ELECTROSTATICS - 1



Sol.

Sol.

**6.** Two free positive charges 4q and q are a distance *l* apart. What charge Q is needed to achieve equilibrium for the entire system and where should it be placed form charge q ?

(A)  $Q = \frac{4}{9}q$  (negative) at  $\frac{l}{3}$  (B)  $Q = \frac{4}{9}q$  (positive) at  $\frac{l}{3}$ (C) Q = q (positive) at  $\frac{l}{3}$  (D) Q = q (negative) at  $\frac{l}{3}$ **Sol.**  **8.** A charged particle of charge q and mass m is released from rest in an uniform electric field E. Neglecting the effect of gravity, the kinetic energy of the charged particle after time 't' seconds is

(A) 
$$\frac{\text{Eqm}}{\text{t}}$$
 (B)  $\frac{\text{E}^2 q^2 t^2}{2\text{m}}$  (C)  $\frac{2\text{E}^2 t^2}{\text{mq}}$  (D)  $\frac{\text{E}q^2 \text{m}}{2t^2}$ 

Sol.

**9.** Two identical positive charges are fixed on the yaxis, at equal distances from the origin O. A particle with a negative charge starts on the x-axis at a large distance from O, moves along the +x-axis, passes through O and moves far away from O. Its acceleration a is taken as positive along its direction of motion. The particle's acceleration a is plotted against its xcoordinate. Which of the following best represents the plot ?



(A) Zero (B) Along OF (C) Along OC (D) None of these





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Sol.

**10.** Four equal positive charges are fixed at the vertices of a square of side L. Z-axis is perpendicular to the plane of the square. The point z = 0 is the point where the diagonals of the square intersect each other. The plot of electric field due to the four charges, as one moves on the z-axis.



Sol.



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Sol.	<ul> <li>14. Two equal negative charge [0, a] and [0, -a] on the y-ax is released from rest at the p axis. The charge Q will -</li> <li>(A) execute simple harmonic r</li> <li>(B) move to the origin and rer</li> <li>(C) move to infinity</li> <li>(D) execute oscillatory but not a</li> </ul>	es are fixed at the points kis. A positive charge ( points [2a, 0] on the x motion about the origin main at rest simple harmonic motion
<b>12.</b> The charge per unit length of the four quadrant of the ring is $2\lambda$ , $-2\lambda$ , $\lambda$ and $-\lambda$ respectively. The electric field at the centre is -		
(A) $-\frac{\lambda}{2\pi\epsilon_0 R}\hat{i}$ (B) $\frac{\lambda}{2\pi\epsilon_0 R}\hat{j}$ (C) $\frac{\sqrt{2}\lambda}{2\pi\epsilon_0 R}\hat{i}$ (D) None		
Sol.	<b>15.</b> A small particle of mass charge $-q$ is placed at point P axis of uniformly charged rin released. If $R >> x$ , the particulations along the symmetry with an angular free that is equal to -	m and on the ng and cle will axis of quency
	(A) $\sqrt{\frac{qQ}{4\pi\epsilon_0 mR^3}}$ (	B) $\sqrt{\frac{qQx}{4\pi\epsilon_0 mR^4}}$
<b>13.</b> The direction ( $\theta$ ) of $\vec{E}$ at point P due to uniformly charged finite rod will be - (A) at angle 30° from x-axis (B) 45° from x-axis (C) 60° from x-axis (D) none of these <b>Sol.</b>	(C) $\frac{qQ}{4\pi\epsilon_0 mR^3}$ Sol.	(D) $\frac{qQx}{4\pi\epsilon_0 mR^4}$
	<b>16.</b> A charged particle having equilibrium at a height H above charged non-conducting hori The force of gravity acts dowr of the particle will be stable -	some mass is resting ir the centre of a uniformly zontal ring of radius R wards. The equilibrium
	(A) for all values of H (	(B) only if H > R / $\sqrt{2}$
	(C) only if H < R / $\sqrt{2}$ (	(D) only if H = $R / \sqrt{2}$
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Sol.

18. Find the force experienced by the semicircular rod charged with a charge q, placed as shown in figure. Radius of the wire is R and the infinitely long line of charge with linear density  $\lambda$  is passing through its centre and perpendicular to the plane of wire. (A)  $\frac{\lambda q}{2\pi^2 \varepsilon_0 R}$ (B)  $\frac{\lambda q}{\pi^2 \epsilon_0 R}$  (C)  $\frac{\lambda q}{4\pi^2 \epsilon_0 R}$  (D)  $\frac{\lambda q}{4\pi \epsilon_0 R}$ Sol.  $\cdot$  A wheel having mass m has charges +q and -q on diametrically opposite points. It remains in equilibrium on a rough inclined plane in the presence of uniform vertical electric field E = Τe (A) mg  $\frac{mg \tan \theta}{2\pi}$ mg (B) (C) (D) none (D) √<u>5g</u> 2a 2a

**17.** In space of horizontal EF(E = (mg)/q) exist as shown in figure and a mass m attached at the end of a light rod. If mass m is released from the position shown in figure find the angular velocity of the rod when it passes through the bottom most position.

(B)



Sol.

