# **CBSE Guess.com**

# PART A - CHEMISTRY

- Identify the incorrect statement from the following:
  - Ozone absorbs the intense ultraviolet radiation of the sun.
  - (2) Depletion of ozone layer is because of its chemical reactions with chlorofluoro alkanes.
  - (3) Ozone absorbs infrared radiation.
  - (4) Oxides of nitrogen in the atmosphere can cause the depletion of ozone layer.
- **Sol.** [3]

Ozone absorbs UV rays from sun and not infrared radiation.

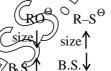
- When r, P and M represent rate of diffusion, pressure and molecular mass, respectively, then the ratio of the rates of diffusion (r<sub>A</sub>/r<sub>B</sub>) of two gases A and B, is given as:
  - (1)  $(P_A/P_B) (M_B/M_A)^{1/2}$
  - (2)  $(P_A/P_B)^{1/2} (M_B/M_A)$
  - (3)  $(P_A/P_B) (M_A/M_B)^{1/2}$
  - (4)  $(P_A/P_B)^{1/2} (M_A/M_B)$
- Sol. [1]

$$r \propto \frac{p}{\sqrt{d}} \propto \frac{p}{\sqrt{M}}$$

$$\frac{r_{A}}{r_{B}} = \frac{P_{A}}{P_{B}} \left( \frac{M_{B}}{M_{A}} \right)$$

- 3. Consider thiol anion (RS<sup>®</sup>) and allow anion (RO<sup>®</sup>). Which of the relowing statements is **correct**?
  - (1) RS is less basic but (tore nucleophilic than RO)
  - (2) RS is more asily and more nucleophilic han RO
  - (3) RS<sup>2</sup> is more basic but less nucleophilic
  - (4) RS sees basic and less nucleophilic

Sol.



The change in the optical rotation of freshly prepared solution of glucose is known as:

- (1) racemisation
- (2) specific rotation
- (3) mutarotation
- (4) tautomerism
- Sol. [3] Fact
- 5. The molality of a urea solution in which 0.0100 g of urea, [(NH<sub>2</sub>)<sub>2</sub>CO] is added to  $0.3000 \text{ dm}^3$  of water at STP is :
  - (1)  $5.55 \times 10^{-4} m$
  - (2) 33.3 m
  - (3)  $3.33 \times 10^{-2} m$
  - (4) 0.555 m

$$m = \frac{0.01}{60 \times 0.30} = \frac{1}{60 \times 30} = 5.55 \times 10^{-4}$$
  
$$d_{water} = 1 \text{ kg/dm}^3$$

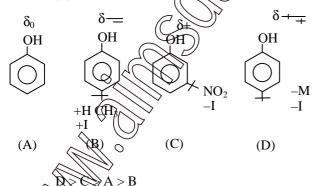
- 6. The molecular velocity of any gas is:
  - (1) inversely proportional to absolute temperature
  - (2) directly proportional to square of temperature
  - (3) directly proportional to square root of temperature
  - (4) inversely proportional to the square root of temperature

# Sol. [3]

$$V_{mp}, V_{rms}, V_{av.} \propto \sqrt{T}$$

- 7. The correct order of acid strength of the following compounds:
  - A. Phenol
  - B. p-Cresol
  - C. m-Nitrophenol
  - D. p-Nitrophenol
  - is:
  - (1)  $\mathbb{D} > \mathbb{C} > \mathbb{A} > \mathbb{B}$
  - (2) B > D > A > C
  - (3) A > B > D > C
  - $(4) \quad C > B > A > D$

### Sol. [1]



8. The value of enthalpy change (ΔH) for the reaction

$$C_2H_5OH_{(1)} + 3O_{2(g)} \rightarrow 2CO_{2(g)}$$

at 27°C is -1366.5 kJ mol<sup>-1</sup>. The whole of internal energy change to the above reaction at this temperature will be:

- (1) -1369.0 kJ
- (2) -1364.0
- (3) -136(.51)
- (4) (B) (3)

### Sol.

[2]

$$\Delta \mathbf{H} = \Delta \mathbf{E} \, \mathbf{\hat{\Delta}} \, \mathbf{n_g} \mathbf{R} \mathbf{T}$$

$$\Delta E = \Delta H - \Delta n_g RT$$
  
= -1366.5 - (-1) (8.3 × 10<sup>-3</sup>) × 300

$$=-1366.5+2.490$$

$$=-1364.01$$

Thermosetting polymer, Bakelite is formed by the reaction of phenol with:

- (1) CH<sub>3</sub>CHO
- (2) HCHO
- (3) HCOOH
- (4) CH<sub>3</sub>CH<sub>2</sub>CHO

## Sol. [2]

$$+ \underline{\text{H-CH=O}} \longrightarrow \text{Bakelite}$$

- 10. Ozonolysis of an organic compound 'A' produces acetone and propionaldehyde in equimolar mixture. Identify 'A' from the following compounds:
  - 1 Pentene (1)
  - 2 Pentene (2)
  - 2 Methyl 2 pentene
  - (4) 2 Methyl 1 pentene

Sol. [3]  

$$CH_3 - C - CH_3$$
  $CH_3 - CH_2 - CH = O$   
 $CH_3$   
 $CH_3 - C = CH - CH_2 - CH_3$   
 $CH_3 - C = CH - CH_2 - CH_3$ 

11. Consider the reaction:

$$\begin{split} 4NO_{2(g)} + O_{2(g)} &\rightarrow 2N_2O_{5(g)}, \ \Delta_r H = -111\,kJ. \end{split}$$
 If  $N_2O_{5(s)}$  is formed instead of  $N_2O_{5(g)}$  in

the above reaction, the  $\Delta_r$ H value will be  $\zeta$ (given,  $\Delta H$  of sublimation for N<sub>2</sub>O<sub>3</sub>

54 kJ mol-1)

- (1)+54 kI
- +219 kJ(2)
- -219 kJ
- -165 kJ

Sol.

