OA respectively. Then,

$$u_x = u = 10\sqrt{3} \text{ m/s}, u_y = 0$$

$$a_x = -g \sin 60^\circ = -5\sqrt{3} \text{ m/s}^2$$

$$\text{and } a_y = -g \cos 60^\circ = -5 \text{ m/s}^2$$

(a) At point Q, x-component of velocity is zero. Hence, substituting in

$$v_x = u_x + a_x t$$

$$0 = 10\sqrt{3} - 5\sqrt{3}t \Rightarrow t = \frac{10\sqrt{3}}{5\sqrt{3}} = 2 \text{ s}$$

Ans.

(b) At point Q, $v = v_y = u_y + a_y t$

$$\therefore v = 0 - (5)(2) = -10 \text{ m/s}$$

Ans.

Here, negative sign implies that velocity of particle at Q is along negative y direction.

(c) Distance PO = |displacement of particle along y-direction| = $|s_y|$

$$\text{Here, } s_y = u_y t + \frac{1}{2} a_y t^2 = 0 - \frac{1}{2} (5)(2)^2 = -10 \text{ m}$$

$$\therefore PO = 10 \text{ m}$$

Therefore, $h = PO \sin 30^\circ = (10) \left(\frac{1}{2}\right)$ or $h =$

5m **Ans.**

(d) Distance OQ = displacement of particle along x-direction = s_x

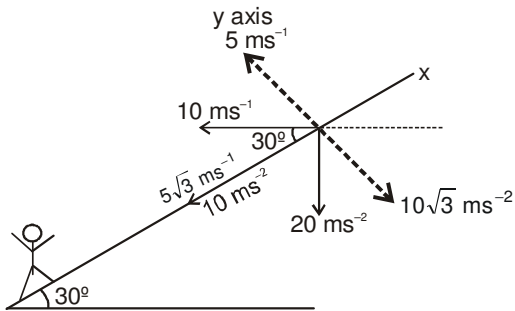
$$\text{Here, } s_x = u_x t + \frac{1}{2} a_x t^2 = (10\sqrt{3})(2) - \frac{1}{2}(5\sqrt{3})(2)^2 = 10\sqrt{3} \text{ m}$$

$$\text{or } OQ = 10\sqrt{3} \text{ m}$$

$$PQ = \sqrt{(PO)^2 + (OQ)^2} = \sqrt{(10)^2 + (10\sqrt{3})^2} = \sqrt{100 + 300} = \sqrt{400}$$

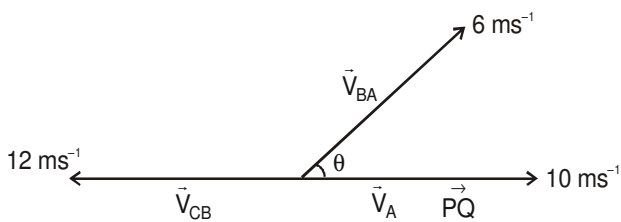
$$PQ = 20 \text{ m}$$

6



$$0 = 5T - \frac{1}{2} \times 10\sqrt{3} T^2 \Rightarrow T = \frac{1}{\sqrt{3}}$$

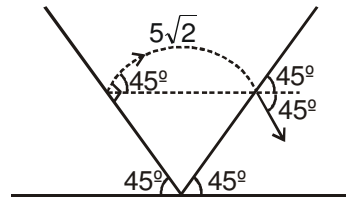
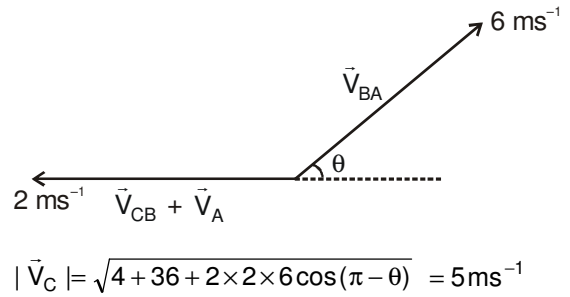
7



$$\therefore \vec{V}_C = \vec{V}_{CB} + \vec{V}_B$$

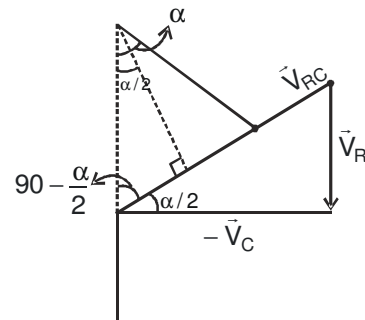
$$= \vec{V}_{CB} + \vec{V}_{BA} + \vec{V}_A$$