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23. An equipotential surface and a line of force :	
(A) never intersect each other (B) intersect at 45°	
(C) intersect at 60° (D) intersect at 90° <b>Sol.</b>	
	<b>27.</b> In a regular polygon of n sides, each corner is at a distance r from the centre. Identical charges are
<b>24.</b> Which of the following is a volt -(A) Erg per cm(B) Joule per coulomb	placed at $(n - 1)$ corners. At the centre, the intensity is E and the potential is V. The ratio V/E has magnitude.
(C) Erg per ampere (D) Newton / (coulomb × m <sup>2</sup> ) <b>Sol.</b>	<b>Sol.</b>
<b>25.</b> An infinite nonconducting sheet of charge has a surface charge density of $10^{-7}$ C/m <sup>2</sup> . The separation	<b>28.</b> In a certain region of space, the potential is given
whose potential differ by 5V is (A) 0.88 cm (B) 0.88 mm (C) 0.88 m (D) $5 \times 10^{-7}$ m	by $y = x^2 - y^2 + z^2$ ]. The electric field at the point (1,1,1) has magnitude =
Sol.	(A) $k\sqrt{6}$ (B) $2k\sqrt{6}$ (C) $2k\sqrt{3}$ (D) $4k\sqrt{3}$ Sol.
<b>26.</b> In a uniform electric field, the potential is 10 V at the origin of coordinates, and 8V at each of the points	
(1, 0, 0), (0, 1, 0) and $(0, 0, 1)$ . The potential at the point $(1, 1, 1)$ will be -	
(A) 0 (B) 4 V (C) 8 V (D) 10 V	<b>29.</b> When the seperation between two charges is
501.	(A) increases (B) decreases
	(C) remains the same
	(D) may increase or decrease
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30. When a negative charge is released and moves in electric field, it moves toward a position of
(A) lower electric potential and lower potential energy
(B) lower electric potential and higher potential energy
(C) higher electric potential and lower potential energy
(D) higher electric potential and higher potential energy
Sol.

**31.** Four equal charges +q are placed at four corners of a square with its centre of origin and lying in yz plane. The electrostatic potential energy of a fifth charge +q varies or x-axis as



Sol.

**32.** Two identical thin rings, each of radius R meter are coaxially placed at distance R meter apart. If  $Q_1$  and  $Q_2$  coulomb are respectively the charges uniformly spread on the two rings, the work done in moving a charge q from the centre of one ring to that of the other is (A) zero

(B)  $q(Q_1 - Q_2)(\sqrt{2} - 1) / (\sqrt{2}.4\pi\epsilon_0 R)$ (C)  $q\sqrt{2} (Q_1 + Q_2) / 4\pi\epsilon_0 R$ (D)  $q(Q_1 - Q_2)(\sqrt{2} + 1) / (\sqrt{2}.4\pi\epsilon_0 R)$ **Sol.** 

33. Two positively charged particles X and Y are initially far away from each other and at rest. X begins to move towards Y with some initial velocity. The total momentum and energy of the system are p and E.
(A) If Y is fixed, both p and E are conserved
(B) If Y is fixed, E is conserved, but not p
(C) If both are free to move, p is conserved but not E

(D) If both are free, E is conserved, but not p **Sol.** 



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Sol.

**38.** Electric field given by the vector  $\vec{E} = x\hat{i} + y\hat{j}$  is present in the XY plane. A small ring carrying charge +Q, which can freely slide on a smooth non conducting rod, is projected along the rod from the point (0, L) such that it can reach the other end of the rod. What minimum velocity should be given to the ring ? (Assume zero gravity)

(A)  $(QL^2/m)^{1/2}$ (C)  $4(QL^2/m)^{1/2}$ Sol. (L, 0) X (B) 2(QL<sup>2</sup>/m)<sup>1/2</sup> (D) (QL<sup>2</sup>/2m)<sup>1/.2</sup> **39.** A particle of mass 1 kg & charge  $1/3\mu$ C is projected towards a non conducting fixed spherical shell having the same charge uniformly distributed on its surface.

Find the minimum initial velocity of projection required if the particle just grazes the shell.  $V \text{ from } \infty$ 

(A) 
$$\sqrt{\frac{2}{3}}$$
 m/s (B)  $2\sqrt{\frac{2}{3}}$  m/s (C)  $\frac{2}{3}$  m/s (D) none

Sol.

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<b>44.</b> The equation of an equipotential line in an electric field is $y = 2x$ , then the electric field strength vector at (1, 2) may be	Sol.
(A) $4\hat{i} + 3\hat{j}$ (B) $4\hat{i} + 8\hat{j}$ (C) $8\hat{i} + 4\hat{j}$ (D) $-8\hat{i} + 4\hat{j}$ Sol.	
<b>45.</b> The electric field in region is given by : E = $(4axy\sqrt{z})\hat{i} + (2ax^2\sqrt{z})\hat{j} + (ax^2y/\sqrt{z})\hat{k}$ , where a is a positive constant. The equation of an equipotential surface will be of the form - (A) z = constant / $[x^3y^2]$ (B) z = constant / $[xy^2]$ (C) z = constant / $[x^4y^2]$ (D) None <b>Sol.</b>	<b>48.</b> Uniform electric field of magnitude 100 V/m in space is directed along the line $y = 3 + x$ . Find the potential difference between point A(3, 1) & B(1, 3) (A) 100 V (B) $200\sqrt{2}$ V (C) $200$ V (D) 0 <b>Sol.</b>
<b>46.</b> A charge 3 coulomb experiences a force 3000 N when placed in a uniform electric field. The potential difference between two points separated by a distance of 1 cm along the field lines is (A) 10 V (B) 90 V (C) 1000 V (D) 9000 V <b>Sol.</b>	<b>49.</b> A, B, C, D, P and Q are points in a uniform electric field. The potentials at these points are V(A) =2 volt. V(P) = V(B) = V(D) = 5 volt. V(C) = 8 volt. The electric field at P is (A) 10 Vm <sup>-1</sup> along PQ (B) $15\sqrt{2}$ Vm <sup>-1</sup> along PA (C) 5 Vm <sup>-1</sup> along PC (D) 5 Vm <sup>-1</sup> along PA <b>Sol.</b>
<b>47.</b> A uniform electric field having strength $\vec{E}$ is existing in x - y plane as shown in figure. Find the p.d. between origin O & A (d, d, 0)	<b>50.</b> A and B are two points on the axis and the perpendicular bisector respectively of an electric dipole. A and B are far away from the dipole and at equal distance from it. The field at A and B are $\vec{E}_A$ and $\vec{E}_B$ . (A) $\vec{E}_A = \vec{E}_B$ (B) $\vec{E}_A = 2\vec{E}_B$ (C) $\vec{E}_A = -2\vec{E}_B$ (D) $ E_B  = \frac{1}{2} E_A $ , and $\vec{E}_B$ is perpendicular to $\vec{E}_A$
(C) √2Ed (D) None of these <b>MOTION</b> 394,50 - Rajeev Gandhi Nagar Kota, Ph. No. : 93141-87482, 0744-2209671 IVRS No : 0744-2439051. 52. 53. www. motioniitiee.com . hr@motioniitiee.com	

Sol.