[3] 
$$4NO_2 + O_2 \rightarrow 2N_2O_3 \longrightarrow H = -111 \dots (1)$$

$$4NO_2 + O_2 + O_3 \rightarrow \Delta H = ?$$
 ...(2)

$$2N_2O_5 \Leftrightarrow 2N_2O_5 \qquad \Delta H = 54 \times 2 \qquad ...(3)$$

$$k = -111 - 108 = -219 \text{ kJ}$$

12. An acid HA ionises as

$$HA \rightleftharpoons H^+ + A^-$$

The pH of 1.0 M solution dissociation constant would be

- (1)
- $5 \times 10^{-8}$ (2)
- $1 \times 10^{-5}$

Sol.



- The correct order of electron gain enthalpy with negative sign of F, Cl, Br and I, having atomic number 9, 17, 35 and 53 respectively, is:
  - F > Ci > Br > I
  - Cl > F > Br > I
  - Br > Cl > I > F
  - I > Br > Cl > F

Sol. [2]

Order of electron gain enthalpy.

- 14. The frequency of light emitted for the transition n=4 to n=2 of  $He^+$  is equal to the transition in H atom corresponding to which of the following?
  - (1) n=2 to n=1
  - (2) n=3 to n=2
  - (3) n=4 to n=3
  - (4) n=3 to n=1
- Sol. [1]

$$\overline{\nu}_{H} = \overline{\nu}_{He^{+}}$$

$$\left[ RZ^{2} \left( \frac{1}{n_{1}^{2}} - \frac{1}{n_{2}^{2}} \right) \right]_{H} = \left[ RZ^{2} \left( \frac{1}{n_{1}^{2}} - \frac{1}{n_{2}^{2}} \right) \right]_{He^{4}}$$

$$\frac{1}{n_1^2} - \frac{1}{n_2^2} = \left[ 4 \left( \frac{1}{4} - \frac{1}{16} \right) \right]$$

$$\frac{1}{n_1^2} - \frac{1}{n_2^2} = \frac{1}{1} - \frac{1}{4}$$

$$n_1 = 1$$

$$n_2 = 2$$

- 15. A 5% solution of cane sugar (molar mass 342) is isotonic with 1% of a solution of an unknown solute. The molar mass of unknown solute in g/mol is:
  - (1) 171.2
  - (2) 68.4
  - (3) 34.2
  - (4) 136.2
- Sol.

$$\pi_1 = \pi_2 \ \bigcirc$$

$$c_1 = c_2$$

$$\frac{5}{342} = \frac{1}{M}$$

16. In view of the signs of  $\Delta_r G^\circ$  for following reactions:

$$PbO_2 + Pb \rightarrow 2 PbO, \Delta_rG^{\circ} < 0$$

$$SnO_2 + Sn \rightarrow 2 SnO, \Delta_r G^{\circ} > 0,$$

which oxidation states are more characteristic for lead and the?

- (1) For lead + Gornin 2
- (2) For lead 4, for tin +4
- (3) For least +2, for tin +4
- (4) For least +4, for tin +2
- Sol.

spontaneous reaction

$$Pb^{+4} \rightarrow Pb^{+2}$$

$$Pb^{+2} > Pb^{+4}$$
 (stability)

 $\Delta G^{\circ} > 0$  non-spontaneous reaction

$$\operatorname{Sn}^{+4} \to \operatorname{Sn}^{+2}$$

$$\operatorname{Sn}^{+4} > \operatorname{Sn}^{+2} \text{ (stability)}$$

$$Pb^{+2}$$
,  $Sn^{+4}$ 

17. The  $K_{sp}$  for  $Cr(OH)_3$  is  $1.6 \times 10^{-30}$ . The molar solubility of this compound in water is:

(i) 
$$\sqrt[4]{1.6 \times 10^{-20}}$$

(2) 
$$\sqrt[4]{1.6 \times 10^{-30}/27}$$

(3) 
$$1.6 \times 10^{-30} / 27$$

(4) 
$$\sqrt[2]{1.6 \times 10^{-30}}$$

Sol. [2]

$$K_{sp} = s(3s)^3 = 27s^4 = 1.6 \times 10^{-30}$$

$$s = \sqrt[4]{\frac{1.6 \times 10^{-30}}{27}}$$

18. The products obtained on heating LiNO<sub>3</sub> will be:

(1) 
$$\text{Li}_2\text{O} + \text{NO}_2 + \text{O}_2$$

(2) 
$$Li_3N + O_2$$

(3) 
$$\text{Li}_2\text{O} + \text{NO} + \text{O}_2$$

(4) 
$$LiNO_2 + O_2$$

Sol. [1] 
$$LiNO_3 \xrightarrow{\Delta} Li_2O + NO_2 + O_2$$

19. Resistance of 0.2 M solution of an electrolyte is 50  $\Omega$ . The specific conductance of the solution is 1.3 S m<sup>-1</sup>. If resistance of the 0.4 M solution of the same electrolyte is 260  $\Omega$ , its molar conductivity is :