8



$$T = \frac{2 \times 5\sqrt{2} \sin 45^\circ}{g} = 1 \text{ sec}$$

9



$$\tan \alpha/2 = \frac{|\vec{V}_R|}{|-\vec{V}_C|} = \frac{2}{6} \Rightarrow \alpha = 2 \tan^{-1}(1/3)$$

10

$$\frac{1}{2} g t^2 = 4$$

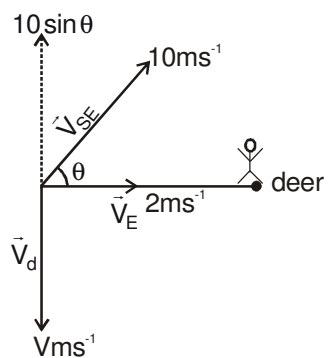
$$\Rightarrow t = \frac{2}{\sqrt{5}} \text{ sec [Time taken by spear to reach deer]}$$

Motion in horizontal plane

$$\vec{a}_{\text{horizontal}} = \vec{0}$$

$$10 \sin \theta = v_d$$

$$(10 \cos \theta + 2) \frac{2}{\sqrt{5}} = 4\sqrt{5}$$

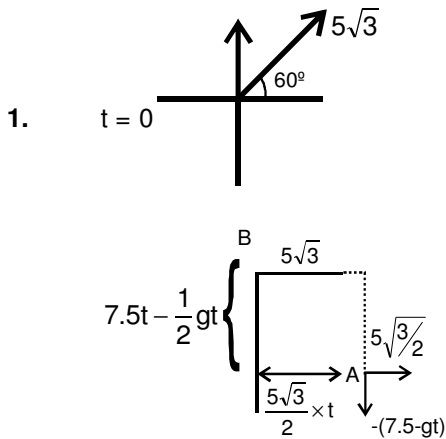
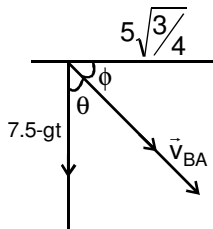


$$\Rightarrow \theta = 37^\circ$$

$$\therefore V_d = 6 \text{ ms}^{-1}$$

EXERCISE – V

JEE QUESTIONS

w.r.t A at $t = t$ 

$$\tan \phi = \frac{7.5 - gt}{5\sqrt{3}/2}$$

$$= - \frac{\left(7.5t - \frac{1}{2}gt^2\right)}{\frac{5\sqrt{3}}{2} \cdot t}$$

$$= 7.5 - gt = -7.5 + \frac{gt}{2}$$

$$15 = \frac{3gt}{2}$$

$$t = 1 \text{ sec (Gap)}$$

2.

$$y = ax - bx^2$$

$$y = x \tan \theta - \frac{gx^2}{24^2 \cos^2 \theta} \text{ on comparing}$$

$$\tan \theta = a \text{ and } b = g/2u^2 \cos^2 \theta$$

$$\theta = \tan^{-1}(a)$$

$$\text{For } u_{\max} \frac{dy}{dx} = 0 \Rightarrow a - 2bx = 0$$

$$x = \frac{a}{2b}$$

3. Acceleration w.r.t. box is $g \cos \theta$

$$T = \frac{2u_y}{a_y} = \frac{2u \sin \alpha}{g \cos \theta}$$

for Box $a_x = 0$

$$\therefore R = \frac{2u \sin \alpha \cdot u \cos \alpha}{g \cos \theta}$$

$$= \frac{u^2 \sin 2\alpha}{g \cos \theta}$$

$$3(b) \vec{v}_{PB} = \vec{v}_P - \vec{v}_B$$

$$\vec{v}_{PB} = u \cos(\alpha + \theta) \hat{i} + u \sin(\alpha + \theta) \hat{j}$$

$$\vec{v}_B = -v \cos \theta \hat{i} - v \sin \theta \hat{j}$$

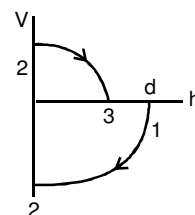
$$\therefore \vec{v}_P = u \cos(\alpha + \theta) \hat{i} + u \sin(\alpha + \theta) \hat{j} - v \cos \theta \hat{i} - v \sin \theta \hat{j}$$

$$3 \quad (b) \quad \hat{i} \text{ component zero} \Rightarrow v = u \frac{\cos(\alpha + \theta)}{\cos \theta}$$