**51.** Figure shows the electric field lines around an electric dipole. Which of the arrows best represents the electric field at point P ?



**53.** The dipole moment of a system of charge +q distributed uniformly on an arc of radius R subtending an angle  $\pi/2$  at its centre where another charge -q is placed is.

(A) 
$$\frac{2\sqrt{2}qR}{\pi}$$
 (B)  $\frac{\sqrt{2}qR}{\pi}$  (C)  $\frac{qR}{\pi}$  (D)  $\frac{2qR}{\pi}$ 

**54.** An electric dipole is kept on the axis of a uniformly charged ring at distance  $R/\sqrt{2}$  from the centre of the ring. The direction of the dipole moment is along the axis. The dipole moment is P, charge of the ring is Q and radius of the ring is R. The force on the dipole is nearly

(A) 
$$\frac{4kPQ}{3\sqrt{3}R^2}$$
 (B)  $\frac{4kPQ}{3\sqrt{3}R^3}$  (C)  $\frac{2kPQ}{3\sqrt{3}R^3}$  (D) zero

Sol.



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(C)  $2aq[\hat{i} + \hat{j}]$  (D) none

**55.** A large sheet carries uniform surface charge density  $\sigma$ . A rod of length 2*l* has a linear charge density  $\lambda$  on one half and  $-\lambda$  on the second half. The rod is hinged at mid point O and makes an angle  $\theta$  with the normal to the sheet. The torque experienced by the rod is

(A) 0 (B)  $\frac{\sigma \lambda l^2}{2\epsilon_0} \sin \theta$  (C)  $\frac{\sigma \lambda l^2}{\epsilon_0} \sin \theta$  (D)  $\frac{\sigma \lambda l}{2\epsilon_0}$ 

Sol.

**56.** Two short electric dipoles are placed as shown. The energy of electric interaction between these dipoles will be



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### Sol.

(A) 2qaj

Sol.

**58.** 4 charges are placed each at a distance `a' from origin. The dipole moment of configuration is

(B) 3qaj

--2q



60. Statement - 1 : If electric potential while moving 62. Statement - 1 : The electric potential and the in a certain path is constant, then the electric field electric field intensity at the centre of a square having must be zero. four fixed point charges at their vertices as shown in figure are zero. **Statement - 2 :** Component of electric field  $E_r = -\frac{\partial V}{\partial r}$ .....**\_**—q +a (A) Statement - 1 is true, Statement - 2 is true and statement - 2 is correct explanation for statement - 1. (B) Statement - 1 is true, Statement - 2 is true and statement - 2 is NOT correct explanation for statement - 1. ·····•••+q (C) Statement - 1 is true, statement - 2 is false. (D) Statement - 1 is false, statement - 2 is true. Statement - 2 : If electric potential at a point is zero Sol. then the magnitude of electric field at that point must be zero. (A) Statement - 1 is true, Statement - 2 is true and statement - 2 is correct explanation for statement - 1. (B) Statement - 1 is true, Statement - 2 is true and statement - 2 is NOT correct explanation for statement - 1. (C) Statement - 1 is true, statement - 2 is false. (D) Statement - 1 is false, statement - 2 is true. Sol. **61. Statement - 1 :** For a non-uniformly charged thin circular ring with net charge zero, the electric potential at each point on axis of the ring is zero. Statement - 2 : For a non-uniformly charged thin circular ring with net charge zero, the electric field at any point on axis of the ring is zero. (A) Statement - 1 is true, Statement - 2 is true and statement - 2 is correct explanation for statement - 1. (B) Statement - 1 is true, Statement - 2 is true and statement - 2 is NOT correct explanation for statement - 1. (C) Statement - 1 is true, statement - 2 is false. (D) Statement - 1 is false, statement - 2 is true. Sol.



<b>Exercise - II</b> (One or more than one option is correct	
<ol> <li>Select the correct alternative :         <ul> <li>(A) The charge gained by the uncharged body from a charged body due to conduction is equal to half of the total charge initially present.</li> <li>(B) The magnitude of charge increases with the increase in velocity of charge</li> <li>(C) Charge can not exist without matter although matter can exist without charge</li> <li>(D) Between two non-magnetic substances repulsion is the true test of electrification (electrification means body has net charge)</li> </ul> </li> </ol>	<ul> <li>(A) The third charge experienced a net force inclined to the line joining the charges</li> <li>(B) The third charge is in stable equilibrium</li> <li>(C) The third charge is in unstable equilibrium</li> <li>(D) The third charge experiences a net force perpendicular to the line joining the charges</li> <li>Sol.</li> </ul>
<ul> <li>2. Two equal negative charges -q are fixed at the point (0, a) and (0, -a) on the y-axis. A charge +Q is released from rest at the point (2a, 0) on the x-axis. The charge Q will :</li> <li>(A) Execute simple harmonic motion about the origin.</li> <li>(B) At origin velocity of particle is maximum</li> <li>(C) Move to infinity</li> <li>(D) Execute oscillatory but not simple harmonic motion.</li> <li>Sol.</li> </ul>	<ul> <li>4. A negative point charge placed at the point A is</li> <li> <ul> <li>a</li> &lt;</ul></li></ul>
<b>3.</b> Mid way between the two equal and similar charges, we placed the third equal and similar charge. Which of the following statements is correct, concerned to the equilibrium along the line joining the charges ?	<ul> <li>5. Two fixed charges 4Q (positive) and Q (negative are located at A and B, the distance AB being 3 m.</li> <li><sup>+4Q</sup> <ul> <li>-Q</li> <li>A</li> <li>3m</li> <li>B</li> </ul> </li> <li>(A) The point P where the resultant field due to both is zero is on AB outside AB.</li> <li>(B) The point P where the resultant field due to both is zero is on AB inside AB.</li> <li>(C) If a positive charge is placed at P and displaced slightly along AB it will execute oscillations.</li> <li>(D) If a negative charge is placed at P and displaced slightly along AB it will execute oscillation.</li> </ul>

