

EXERCISE – III**SUBJECTIVE PROBLEMS**

- $10^6 \times 28.2 = \Delta m \cdot 931 \times 10^6$
 $\Delta m = 0.03029$
 $\Delta m = 0.03029$ (Take)
 $m_p = 1.007276$
 $m_n = 1.008005$
 $(2 \times m_p + 2 \times m_n - \Delta m)$
 $m_\alpha = 4.001592 \text{ A.M.U.}$
- The no. of protons is ${}^{56}_{26}\text{Fe} = 26$
 The no. of neutrons = $56 - 26 = 30$
 $\text{B.E.} = [26 \times 1.00783 \text{ u} + 30 \times 1.00867 \text{ u} - 55.9349 \text{ u}]c^2$
 $= 492 \text{ MeV}$
- Use energy conservation
 $m({}^{238}\text{Pu})c^2 = m({}^{234}\text{U})c^2 + m({}^4\text{He})c^2 + k$
 $k = [m({}^{238}\text{Pu}) - m({}^{234}\text{U}) - m({}^4\text{He})]c^2$
 $= (238.04955 \text{ u} - 234.04095 \text{ u} - 4.002603 \text{ u})$
 $\frac{931 \text{ MeV}}{\text{u}} = 5.58 \text{ MeV}$
- $[7.0160 + 1.00783 - (2 \times 4.0026)] \times 931$
 $= 17.34 \text{ MeV}$
- ${}^{32}\text{P} \rightarrow {}^{32}\text{S} + {}^0_{-1}\text{e} + \bar{\nu}$
 $\Delta m = 2 \times 10^{-3} \text{ A.M.U.}$
 $E = 1.862 \text{ MeV}$
- ${}^{40}_{19}\text{K} \rightarrow {}^{40}_{20}\text{Ca} + {}^0_{-1}\text{e} + \bar{\nu}$
 $E = \Delta m(931) = 1.3034$
- $\Delta m 931 = E$
 $\therefore \alpha \text{ particle energy} = E - 217 \text{ Kev}$
- $\Delta m = 12.018613 - 12 - 2 \times 0.0005486$
 $\therefore E = 16.3072$
 $E_{e^+} = 16.3072 - 4.43 = 11.88 \text{ MeV}$
- (a) The Q - Value of β^- decay is
 $Q = [m({}^{19}\text{O}) - m({}^{19}\text{F})]c^2$
 $= 4.816 \text{ MeV}$
 (b) The Q - Value of β^+ decay is
 $Q = [m({}^{23}\text{Al}) - m({}^{25}\text{Mg}) - 2mc^2]c^2$
 $= \left[24.990432 \text{ u} - 24.985839 \text{ u} - 2 \times 0.511 \frac{\text{MeV}}{c^2} \right] c^2$
 $= (0.004593) - (931 \frac{\text{MeV}}{\text{u}}) - 1.022 \text{ MeV}$
 $= 3.254 \text{ MeV}$
- The kinetic energy available for the beta particle and the antineutrino is
 $Q = [m({}^{175}\text{Lu}) - m({}^{176}\text{Hf})]c^2$
 $= (175.942694 \text{ u} - 175.941420 \text{ u}) (931 \frac{\text{MeV}}{\text{u}})$
 $= 1.182 \text{ MeV}$

- * This energy is shared by the beta particle and the antineutrino.
 So Max K.E. = 1.182 MeV when antineutrino do not get any share
- If the product nucleus ${}^{198}\text{Hg}$ is formed in its ground state, the kinetic energy available to the e^- and antineutrino is
 $Q = [m({}^{198}\text{Au}) - m({}^{198}\text{Hg})]c^2$
 As ${}^{198}\text{Hg}$ has energy 1.088 MeV more than ${}^{198}\text{Hg}$ is 9.5, K.E. actually available is
 $Q = [m({}^{198}\text{Au}) - m({}^{198}\text{Hg})]c^2 - 1.088$
 $= 0.2806 \text{ MeV}$ (Max^m K.E. of the e^- emitted)
 - Rate = 300 MW = $300 \times 10^6 \text{ J/s}$
 Energy in one second = $300 \times 10^6 \text{ J}$
 Energy from one fission = $200 \times 10^6 \times 1.6 \times 10^{-19} \text{ s}$