(1) 
$$6.25 \times 10^{-4} \text{ S m}^2 \text{ mol}^{-1}$$

(2) 
$$625 \times 10^{-4} \text{ S m}^2 \text{ mol}^{-1}$$

(3) 
$$62.5 \text{ S m}^2 \text{ mol}^{-1}$$

(4) 
$$6250 \text{ S m}^2 \text{ mol}^{-1}$$

$$\lambda_{m} = \kappa \times \frac{1000}{M} (\kappa = 1.3 \text{ S m}^{-1} = 1.3 \text{ M}^{-1} \text{ S cm}^{-1}$$

$$= \frac{1}{\kappa} \times \frac{\ell}{a} \times \frac{1000}{M}$$

$$\kappa = \frac{1}{R} \times \frac{\ell}{a}$$

$$\frac{\ell}{a} = \kappa R = 1.3 \times 10^{2} \times 50 = 65.0 \times 10^{-2} \text{ cm}^{-1}$$

$$\lambda_{m} = \frac{1}{260} \times 65 \times 10^{-2} \times \frac{1000}{0.4}$$

$$= 6.25 \text{ kmp}^{-1} \times \text{cm}^{2}$$

$$= 6.25 \times 10^{-4} \text{ m}^{2} \text{ S mol}^{-1}$$

20. Among the ligands NH<sub>3</sub>, en, CN<sup>-</sup> and CO the correct order of their increasing field strength, is:

(1) 
$$NH_3 < en < CN^- < CO$$

According to spectrochemical series increasing order of strength of ligands is NH<sub>3</sub> < en CO

$$G_2H_5OD$$
 +  $H_2SO_4$  → Product  
Among the following, which of

Among the following, which one cannot be formed as a product under any conditions?

- (1) Ethylene
- (2) Acetylene
- (3) Diethyl ether
- (4) Ethyl-hydrogen sulphate

### **Sol.** [2]

$$C_2H_5OH \xrightarrow{H_2SO_4} C_2H_5-O-SO_3H$$

$$\xrightarrow{140^{\circ}C} C_2H_5-O-C_2H_5$$

$$\xrightarrow{170^{\circ}C} CH_2=CH_2$$

- 22. The non aromatic compound among the following is:
  - (1)
  - (2)
  - (3)
  - (4)
- Sol. [4]



There is no continuous resonance thus it is non-aromatic.

- 23. The number of types of bonds between two carbon atoms in calcium carbide is:
  - (1) One sigma, one pi
  - (2) Two sigma, one pi
  - (3) Two sigma, two pi
  - (4) One sigma, two pi
- Sol. [4]

Calcium carbide is a ionic carbide

$$\Rightarrow$$
  $Ca^{2+} [C \equiv C]^{2-}$ 

It contains  $1\sigma$  and  $2\pi$  bend

24. A reactant (A) forms two products

 $A \xrightarrow{k_1} B$ , Activation Energy Ea

 $A \xrightarrow{k_2} C$ , Activation Energy

If  $Ea_2 = 2 Ea_1$ , then  $k_1$  and  $k_2$  are related as:

- (1)  $k_2 = k_1 e^{Ea_1/RT}$
- (2)  $k_2 = k_1 e^{Ea_2/RT}$
- $(3) \quad k_1 = Ak_2 e^{Ea}$
- (4)  $k_1 = 2k_2e^{E_{12}}$
- Sol. [3]

$$k_1 = A_1 e^{RT}$$

 $A_2 = A_2 e$   $A_2 = A_2 e$   $A_2 = A_2 e$   $A_3 = A_2 e$   $A_4 = A_2 e$   $A_4 = A_2 e$   $A_4 = A_2 e$   $A_5 = A_2 e$   $A_7 = A_2 e$   $A_8 = A_1 e$   $A_1 = A_1 e$   $A_2 = A_1 e$   $A_1 = A_1 e$   $A_2 = A_1 e$   $A_1 = A_1 e$   $A_1 = A_1 e$   $A_2 = A_1 e$   $A_1 = A_1 e$   $A_2 = A_1 e$   $A_1 = A_1 e$   $A_1 = A_1 e$   $A_1 = A_1 e$ 

$$\sum_{i=1}^{K} \frac{Ea_1 - Ea_2}{RT}$$

 $(Ea_2 = 2Ea_1)$ 

$$\frac{\mathbf{k}_2}{\mathbf{k}_1} = \mathbf{A}\mathbf{e}^{-\frac{\mathbf{E}\mathbf{a}_1}{\mathbf{R}\mathbf{T}}}$$

$$k_2 = A k_1 \ e^{-\frac{E a_1}{RT}}$$

$$k_1 = A k_2 \ e^{+\frac{E a_1}{RT}}$$

- 25. Copper crystallises in fcc lattice with a unit cell edge of 361 pm. The radius of copper atom is:
  - (1) 108 pm
  - (2) 128 pm
  - (3) 157 pm
  - (4) 181 pm
- Sol. [2]

$$4r=\sqrt{2}a$$

$$r = \frac{\sqrt{2}}{4} \times 361$$

 $= 127.61 \simeq 128 \text{ pm}$ 

- 26. The mass of potassium dichromate crystals required to oxidise 750 cm<sup>3</sup> of 0.6 M Mohr's salt solution is: (Given molar mass: potassium dichromate = 294, Mohr's salt = 392)
  - (1) 0.45 g
  - (2) 22.05 g
  - (3) 2.2 g
  - (4) 0.49 g
- Sol. [2]

$$gm eqv. = gm. Eqv.$$

of

of

Mohr's K<sub>2</sub>Cr<sub>2</sub>O<sub>7</sub>

salt

$$\frac{NV(ml)}{1000} = \frac{gm}{E.w}$$

$$\frac{(0.6 \times 1 \times 750)}{1000} = \frac{x}{294}$$

$$x = \frac{0.6 \times 750}{1000} \times \frac{294}{6} = \frac{75 \times 294}{1000}$$
$$= 22.05 \text{ gm}$$