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Sol.	Sol.
<ul> <li>6. Select the correct statement : (Only force on a particle is due to electric field)</li> <li>(A) A charged particle always moves along the electric line of force.</li> <li>(B) A charged particle may move along the line of force</li> <li>(C) A charge particle never moves along the line of force</li> <li>(D) A charged particle moves along the line of force only if released from rest.</li> <li>Sol.</li> </ul>	<ul> <li>8. The figure shows a nonconducting ring which has positive and negative charge non uniformly distributed on it such that the total charge is zero. Which of the following statements is true ?</li> <li>(A) The potential at all the points on the axis will be zero.</li> <li>(B) The electric field at all the points on the axis will be zero.</li> <li>(C) The direction of electric field at all points on the axis will be along the axis</li> <li>(D) If the ring is placed inside a uniform external electric field then net torque and force acting on the ring would be zero.</li> <li>Sol.</li> </ul>
<b>7.</b> Two infinite sheets of uniform charge density $+\sigma$ and $-\sigma$ are parallele $+\sigma$ to each other as shown in the figure. Electric field at the (A) points to the left or to the right $+ + + + + + + + + + + + + + + + + + +$	<b>9.</b> If we use permittivity $\varepsilon$ , resistance R, gravitational constant G and voltage V as fundamental physical quantities, then - (A) [angular displacement] = $\varepsilon^0 R^0 G^0 V^0$ (B) [Velocity] = $\varepsilon^{-1} R^{-1} G^0 V^0$ (C) [dipole moment] = $\varepsilon^1 R^0 G^0 V^1$ (D) [force] = $\varepsilon^1 R^0 G^0 V^2$ <b>Sol.</b>

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<ul> <li><b>10.</b> A particle of mass m and charge q is thrown in a region where uniform gravitational field and electric field are present. The path of particle</li> <li>(A) may be a straight line (B) may be a circle</li> <li>(C) may be a parabola (D) may be a hyperbola</li> <li><b>Sol.</b></li> </ul>	<ul> <li>12. An electric charge 10<sup>-8</sup> C is placed at the point (4m, 7m, 2m). At the point (1m, 3m, 2m), the electric (A) potential will be 18 V</li> <li>(B) field has no Y-component</li> <li>(C) field will be along Z-axis</li> <li>(D) potential will be 1.8 V</li> <li>Sol.</li> </ul>
<b>11.</b> Two point charges Q and $-Q/4$ are separated by a distance x. Then Q x -Q/4 (A) potential is zero at a point on the axis which is x/ 3 on the right side of the charge $-Q/4$ (B) potential is zero at a point on the axis which is x/ 5 on the left side of the charge $-Q/4$ (C) electric field is zero at a point on the axis which is at a distance x on the right side of the charge $-Q/4$ (D) there exist two points on the axis where electric field is zero. <b>Sol.</b>	<ul> <li>13. Four identical charges are placed at the points (1, 0, 0), (0, 1, 0), (-1, 0, 0) and (0, -1, 0).</li> <li>(A) The potential at the origin is zero.</li> <li>(B) The field at the origin is zero.</li> <li>(C) The potential at all points on the z-axis, other than the origin, is zero.</li> <li>(D) The field at all points on the z-axis, other than the origin acts along the z-axis.</li> <li>Sol.</li> </ul>
	<ul> <li>14. A proton and a deuteron are initially at rest and are accelerated through the same potential difference. Which of the following is false concerning the final properties of the two particles ?</li> <li>(A) They have different speeds</li> <li>(B) They have same momentum</li> <li>(C) They have same kinetic energy</li> <li>(D) None of these Sol.</li> </ul>
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	<ul> <li>19. Two particles of same mass and charge are thrown in the same direction along the horizontal with same velocity v from two different heights h<sub>1</sub> and h<sub>2</sub> (h<sub>1</sub> &lt; h<sub>2</sub>). Initially they were located on the same vertical line. Choose the correct alternative.</li> <li>(A) Both the particles will lie on a vertical line until either of the ball hits the ground</li> <li>(B) Acceleration of the centre of mass of two particles will be g downwards</li> <li>(C) Horizontal displacement of the particle lying at h<sub>1</sub> is less and the particle lying at h<sub>2</sub> is more than the value, which would had been in the absence of charges on them.</li> </ul>
<b>16.</b> Three point charges Q, 4Q and 16Q are placed on a straight line 9cm long. Charges are placed in such a way that the system has minimum potential energy. Then (A) 4Q and 16Q must be at the ends and Q at a distance of 3 cm from the 16Q (B) 4Q and 16Q must be at the ends and Q at a distance of 6 cm from the 16Q (C) Electric field at the position of Q is zero (D) Electric field at the position of Q is $\frac{Q}{4\pi\epsilon_0}$ <b>Sol.</b>	<ul> <li>18. A particle of charge 1μC &amp; mass 1 gm moving with a velocity of 4m/s is subjected to a uniform electric field of magnitude 300 V/m for 10 sec. Then it's final speed cannot be :</li> <li>(A) 0.5 m/s (B) 4 m/s (C) 3 m/s (D) 6 m/s Sol.</li> </ul>
<b>15.</b> Which of the following is true for the figure showing electric lines of force ? (E is electrical field, V is potential) (A) $E_A > E_B$ (B) $E_B > E_A$ (C) $V_A > V_B$ (D) $V_B > V_A$ <b>Sol.</b>	<ul> <li>17. Potential at a point A is 3 volt and at a point B is 7 volt, an electron is moving towards A from B.</li> <li>(A) It must have some K.E. at B to reach A</li> <li>(B) It need not have any K.E. at B to reach A</li> <li>(C) to reach A it must have more than or equal to 4eV K.E. at B.</li> <li>(D) when it will reach A, it will have K.E. more then or at least equal to 4eV if it was released from rest at B.</li> <li>Sol.</li> </ul>