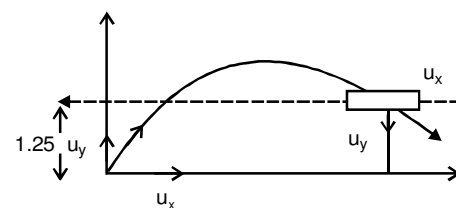
4. B
Nahi.....

5. A

$$\therefore v^2 = u^2 \pm 2gh$$

 $\therefore v-h$ graph gives parabolainitially v is $\downarrow$ and after collision v $\uparrow$ At $t=0$ $h = d$ 1 $\rightarrow$ 2 v $\uparrow$ (Downwards)At 2 v change directionAt 2-3 v $\downarrow$ (upwards)

6.



$$v_y = u_y + a_y t$$

$$-u_x = u_y - gt \quad (1)$$

$$u_x t = 3 + \frac{1}{2} \times 1.5t^2 \quad (2)$$

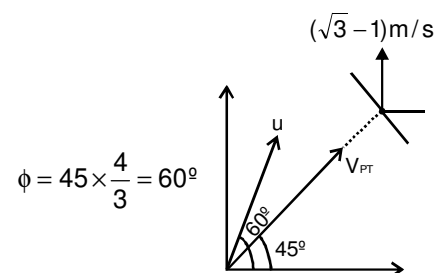
$$1.25 = u_y t - \frac{1}{2} gt^2 \quad (3)$$

on solving $u = 7.29 \text{ m/sec}$

$t = 1 \text{ sec}$

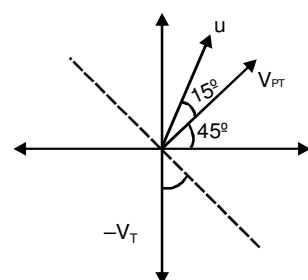
7.

Socho



$$\vec{v}_{PT} = \vec{v}_P - \vec{v}_T$$

$$v_T \cos 45^\circ = u \sin 15^\circ$$



$$\frac{v_T}{\sqrt{2}} = \frac{u(\sqrt{3}-1)}{2\sqrt{2}}$$

$$u = 2 \text{ m/s}$$

8.

B

$$\text{Area} = v_f - v_i \quad a = \frac{dv}{dt}$$

$$\frac{1}{2} \times 11 \times 10 = v_f - 0 \quad dv = \int a dt$$

$$v_f = 55 \text{ m/s}$$

9.

C

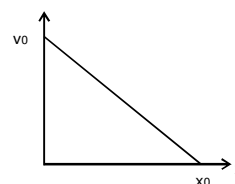
Nahi.....

10.

B

$$v \frac{dv}{dx} \text{ is negative}$$

$$\frac{dv}{dx} \text{ is constant}$$



but, v is decreasing with x

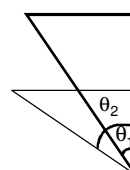
$$\therefore \left| v \frac{dv}{dx} \right| \text{ is decreasing}$$

$\therefore$ B is correct.

11.

B

$$\theta_2 > \theta_1$$



12.

$$t = \frac{2u \sin \theta}{g} \therefore t = \frac{2 \times 10 \times \sqrt{3}/2}{10} = \sqrt{3} \text{ sec}$$

Now

$$S = ut + \frac{1}{2} at^2$$

$$\therefore 1.15 = 5 \times \sqrt{3} - \frac{1}{2} \times a \times 3$$

$$\text{or } 1.15 = 5\sqrt{3} - \frac{3a}{2}$$

$$\text{or } a = 5 \text{ m/s}^2$$