- 27. What is the best description of the change that occurs when Na<sub>2</sub>O(s) is dissolved in water?
  - (1) Oxide ion accepts sharing in a pair of electrons
  - (2) Oxide ion donates a pair of electrons
  - (3) Oxidation number of oxygen increases
  - (4) Oxidation number of sodium decreases

Sol. [1]

 $Na_2O + H_2O \rightarrow 2NaOH$ 

- 28. Which of the following has maximum number of lone pairs associated with Xe?
  - (1) XeF<sub>4</sub>
  - (2) XeF<sub>6</sub>
  - (3) XeF<sub>2</sub>
  - (4) XeO<sub>3</sub>
- Sol. [3]

XeF<sub>2</sub> has maximum number of lone pairs (3 lone pairs)

29. In the chemical reactions



compounds A and B respectively are :

(1) Berteene diazonium chloride and

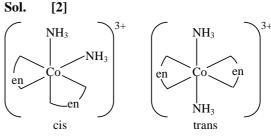
Nitrobenzene and chlorobenzene Phenol and bromobenzene

- ) Fluorobenzene and phenol
- $\begin{array}{c|c}
  \hline
  \text{NH}_2 & \text{N=N-Cl} & \text{CN} \\
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- 30. Which one of the following complex ions has geometrical isomers?

reaction

- (1) [Ni (NH<sub>3</sub>)<sub>5</sub> Br]<sup>+</sup>
- (2) [ Co (NH<sub>3</sub>)<sub>2</sub> (en)<sub>2</sub> ]<sup>3+</sup>
- (3) [ Cr (NH<sub>3</sub>)<sub>4</sub> (en) ]<sup>3+</sup>
- (4) [Co (en)<sub>3</sub>]<sup>3+</sup>
- (en = ethylenediamine)

  Sol. [2]



It has geometrical isomers.

# PART B - PHYSICS

- 31. At time t = 0s a particle starts moving along the x-axis. If its kinetic energy increases uniformly with time 't', the net force acting on it must be proportional to:
  - (1) constant
  - (2) t
  - (3)  $\frac{1}{\sqrt{t}}$
  - (4)  $\sqrt{t}$

**Ans.**[3]

Sol. K.E. 
$$\propto$$
 t i.e.,  $\frac{1}{2}mv^2 \propto t$   
 $v \propto \sqrt{t}$   
 $a = \frac{dv}{dt} \propto \frac{1}{2\sqrt{t}}$ ,  $F = ma$   
 $F \propto \frac{1}{\sqrt{t}}$ 

32. At two points P and Q on a screen in Young's double slit experiment, waves from slits S<sub>1</sub> and S<sub>2</sub> have a path difference

of 0 and  $\frac{\lambda}{4}$  respectively. The ratio of intensities at P and Q will be:

- (1) 2:1
- (2)  $\sqrt{2}$ :
- (3) 4:1

Ans.[1]

Sol. 
$$I = 4I_0 \cos^2 \phi / 2$$
  
 $I_P = 4I_0 \cos^2 0 = 4I_0$   
 $I_Q = 4I_0 \cos^2 \left(\frac{\pi}{4}\right) = \frac{4I_0}{2} = 2I_0$  (2)  
 $\frac{I_P}{I_Q} = 2$ 

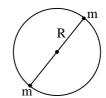
33. Two particles of equal mass in go around a circle of radius R under the action of their mutual gravitational attraction. The speed of each particle of respect to their centre of mass is:



- (3)  $\sqrt{\frac{Gm}{2R}}$
- (4)  $\sqrt{\frac{Gm}{R}}$

Ans.[1]

Sol. 
$$\frac{Gm^2}{(2R)^2} = \frac{mv^2}{R}$$
$$v = \sqrt{\frac{GM}{4R}}$$



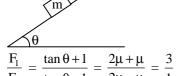
- 34. The minimum force required to start pushing a body up a rough (frictional coefficient  $\mu$  ) inclined plane is  $F_1$  while the minimum force needed to prevent it from sliding down is F2. If the inclined plane makes an angle  $\theta$  from the horizontal such that  $\tan \theta = 2\mu$  then the ratio  $F_1$  is:
  - (1)1
  - (2)2
  - (3)3
  - (4)

Ans.[3]

 $F_1 = mg \sin\theta + \mu mg \cos\theta$ ...(i)

...(ii)

 $F_2 = mgsin\theta - \mu mgcos\theta$ 



- If 400  $\Omega$  of resistance is made by adding 35. four 100 Ω resistances of tolerance 5%, then the tolerance of the combination is
  - 5% (1)
  - (2)10%
  - (3)15%
  - (4)20%

Ans.[1]

 $R_4 = 400 \Omega$ 

$$\frac{\Delta R}{R} = \frac{100}{400} \times 100$$

$$= \frac{100}{100} \times 100 = 5\%$$

36. An electric charge + q moves with vel  $\vec{V} = 3\hat{i} + 4\hat{j} + \hat{k}$ , in an electromag field given by:

 $\vec{E} = 3\hat{i} + \hat{j} + 2\hat{k}$  and

 $\vec{B} = \hat{i} + \hat{j} - 3\hat{k}$ . The x-component of the force experienced by

- (1) 11 q
- (2)
- (3)

**Ans.[1]** 

Magnetic force  $\vec{F} = q(\vec{V} \times \vec{B}) = 10q \hat{j}$ Sol.

and electric force in direction of y-axis  $\vec{F} = q \hat{j}$ 

 $E_{\text{Net}} = 11q$  in direction of y-axis.