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Sol.	<b>22</b> Variation of electrostatic potential along x-direction is shown in the graph. The correct statement about electric field is (A) x component at point B is maximum (B) x component at point A is towards positive x-axis (C) x component at point C is along negative x-axis (D) x component at point C is along positive x-axis <b>Sol.</b>
<ul> <li>20. Let V be electric potential and E the magnitude of the electric field. At a given position, which of the statement is true ?</li> <li>(A) E is always zero where V is zero</li> <li>(B) V is always zero where E is zero</li> <li>(C) E can be zero where V is non zero</li> <li>(D) E is always nonzero where V is nonzero</li> <li>Sol.</li> </ul>	<b>23</b> An electric dipole moment $\vec{p} = (2.0\hat{i} + 3.0\hat{j})\mu C.m$ is placed in a uniform electric field $\vec{E} = (3.0\hat{i} + 2.0\hat{k}) \times 10^5 N C^{-1}$ . (A) The torque that $\vec{E}$ exerts on $\vec{p}$ is $(0.6\hat{i} - 0.4\hat{j} - 0.9\hat{k})Nm$ (B) The potential energy of the dipole is -0.6 J. (C) The potential energy of the dipole is 0.6 J (D) If the dipole is rotated in the electric field, the maximum potential energy of the dipole is 1.3 J. <b>Sol.</b>
<ul> <li>21. The electric potential decreases uniformly from V to -V along X-axis in a coordinate system as we moves from a point (-x<sub>0</sub>, 0) to (x<sub>0</sub>, 0), then the electric field at the origin.</li> <li>(A) must be equal to V/x<sub>0</sub> (B) may be equal to V/x<sub>0</sub> (C) must be greater than V/x<sub>0</sub> (D) may be less than V/x<sub>0</sub> Sol.</li> </ul>	

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Sol.

24. Three points charges are placed at the corners of 26. For the situation shown in the figure below (asan equilateral triangle of side L as shown in the figure. sume r >> lenth of dipole) mark out the correct statement(s). p (Small dipole) (A) The potential at the centroid of the triangle is zero. (B) The electric field at the centroid of the triangle is zero. (A) Force acting on the dipole is zero (C) The dipole moment of the system is  $\sqrt{2}$  gL (B) Force acting on the dipole is approximately  $\frac{pQ}{4\pi\epsilon_{r}r^{3}}$ (D) The dipole moment of the system is  $\sqrt{3}$  qL Sol. & is acting upward. (C) Torque acting on the dipole is  $\frac{pQ}{4\pi\epsilon_0 r^2}$  in clockwise direction (D) Torque acting on the dipole is  $\frac{pQ}{4\pi\epsilon_{n}r^{2}}$  in anticlockwise direction Sol. 25. Particle A having positive charge is moving directly head-on towards initially stationary positively charged particle B. At the instant when A and B are closest together. (A) the momenta of A and B must be equal (B) the velocities of A and B must be equal (C) B would have gained less kinetic energy than A would have lost. (D) B would have gained the same momentum as A would have lost.



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Exercise - III	(SUBJECTIVE PROBLEMS)
1. The distance between two fixed positive charges 4e and e is l. How should a third charge 'q' be arranged for it to be in equilibrium ? Under what condition will equilibrium of the charge 'q' be stable (for displacement on the line joining 4e and e) or will it be unstable ? Sol.	<ul> <li>4. Two particles A and B each carrying a charge Q are held fixed with a separation d between then A particle C having mass m and charge q is kept at the midpoint of line AB. If it is displaced through a small distance x (x&lt;<d) ab,<="" li="" perpendicular="" to=""> <li>(a) then find the time period of the oscillations of C for q &lt; 0.</li> <li>(b) If in the above question C is displaced along AB, find the time period of the oscillations of C for q &lt; 0.</li> </d)></li></ul>
<ul> <li>2. Two particles A and B, each having a charge Q are placed a distance d apart. Where should a particle of charge q be placed on the perpendicular bisector of AB so that it experiences maximum force ? What is the magnitude of the maximum force ?</li> <li>Sol.</li> </ul>	
<b>3.</b> A negative point charge 2q and a positive charge q are fixed at a distance <i>l</i> apart. Where should a positive test charge Q be placed on the line connecting the charge for it to be in equilibrium? What is the nature of the equilibrium with respect to longitudinal motions? <b>Sol.</b>	



ELECTROSTATICS - 1



**9.** A thin circular wire of radius r has a charge Q. If a point charge q is placed at the centre of the ring, then find the increase in tension in the wire. **Sol.** 

**10.** In the figure shown S is a large nonconducting sheet of uniform charge density  $\sigma$ . A rod R of length *l* and mass `m' is parallel to the sheet and hinged at its mid point. The linear charge densities on the upper and lower half of the rod are shown in the figure. Find the angular acceleration of the rod just after it is released.