$$\text{No of fission} = \frac{3 \times 1}{2 \times 1.6 \times 10^{-19}}$$

 $= \text{No of u-nucleus}$
 Gm-moles n

$$= \frac{1.5 \times 10^{19}}{1.6 \times 6.023 \times 10^{23}} = 0.1556 \times 10^{-4}$$

 amount = n M = $36.578 \times 10^{-4} \text{ gm}$
 $\Rightarrow 3.6578 \text{ mg} = 3.7 \text{ mg}$
 - Q value =
 $[2(4.0026) - 8.0053]931 = -1 \times 10^{-4} \times 931$
 $= -931 \times 10^{-4} \text{ MeV} \times 10^3 = -93.1 \text{ KeV}$
 Q value is energy released So because q value is -ve hence energy has to be given.
 - $B({}_1\text{H}^2) = 1.1 \text{ MeV}$
 $B({}_2\text{He}^4) = 7.0 \text{ MeV}$
 Energy release = $4(7.0) - 4(1.1)$
 $= 28 - 4.4 = 23.6 \text{ MeV}$
 - Mass of ${}_1\text{H} = 1.67 \times 10^{-27} \text{ kg}$
 Now No. of ${}_1\text{H}$ atom is sun

$$= \frac{1.7 \times 10^{50}}{1.67 \times 10^{-27}} \text{ atom}$$

 No. of ${}_2\text{He}$ from = $\frac{1.7 \times 10^{30}}{1.67 \times 10^{-27} \times 4}$
 Energy release

$$= \frac{1.7 \times 10^{30}}{1.67 \times 10^{-27} \times 4} \times 26 \times 10^6 \times 1.6 \times 10^{-19} \text{ Joule}$$

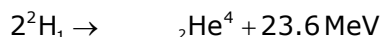
 Time taken = $\frac{\text{Energy release}}{3.9 \times 10^{26}}$

$$= \frac{1.7 \times 10^{30} \times 26 \times 10^6 \times 1.6 \times 10^{-19}}{1.7 \times 10^{-27} \times 4 \times 3.9 \times 10^{26}} = \frac{8}{3} \times 10^{18} \text{ s}$$

16. $E = 2 \times 0.5 = 1 \text{ MeV}$

$$\frac{E}{2} = \frac{hc}{\lambda} = \frac{1.24 \times 10^{-12} \text{ MeV m}}{\lambda}$$

$$\lambda = 2.48 \times 10^{-12} \text{ m} = 2.48 \times 10^{-12} \text{ m}$$



17. $\downarrow \quad \quad \quad \downarrow \quad \quad \quad E = 28 \text{ MeV}$
 $1.1 \times 2 \times 2.2 \quad E - 4.4$

18. $\pi^+ \rightarrow \mu^+ + \text{neutrino}$

$$100 \rightarrow 100 \text{ MeV}$$

$$50 = \frac{1}{2}mv^2 + \frac{hc}{\lambda} \quad mv = \frac{h}{\lambda}$$

$$50 = \frac{1}{2}100 \frac{v^2}{c^2} + 100 \frac{v}{c}$$

$$x^2 + 2x - 1 = 0 \quad x = 0.41 \Rightarrow \frac{v}{c} = 0.41$$

$$\frac{1}{2}mv^2 = \frac{1}{2} \frac{100 \times 10^6 \times 0.41 \times c^2}{c^2} = 9 \times 10^6 \text{ eV}$$

19. $\Delta m = (2.0141) - 4.0024$

$$= 0.0258 \text{ u}$$

$$Q = 0.0258 \times 931$$

$$= 24 \text{ Me}$$

20. $A = A_0 e^{-\lambda t} \quad 500 = 600 e^{-\lambda t}$

$$\lambda = \frac{\ln 6/5}{t} = \frac{\ln(5/6)}{40 \text{ min}}$$

$$\text{Half life } t_{1/2} = \frac{\ln 2}{\lambda} = \frac{\ln 2}{\ln 6/5} \times 40 = 152 \text{ min}$$