The current in the primary circuit of a potentiometer is 0.2 A. The specific resistance and cross-section of the potentiometer wire are  $4 \times 10^{-7}$  ohm metre and  $8 \times 10^{-7}$  m<sup>2</sup> respectively. The potential gradient will be equal to:

- 1 V/m (1)
- (2)0.5 V/m
- 0.1 V/m
- (4)0.2 V/m

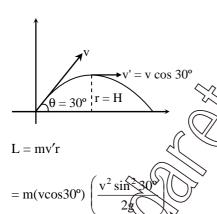
**Ans.**[3]

**Sol.** 
$$\phi = \frac{V_{AB}}{L} = \frac{i \times \rho}{A} = 0.1 \text{ volt/meter}$$

- 38. A particle of mass 'm' is projected with a velocity v making an angle of 30° with the horizontal. The magnitude of angular momentum of the projectile about the point of projection when the particle is at its maximum height 'h' is:
  - (1) zero
  - $(2) \quad \frac{\text{m } v^3}{\sqrt{2} \text{ g}}$
  - $(3) \quad \frac{\sqrt{3}}{16} \ \frac{\mathrm{m} \, v^3}{\mathrm{g}}$
  - $(4) \qquad \frac{\sqrt{3}}{2} \quad \frac{m \, v^2}{g}$

Ans.[3]

Sol.



$$= \frac{\text{mv}^3}{2\text{g}} \frac{\sqrt{3}}{2}$$

$$=\frac{\sqrt{3}m\sqrt{3}}{16}$$

39. The specific heat capacity of a metal at temperature (T) is given as:

$$C_p(kJK^{-1}kg^{-1}) = 32 \left(\frac{3}{400}\right)^3$$

A 100 gram vessel of this metal is to be cooled from 20°K to the a special refrigerator operating at room temperature (27°C). The amount of work required to coop the vessel is:

- (1) greater than 0.140 k
- (2) Six (west) .148 kJ and 0.028 kJ
  - 3) less than 0.028 kJ
- (4) equal to 0.002 kJ

 $\Delta Q = mC_p dT$ 

$$= (100 \times 10^{-3}) \times \left[ 32 \times \int_{20}^{4} \left( \frac{T}{400} \right)^{3} . dT \right]$$

= 0.002 KJ

$$\beta = \frac{T_2}{T_1 - T_2} = \frac{Q_2}{W}$$
;  $T_2 = 300 \text{ K}, Q_2 = 0.002 \text{ KJ}$ 

If 
$$T_1 = 20 \text{ K}$$
,  $W = 0.148 \text{ KJ}$ 

$$T_2 = 4 \text{ K}, W = 0.028 \text{ KJ}$$

i.e., amount of work will be between 0.148 KJ to 0.028 KJ.

40. A wooden cube (density of wood 'd') of side 'l' floats in a liquid of density 'ρ' with its upper and lower surfaces horizontal. If the cube is pushed slightly down and released, it performs simple harmonic motion of period 'T'. Then, 'T' is equal to:

(1) 
$$2\pi \sqrt{\frac{ld}{\rho g}}$$

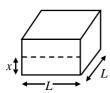
(2) 
$$2\pi \sqrt{\frac{l\rho}{dg}}$$

(3) 
$$2\pi \sqrt{\frac{Id}{(\rho - d)g}}$$

$$(4) 2\pi \sqrt{\frac{l\rho}{(\rho-d)g}}$$

Ans.[1]

Sol.



Restoring force  $F_R = (L^2 x) \rho g$ 

In case of SHM  $F_R = m\omega^2 x$ 

From equation (1) & (2)

$$m\omega^2 x = L^2 x \rho g$$

$$(d)L^3\omega^2 = L^2\rho g$$

$$dL\omega^2 = \rho g$$

$$\omega = \sqrt{\frac{\rho g}{dk}}$$

$$T = 2\pi \sqrt{\frac{dL}{\rho g}}$$

41. A container with insulating walls is divided into two equal parts by a partition fitted with a valve. One part is filled with an ideal gas at a pressure P and temperature T, whereas the other part is completely evacuated. If the valve is suddenly opened, the pressure and temperature of the gas will be:

(1) 
$$\frac{P}{2}$$
,  $\frac{T}{2}$ 

Ans.[4

Sol It is free expansion of Ideal gas which is both adiabatic and isothermal process.