 $\begin{bmatrix} \mathbf{s} & \mathbf{h} \\ \mathbf{a} & \mathbf{a} \end{bmatrix}_{\lambda}$ 

Sol.

**11.** In the following figures find the magnitude of electric field at a point 'P' on the axis of the square. The distance of 'P' from the centre is 'x'.



<b>12.</b> In the above question find electric field for t cases	wo Sol.
(a) x = 0 (b) x > > a Sol.	
	<ul> <li>14. A particle of mass m, charge q &gt; 0 and initial kinetic energy K is projected from infinity toward a heavy nucleus of charge Q assumed to have a fixed position.</li> <li>(a) If the aim is perfect, how close to the centre of the nucleus is the particle when it comes instantaneously to rest?</li> <li>Sol.</li> </ul>
	(b) With a particular imperfect aim the particle's closest approach to nucleus is twice the distance determined in (a) Determine speed of particle at the closest distance of approach. <b>Sol.</b>
<b>13.</b> A charge of 8 mC is located at the origin. Calcult the work done by external agent in taking a sm charge of $-2 \times 10^{-9}$ C from a point A (0, 0, 0.03 m) a point B(0, 0.04m, 0) via a point C(0, 0.06m, 0.09m) <b>394.50 - Bajeev Gandhi Nagar Kota, Ph. No.</b>	ate hall h to m). <b>: 93141-87482: 0744-2209671</b>
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**15.** Three point charges are arranged at the three vertices of a triangle as shown in figure. Given :  $q = 10^{-7}$ C. Calculate the electrostatic potential energy of the system.



Sol.

**16.** Eight equal point charges each of charge 'q' and mass 'm' are placed at eight corners of a cube of side 'a'.



(i) Find out potential energy of charge system

(ii) Find out work done by external agent against electrostatic forces and by electrostatic forces to increase all sides of cube from a to 2a

(iii) If all the charges are released at rest then find out their speed when they are at the corners of cube of side 2a.

(iv) If keeping all other charges fix, charge of corner 'A' is released then find out its speed when it is at infinite distance ?

(v) If all charges are released at rest then find out their speed when they are at a very large distance from each other.



# **17.** A simple pendulum of length *l* and bob mass m is 19. A point charge +q & mass 100 gm experiences a hanging in front of a large nonconducting sheet having force of 100 N at a point a distance 20 cm from a long surface charge density $\sigma$ . If suddenly a charge +q is infinite uniformly charged wire. If it is released find its given to the bob & it is released from the position speed when it is at a distance 40 cm from wire shown in figure. Find the maximum angle through which Sol. the string is deflected from vertical. <u>///////</u> 1 Sol. **18.** A charge +Q is uniformly distributed over a thin ring with radius R. A negative point charge -Q and mass m starts from rest at a point far away from the centre of the ring and moves towards the centre. Find the velocity of this particle at the moment it passes through the centre of the ring. Sol. 20. Consider the configuration of a system of four charges each of value +q. Find the work done by external agent in changing the configuration of the system from figure (i) to fig (ii). +q +a а +0 fig(i)

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Sol.	<b>21.</b> Two identical particles of mass m carry charge (each. Initially one is at rest on a smooth horizontal plane and the other is projected along the plane directly towards the first from a large distance with an initial speed V. Find the closest distance of approach. <b>Sol.</b>
	<b>22.</b> A particle of mass m and negative charge q is thrown in a gravity free space with speed u from the point A on the large non conducting charged shee with surface charge density $\sigma$ , as shown in figure Find the maximum distance from A on sheet where the particle can strike.
	Sol.
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23. Three charges 0.1 coulomb each are placed on the corners of an equilateral triangle of side 1 m. If the energy is supplied to this system at the rate of 1 kW, how much time would be required to move one of the charges onto the midpoint of the line joining the other two ? Sol. 26. A charge 'q' is carried from a point A (r, 135°) to point B(r, 45°) following a path which is a quadrant of circle of radius 'r'. If the dipole moment is  $\vec{p}$ . then find out the work done by external agent ? Sol. 24. Two identical nonconducting spherical shells having equal charge Q are placed at a distance d apart. When they are released find out kinetic energy of each sphere when they are at a large distance. **27.** Find out force experienced by short dipole  $\vec{P}_0$  is Sol. following different arrangements as shown in figures. [Assume point charge is Q,  $\vec{P}_0 = q_0(2a)$  and  $\vec{P} = q(2a)$ ]  $\xrightarrow{P_0 \qquad Q} \xrightarrow{r} \uparrow$ 

**25.** If  $\vec{E} = 2x^2\hat{i} - 3y^2\hat{j}$  then find v(x, y, z) **Sol.** 



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Sol.	<b>28.</b> Find out the magnitude of electric field intensity at point (2, 0, 0) due to a dipole of dipole moment, $\vec{P} = \hat{i} + \sqrt{3}\hat{j}$ kept at origin ? Also find out the potential at that point. <b>Sol.</b>
	<b>29.</b> A dipole is placed at origin of coordinate system as shown in figure, find the electric field at point P(0, y).
	Sol.
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## Exercise - IV

**Q.1** A rigid insulated wire frame in the form of a right angled triangle ABC, is set in a vertical plane as shown. Two bead of equal masses m each and carrying charges  $q_1 \& q_2$  are connected by a cord of length *I* & slide without friction on the wires. Considering the case when the beads are stationary, determine.



(a) The angle  $\alpha$ .