21. $\lambda = \frac{\ln^2}{4.5 \times 10^9}$

$$\text{No of } {}^{238}\text{U atoms} = N_u \quad \text{No of } {}^{206}\text{Pb atoms} = N_{pb}$$

$$N_u = N_{pb} e^{-\lambda t}$$

$$e^{-\lambda t} = 1 - e^{-\lambda t}$$

$$t = 4.5 \times 10^9 \text{ y}$$

22.

$$\text{From } N = N_0 [1 - e^{-\lambda t}]$$

$$1 \times 10^5 = N_0 [1 - e^{-\lambda 36}] \quad \dots\dots (1)$$

$$1.11 \times 10^5 = N_0 [1 - e^{-108\lambda}] \quad \dots\dots (2)$$

$$\text{From eq. (1) \& (2)}$$

$$\lambda = \frac{2.27}{36} = 0.0630 \quad t_{1/2} = \frac{0.693}{0.0638} = 10.89 \text{ Sec.}$$

23. ${}^{40}_{19}\text{K} \rightarrow {}^{40}_{18}\text{Ar} + {}^0_{+1}\text{e} + \nu$

$$\lambda = \frac{0.693}{1.4 \times 10^9} \quad N = N_0 e^{-\lambda t}$$

$$1 = 8 e^{-\lambda t} \quad \lambda t = \ln(8) \Rightarrow \frac{2.079 \times 1.4 \times 10^9}{0.693} = t$$

$$t = 4.2 \times 10^9 \text{ years.}$$

24. Given $R = R_0 e^{-\lambda t}$

No of atom disasocile in twis t

$$= 80\%$$

$$\Rightarrow \frac{80 N_0}{100} = N_0 [1 - e^{-\lambda t}] \quad 4 = 5 - 5 e^{-\lambda t}$$

$$\Rightarrow 5 e^{-\lambda t} = 1 \Rightarrow \ln 5 = \lambda t$$

$$t = \frac{\ln 5}{\lambda} = \left(\frac{\ln 5}{\ln 2} \right) \tau$$

25.

$$t_{1/2} = 8 \text{ days}$$

$$A_0 = 20 \mu\text{Ci}$$

$$A = A_0 e^{-\lambda t}$$

26. Since the number o ${}^{206}\text{Pb}$ atoms equals the no. of ${}^{238}\text{U}$ atoms, half of the original ${}^{238}\text{U}$ atom have decayed. It takes one half life to decay half of the active mudei, Thus the sample is $4.5 \times 10^9 \text{ y}$ old

27.

$$t = \frac{1}{\lambda} \ln \left(1 + \frac{N_d}{N_c} \right) \quad t_1 = \frac{1}{\lambda} \ln \left(1 + \frac{1}{9} \right)$$

$$t_2 = \frac{1}{\lambda} \ln(1 + 9) \quad t_1 - t_2 = 24 \text{ min}$$

28. $t = \frac{1}{\lambda} \ln \left(1 + \frac{N_{pb}}{N_u} \right)$

$$t = \frac{4.47 \times 10^9}{\ln 2} \left(1 + \frac{\frac{0.6 \times 10^3}{286}}{\frac{2 \times 10^3}{238}} \right)$$

$$= \frac{4.47 \times 10^9}{\ln 2} \ln(1.34660)$$

$$= 1.92 \times 10^9 \text{ years}$$

29. $\xrightarrow{\alpha} A \xrightarrow{\lambda} B \quad t = 0$

$$N = N_0 e^{-\lambda t} + \frac{R}{\lambda} (1 - e^{-\lambda t})$$

$$N = \frac{1}{\lambda} [\alpha(1 - e^{-\lambda t}) + \lambda N_0 e^{-\lambda/2}]$$

$$\alpha = 2N_0 x$$

$$N_{\lambda/2} = \frac{1}{\lambda} \left[2N_0 \lambda \left(\frac{1}{2} \right) + \frac{\lambda N_0}{2} \right]$$

$$= \frac{3N_0}{2}$$

$$N_{\infty} = \frac{1}{\lambda} [2N_0 \lambda (1 - 0) + \lambda N_0 \times 0] = 2N_0$$