 $T \rightarrow constant$ , so for the isothermal process

$$P_1V_1 = (P_2V_2)$$

$$P_1V_1 = P_2(2V_1)$$

$$P_2 = \frac{P_1}{2}$$

- 42. In a Young's double slit experiment, the two slits act as coherent sources of waves of equal amplitude A and wavelength  $\lambda$ . In another experiment with the same arrangement the two slits are made to act as incoherent sources of waves of same amplitude and wavelength. If the intensity at the middle point of the screen in the first case is  $I_1$  and in the second case is  $I_2$ , then the ratio  $I_1/I_2$  is:
  - (1) 2
  - (2) 1
  - (3) 0.5
  - (4) 4

Ans.[1]

Sol.  $I_1 = 4I_0\cos^2\phi/2 = 4I_0$  .... (1)  $I_2 = I_0 + I_0 = 2I_0$  .... (2) (for non coherent sources)  $I_1$  2

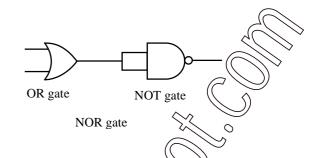
both the inputs of a NAND gat

combination will serve as a:

- $I_2$  1
  43. The output of an OR gate is connected
  - (1) NOT gate
  - (2) NOR gate
  - (3) AND ga
  - (4) OR gate

Ans.[2]

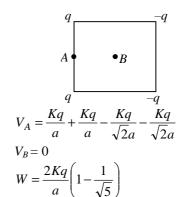
Sol.



- 44. Two positive charges of magnitude 'q' are placed at the ends of a side (side 1) of a square of side '2a. Fwo negative charges of the same magnitude are kept at the other corners. Tearthing from rest, if a charge Quoves from the middle of side 1 to the tentre of square, its kinetic energy at the centre of square is:
  - $\frac{1}{4\pi\epsilon_0} \cdot \frac{2qQ}{a} \left(1 + \frac{1}{\sqrt{5}}\right)$
  - (3)  $\frac{1}{4\pi\epsilon_0} \frac{2qQ}{a} \left(1 \frac{2}{\sqrt{5}}\right)$
  - $(4) \quad \frac{1}{4\pi\varepsilon_0} \, \frac{2qQ}{a} \left(1 \frac{1}{\sqrt{5}}\right)$

Ans.[4]

**Sol.**  $W = q(\Delta V) = \Delta KE$ 



- 45. Combination of two identical capacitors, a resistor R and a dc voltage source of voltage 6V is used in an experiment on a (C-R) circuit. It is found that for a parallel combination of the capacitor the time in which the voltage of the fully charged combination reduces to half its original voltage is 10 second. For series combination the time needed for reducing the voltage of the fully charged series combination by half is:
  - (1) 10 second
  - (2) 5 second
  - (3) 2.5 second
  - (4) 20 second

Ans.[3]

$$\frac{0.693 \times R \times 2C = 10}{0.693 \times R \times \frac{C}{2} = T}$$

$$\Rightarrow \frac{2/1}{1/2} = \frac{10}{T}$$

$$\Rightarrow \frac{4}{10} = \frac{10}{T}$$

$$T = 2.5 \text{ sec}$$

46. A beaker contains water up to a height h<sub>1</sub> and kerosene of height h<sub>2</sub> above water so that the total height of (water + kerosene) is (h<sub>1</sub> + h<sub>2</sub>). Refractive index of water is μ<sub>1</sub> and that of kerosene is μ. The parent shift in the position of the bottom of the beaker when viewed from above is:

(1) 
$$\left(1 + \frac{1}{\mu_1}\right)h_2$$

(2) 
$$\left(1 - \frac{1}{\mu_2}\right) h_2$$

$$3 \left( \frac{1}{\mu_1} \right) h_2 - \left( 1 + \frac{1}{\mu_2} \right) h_1$$

$$\left(1-\frac{1}{\mu_1}\right)h_2+\left(1-\frac{1}{\mu_2}\right)h_1$$

**Ans.**[2]

**Sol.** Actual depth = 
$$(h_1 + h_2)$$

Apparent depth = 
$$\frac{h_1}{\mu_1} + \frac{h_2}{\mu_2}$$

Shift 
$$\Rightarrow (h_1 + h_2) - \left(\frac{h_1}{\mu_1} + \frac{h_2}{\mu_2}\right)$$

$$\Rightarrow h_1 \left( 1 - \frac{1}{\mu_1} \right) + h_2 \left( 1 - \frac{1}{\mu_2} \right)$$

47. A metal rod of Young's modulus Y and coefficient of thermal expansion α is held at its two ends such that its length remains invariant. If its temperature is raised by t°C, the linear stress developed in it is:

(1) 
$$\frac{Y}{\alpha t}$$

(3) 
$$\frac{1}{(Y\alpha t)}$$

(4) 
$$\alpha t/\gamma$$

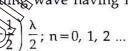
**Ans.[2]** 

**Sol.** 
$$Y = \frac{Stress}{Strain}$$

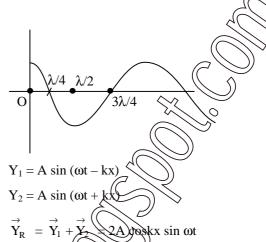
Strain = 
$$\frac{\Delta L}{L} = \frac{L\alpha\Delta t}{L} = \alpha t$$

$$Stress = Y \alpha t$$

- 48. A travelling wave represented by  $y = A \sin(\omega t kx)$  is superimposed on another wave represented by  $y = A \sin(\omega t + kx)$ . The resultants:
  - (1) A wave travelling along +x direction.
  - (2) A wave travelling along -x direction.
  - (3) A standing wave having nodes at  $x = \frac{n\lambda}{2}$   $x = 0, 1, 2 \dots$
  - (4) A standing wave having nodes at



Sol.



So, nodes will be at 
$$\frac{\lambda}{\lambda}$$
,  $\frac{3\lambda}{\lambda}$ ,  $\frac{5\lambda}{\lambda}$ .....