(b) The tension in the cord &

(c) The normal reaction on the beads. If the cord is now cut, what are the values of the charges for which the beads continue to remain stationary.

**Q.2** A clock face has negative charges -q, -2q, -3q, ..., -12q fixed at the position of the corresponding numerals on the dial. The clock hands do not disturb the net field due to point charges. At what time does the hour hand point in the same direction is electric field at the centre of the dial.

**Q.3** A circular ring of radius R with uniform positive charge density  $\lambda$  per unit length is fixed in the Y-Z plane with its centre at the origin O. A particle of mass m and positive charge q is projected from the

point P  $(\sqrt{3}R, 0, 0)$  on the positive X-axis directly

towards O, with initial velocity v. Find the smallest value of the speed v such that the particle does not return of P.

**Q.4** 2 small balls having the same mass & charge & located on the same vertical at heights  $h_1 \& h_2$  are thrown in the same direction along the horizontal at the same velocity v. The 1<sup>st</sup> ball touches the ground at a distance *l* from the initial vertical. At what height will the 2<sup>nd</sup> ball be at this instant? The air drag & the charges induced should be neglected.

### (TOUGH SUBJECTIVE PROBLEMS)

**Q.5** Two concentric rings of radii r and 2r are placed with centre at origin. Two charges +q each are fixed at the diametrically opposite points of the rings as shown in figure. Smaller ring is now rotated by an angle 90° about Z-axis then it is again rotated by 90° about Y-axis. Find the work done by electrostatic forces in each step. If finally larger ring is rotated by 90° about X-axis, find the total work required to perform all three steps.



**Q.6** Two identical balls of charges  $q_1 \& q_2$  initially have equal velocity of the same magnitude and direction. After a uniform electric field is applied for some time, the direction of the velocity of the first ball changes by 60° and the magnitude is reduced by half. The direction of the velocity of the second ball changes there by 90°. In what proportion will the velocity of the second ball changes ?

**Q.7** Small identical balls with equal charges are fixed at vertices of regular 2004 - gon with side a. At a certain instant, one of the balls is released & a sufficiently long time interval later, the ball adjacent to the first released ball is freed. The kinetic energies of the released balls are found to differ by K at a sufficiently long distance from the polygon. Determine the charge q of each part.

**Q.8**The electric field in a region is given by  $\vec{E} = \frac{E_0 x}{l} \vec{i}$ .

Find the charge contained inside a cubical volume bounded by the surfaces x = 0, x = a, y = 0, y = a, z = 0 and z = a. Take  $E_0 = 5 \times 10^3$  N/C, l = 2cm and a = 1 cm.

**Q.9** 2 small metallic balls of radii  $R_1 \& R_2$  are kept in vacuum at a large distance compared to the radii. Find the ratio between the charges on the 2 balls at which electrostatic energy of the system is minimum. What is the potential difference between the 2 balls ? Total charge of balls is constant.



**Q.10** A nonconducting ring of mass m and radius R is charged as shown. The charged density i.e. charge per unit length is  $\lambda$ . It is then placed on a rough nonconducting horizontal surface plane. At time t =

0, a uniform electric field  $\vec{E} = E_0 i$  is switched on and

the ring start rolling without sliding. Determine the friction force (magnitude and direction) acting on the ring, when it starts moving.



**Q.11** Two spherical bobs of same mass & radius having equal charges are suspended from the same point by strings of same length. The bobs are immersed in a liquid of relative permittivity  $\epsilon_r$  & density  $\rho_0$ . Find the density  $\sigma$  of the bob for which the angle of divergence of the strings to be the same in the air & in the liquid ?

**Q.12** Find the electric field at centre of semicircular ring shown in figure.





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(b) Three charges Q, +q and +q are placed at the verticles of a right-angled isosceles triangle as shown. The net electrostatic energy of the configuration is zero if Q is equal to

+q a +q

(A)  $\frac{-q}{1+\sqrt{2}}$  (B)  $\frac{-2q}{2+\sqrt{2}}$  (C) -2q Sol. **5.** Three positive charges of equal value q are placed at the vertices of an equilateral triangle. The resulting lines of force should be sketched as in



[IIT-2001]



(D) +q

(c) Four point charges + 8µC,  $-1\mu$ C,  $-1\mu$ C and + 8µC, are fixed at the points,  $-\sqrt{\frac{27}{2}}$  m,  $-\sqrt{\frac{3}{2}}$  m,  $+\sqrt{\frac{3}{2}}$  m and velo

 $+\sqrt{\frac{27}{2}}$  m respectively on the y-axis. A particle of mass

 $6 \times 10^{-4}$  kg and of charge +  $0.1\mu$ C moves along the -x direction. Its speed at x = +  $\infty$  is v<sub>0</sub>. Find the least value of v<sub>0</sub> for which the particle will cross the origin. Find also the kinetic energy of the particle at the origin. Assume that space is gratity free. (Given :  $1/(4\pi\epsilon_0) = 9 \times 10^9$  Nm<sup>2</sup>/C<sup>2</sup>) [IIT-2000,10]

Sol.

**6.** A small ball of mass  $2 \times 10^{-3}$  Kg having a charge of  $1\mu$ C is suspended by a string length 0.8m. Another identical ball having the same charge is kept at the point of suspension. Determine the minimum horizontal velocity which should be imparted to the lower ball so that it can make complete revolution.

Sol.



#### ELECTROSTATICS - 1

7. Two equal point charges are fixed at x = -a and x = +a on the x-axis. Another point charge Q is placed at the origin. The change in the electrical potential energy of Q, when it is displaced by a small distance x along the x-axis, is approximately proportional to [JEE 2002 (Scr).]

(A) x (B)  $x^2$  (C)  $x^3$  (D) 1/xSol.