49. A thin circular disk of radius R is uniformly charged with density  $\sigma > 0$  per unit area. The disk rotates about its axis with a uniform angular speed  $\omega$ . The magnetic milment of the disk is:

$$(1)$$
  $\pi R^4 \sigma \omega$ 

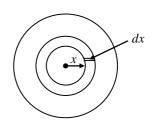
(2) 
$$\frac{\pi R^4}{2} \sigma \omega$$

(3) 
$$\frac{\pi R^4}{4} \sigma \omega$$

(4) 
$$2\pi R^4 \sigma \omega$$

**Ans.**[3]

Sol.



$$M = i \times A = \frac{q}{T} \times \pi R^2$$

$$dM = \frac{dq}{T} \times \pi x^2$$

$$= \frac{\sigma \times dA}{T} \times \pi x^2$$

$$d\mathbf{M} = \frac{\mathbf{\sigma} \times 2\pi x \, dx \times \pi x^2}{2\pi} \mathbf{\omega}$$

$$M = \sigma \times \omega \int x^3 dx$$

$$= \sigma \times \omega \times \left(\frac{x^4}{4}\right)_0^R = \frac{\sigma \times \omega R^4}{4}$$

- 50. An aluminium sphere of 20 cm diameter is heated from 0°C to 100°C. Its volume changes by (given that coefficient of linear expansion for aluminium  $\alpha_{Al} = 23 \times 10^{-6}/^{\circ}\text{C}$ ):
  - (1) 2.89 cc
  - (2) 9.28 cc
  - (3) 49.8 cc
  - (4) 28.9 cc

# Ans.[4]

**Sol.** 
$$\gamma = 3\alpha = 3 \times 23 \times 10^{-6} = 69 \times 10^{-6} / ^{\circ}\text{C}$$

$$V = \frac{4}{3}\pi r^{3} = \frac{4}{3}\pi \times (10 \times 10^{-2})^{3}$$
$$= \frac{4}{3} \times \pi \times 10^{-3}$$

Change in volume  $(\Delta V)$ 

$$V'-V=V\gamma\Delta t$$

$$= \left(\frac{4}{3}\pi R^3 \times 69 \times 10^{-6}\right) \times (100 - 0)$$

51. Two mercury drops (each of radius r)
merge to form a bigger drop. The surface
energy of the bigger drop, if T is the surface
tension, is:

- (i) in T
- (2)  $2\pi r^2 T$
- (3)  $2^{\frac{8}{3}} \pi r^2 T$
- (4)  $2^{\frac{5}{3}} \pi r^2 T_3$

Ans.[3]

Sol. Volume of big drop = total volume of small drops  $R = 2^{1/3}r$ 

Surface energy of small drops  $U = 2T 4\pi r^2$ 

Surface energy of big drop

 $V_{\perp} = T4\pi R^2$ 

$$T 4\pi (2^{1/3})^2 r^2$$

$$= T 4\pi(2)^{2/3} r^2$$

$$U' = T(2)^{2}\pi 2^{2/3} r^{2}$$

$$U' = T(2)^{8/3} \pi r^{2}$$

52. If a ball of steel (density  $\rho = 7.8 \text{ g cm}^{-3}$ ) attains a terminal velocity of 10 cm s<sup>-1</sup> when falling in a tank of water (coefficient of viscosity  $\eta_{\text{water}} = 8.5 \times 10^{-4} \text{ Pa.s}$ ) then its terminal velocity in glycerine ( $\rho = 1.2 \text{ g cm}^{-3}$ ,  $\eta = 13.2 \text{ Pa.s}$ ) would be, nearly:

- (1)  $6.25 \times 10^{-4}$  cm s<sup>-1</sup>
- (2)  $6.45 \times 10^{-4}$  cm s<sup>-1</sup>
- (3)  $1.5 \times 10^{-5}$  cm s<sup>-1</sup>
- (4)  $1.6 \times 10^{-5}$  cm s<sup>-1</sup>

Ans.[1]

**Sol.** 
$$V = \frac{2r^2}{9\eta} g\{d_b - d_\ell\}$$

$$\frac{V_1}{V_2} = \frac{\eta_2}{\eta_1} \left\{ \frac{d - d_1}{d - d_2} \right\}$$

$$\frac{10}{V} = \frac{13.2}{8.5 \times 10^{-4}} \left\{ \frac{7.8 - 1}{7.8 - 1.2} \right\}$$

$$V = 6.25 \times 10^{-4} \text{ cm/s}$$

- A horizontal straight wire 20 m long 53. extending from east to west is falling with a speed of 5.0 m/s, at right angles to the horizontal component of the earth's magnetic field  $0.30 \times 10^{-4}$  Wb/m<sup>2</sup>. The instantaneous value of the e.m.f induced in the wire will be:
  - (1) 3 mV
  - (2)4.5 mV
  - (3)1.5 mV
  - 6.0 mV (4)

#### Ans.[1]

**Sol.** 
$$e = B \times v \times \ell$$

$$= 0.30 \times 10^{-4} \times 5 \times 20$$

- After absorbing a slowly moving neutron 54. of mass m<sub>N</sub> (momentum 70) a nucleus of mass M breaks into two nuclei of masses  $m_1$  and  $5 m_1$  (6  $m_1 = M + m_1$ ) respectively. If the de Broglie wavelength of the nucleus with mass m1 (is the de Broglie wavelength of the other nucleus will be:
  - (1)

- Sol. Acceleration to momentum conservation, linear momentum of both point is wavelength is also same.
- Which of the following four alternatives is 55. not correct?