**8.** Charges +q and -q are located at the corners of a cube of side a as shown in the figure. Find the work done to separate the charges to infinite distance. **[JEE-2003]** 



Sol.

**9.** A charge +Q is fixed at the origin of the co-ordinate system while a small electric dipole of dipole-moment

 $\vec{p}\,$  pointing away from the charge along the x-axis is set free from a point far away from the origin.

(a) calculate the K.E. of the dipole when it reaches to a point (d, 0) [JEE 2003]
(b) calculate the force on the charge +Q at this moment.

Sol.

**10.** Six charges, three positive and three negative of equal magnitude are to be placed at the vertices of a regular hexagon such that the electric field at O is double the electric field when only one positive charge of same magnitude is placed at R. Which of the following arrangements of charges is possible for P, Q, R, S, T and U respectively ? **[JEE 2004 (SCR)]** 

(A) +, -, +, -, -, + (B) +, -, +, -, +, -(C) +, +, -, +, -, - (D) -, +, +, -, +, -**Sol.** 

**11.** Two uniformly charged infinitely large planar sheet  $S_1$  and  $S_2$  are held in air parallel to each other with separation d between them. The sheets have charge distribution per unit area  $\sigma_1$  and  $\sigma_2$  (Cm<sup>-2</sup>), respectively, with  $\sigma_1 > \sigma_2$ . Find the work done by the electric field on a point charge Q that moves from  $S_1$  towards  $S_2$  along a line of length a (a < d) making an angle  $\pi/4$  with the normal to the sheets. Assume that the charge Q does not affect the charge distributions of the sheets. **[JEE 2004]** 

Sol.



Page # 88 **ELECTROSTATICS - 1** 12. Which of the following groups do not have same (A) The electric field at point O is  $\frac{q}{8\pi\epsilon_0R^2}$  directed dimensions -(A) Young's modulus, pressure stress along the negative x-axis (B) work, heat, energy (B) The potential energy of the system is zero (C) electromotive force, potential difference, voltage (C) The magnitude of the force between the charges (D) electric dipole, electric flux, electric field at C and B is  $\frac{q^2}{54\pi\epsilon_0 R^2}$ Sol. (D) the potential at point O is  $\frac{q}{12\pi\epsilon_0 R}$ Sol. 13. Positive and negative point charges of equal magnitude are kept at  $\left(0,0,\frac{a}{2}\right)$  and  $\left(0,0,-\frac{a}{2}\right)$ , respectively. The work done by the electric field when another positive point charge is moved from (-a, 0, 0)15. A few electric field lines for a system of two charges to (0, a, 0) is - $\boldsymbol{Q}_{_1}$  and  $\boldsymbol{Q}_{_2}$  fixed at two different points on the x - axis (A) positive (B) negative (C) zero are shown in the figure. These lines suggest that (D) depends on the path connecting the initial and final positions [JEE 2007] Sol. (A)  $|Q_1| > |Q_2|$ (B)  $|Q_1| < |Q_2|$ (C) at a finite distance to the left of  $Q_1$  the electric field is zero. (D) at a finite distance to the right of Q<sub>2</sub> the electric field is zero. [JEE 2010] Sol. **14.** Consider a system of three charges  $\frac{q}{3}, \frac{q}{3}$  and  $-\frac{2q}{3}$ placed at points A, B and C, respectively, as shown in the figure. Take O to be the centre of the circle of radius R and angle CAB = 60° [JEE 2008] Figure : 394,50 - Rajeev Gandhi Nagar Kota, Ph. No. : 93141-87482, 0744-2209671 **ON** IVRS No: 0744-2439051, 52, 53, www. motioniitjee.com , hr@motioniitjee.com

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<ul> <li>16. Under the influence of the Coulomb field of charge +Q, a charge -q is moving around it in an elliptical orbit. Find out the correct statement(s)</li> <li>(A) The angular momentum of the charge -q is constant</li> <li>(B) The linear momentum of the charge -q is constant</li> <li>(C) The angular velocity of the charge -q is constant</li> <li>(D) The linear speed of the charge -q is constant</li> <li>[JEE 2010]</li> <li>Sol.</li> </ul>	<b>18.</b> Four point charges, each of +q are rigidly fixed at the four corners of a square planar soap film of side 'a'. The surface tension of the soap film is $\gamma$ . the system of charges and planar film are in equilibrium, and $a = k \left[ \frac{q^2}{\gamma} \right]^{1/N}$ , where 'k' is a constant. Then N is <b>[JEE 2011]</b> <b>Sol.</b>
<b>17.</b> A tiny spherical oil drop carrying a net charge q is balanced in still air with a vertical uniform electric field of strength $\frac{81\pi}{7} \times 10^5 \text{ Vm}^{-1}$ . When the field is switched off, the drop is observed to fall with terminal velocity $2 \times 10^{-3} \text{ ms}^{-1}$ Given $g = 9.8 \text{ ms}^{-2}$ , viscosity of the air = $1.8 \times 10^{-5} \text{ Ns} \text{ m}^{-2}$ and the density of oil = 900 kg m <sup>-5</sup> , the magnitude of q is : (A) $1.6 \times 10^{-19}$ C (B) $3.2 \times 10^{-19}$ C (C) $4.8 \times 10^{-19}$ C (D) $8.0 \times 10^{-19}$ C [JEE 2010] Sol.	<ul> <li>19. A wooden block performs SHM on a frictionless surface with frequency, v<sub>0</sub>. The block carries a charge +Q on its surface. If now a uniform electric field Ē is switched-on as shown, then the SHM of the block will be</li> <li> Image: A constraint of the sum of the block will be (A) of the same frequency and with shifted mean position (B) of the same frequency and with the same mean position (C) of changed frequency and with shifted mean position (D) of changed frequency and with the same mean position (D) of changed fre</li></ul>
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