We need modulation:

- to reduce the time lag between transmission and reception of the information signal
- to reduce the size of antenna (2)
- to reduce the fractional band width, (3)that is the ratio of the signal band width to the centre frequency
- to increase the selectivity.

**Ans.**[1]

Sol. Time is not dependent on modulation.

- If a spring of stiffness 'k' is cut into two parts 'A' and 'B' of length  $l_A: l_B = 2:3$ , then the stiffness of spring 'A' is given by:
  - (1)

  - (3)
  - 5/2 k

# Ans.[4] Sol.

$$\ell = \ell_{A} + \ell_{B}$$

$$\frac{\ell - \ell_A + \ell}{\ell_A} = \frac{2}{2}$$

$$K \propto \frac{1}{\ell}$$

... (1)

... (2)

$$K_A \propto \frac{1}{\ell_A}$$

From (2)/(1)

$$\begin{split} \frac{K_A}{K} &= \frac{\ell}{\ell_A} \\ K_A &= \frac{K\{\ell_A + \ell_B\}}{\ell_A} \\ K_A &= K\left\{1 + \frac{\ell_B}{\ell_A}\right\} \\ K_A &= K\left\{1 + \frac{3}{2}\right\} \\ K_A &= \frac{5K}{2} \end{split}$$

# 57. Statement - 1:

A nucleus having energy  $E_1$  decays by  $\beta^-$  emission to daughter nucleus having energy  $E_2$  but the  $\beta^-$  rays are emitted with a continuous energy spectrum having end point energy  $E_1-E_2$ .

### Statement - 2:

To conserve energy and momentum in  $\beta$ -decay at least three particles must take part in the transformation.

- (1) Statement-1 is correct but statement-2 is not correct.
- (2) Statement -1 and statement -2 both are correct and statement 2 is the correct explanation of statement-1.
- (3) Statement-1 is correct statement-2 is correct and statement 2 is not the correct explanation of statement-1.
- (4) Statement-1 is incorrect, statement-2 is correct.

Ans.[2]

Sol. Maximum energy = End point energy  $= E_1 - E_2$ Three particles at least required  $0 + \frac{1}{v} + \frac{1}{v} = e^0 + \overline{v}$ 

$$_{1}p^{1} \rightarrow _{0}n^{1} +_{+1}e^{0} + v$$

- 58. When monochromatic red light is used instead of blue light in a convex lens, its focal length will:
  - (1) increase
  - (2) decrease
  - (3) remain same
  - (4) does not depend on colour of light.

**Ans.[1]** 

Sol.  $\frac{1}{f} = (\mu)$ 

so increases.

59. Statement - 1:

On viewing the clear blue portion of the sky through a Calcite Crystal, the intensity of transmitted light varies as the crystal is rotated.

#### Statement - 2:

The light coming from the sky is polarized due to scattering of sun light by particles in the atmosphere. The scattering is largest for blue light.

- (1) Statement 1 is true, statement 2 is
- (2) Statement 1 is true, statement 2 is true, statement 2 is the correct explanation of statement 1.
- (3) Statement 1 is true, statement 2 is true; statement 2 is not the correct explanation of statement 1.
- (4) Statement 1 is false, Statement 2 is true.

**Ans.**[2]

Sol. Statement-I → Polarisation
Statement-II → Raylegh's criteria

$$Statement\text{-}II \rightarrow Raylegh\text{'s criteria}$$

Scattering 
$$\propto \frac{1}{\lambda^4}$$

So statement I and II both correct statement-II is the correct explanation of statement-I.

# 60. Statement - 1:

Two longitudinal waves given by equations:  $y_1(x, t) = 2a \sin(\omega t - kx)$  and  $y_2(x, t) = a \sin(2\omega t - 2kx)$  will have equal intensity.

# Statements - 2:

Intensity of waves of given frequency in same medium is proportional to square of amplitude only.

- (1) Statement 1 is true, statement 2 is false.
- (2) Statement 1 is true, statement 2 true; statement 2 is the correct explanation of statement 1
- (3) Statement 1 is true, statement 2 is true; statement 2 is not correct explanation of statement 1.
- (4) Statement 1 is false, statement 21s true.



**Sol.**  $a_1 = 2a, a_2 = a$ 

$$\omega_1 = \omega$$
,  $\omega_2 = 2\omega$ 

$$I \propto a^2 n^2$$
 (for same medium)

So 
$$I_1 = I_2$$
 statement-I (True)

Statement-II

 $n \rightarrow constant$ 

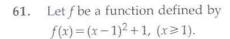
$$I \propto a^2$$

$$I = ka^2$$
 (statement - H- True)

But no correct explanation, because of



# PART C - MATHEMATICS



# Statement - 1:

The set  $\{x : f(x) = f^{-1}(x)\} = \{1, 2\}.$ 

#### Statement - 2:

f is a bijection and  $f^{-1}(x) = 1 + \sqrt{x-1}$ ,  $x \ge 1$ .

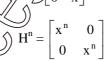
- Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for statement-1.
- Statement-1 is true, statement-2 is true; statement-2 is not a correct explanation for statement-1.
- Statement-1 is true, statement-2 is
- Statement-1 is false, statement-2 is true.

# (1)

to:

0

- Sol. is scalar matrix



$$\Rightarrow H^{70} = \begin{bmatrix} \omega^{70} & 0 \\ 0 & \omega^{70} \end{bmatrix} = \begin{bmatrix} \omega & 0 \\ 0 & \omega \end{bmatrix} = H$$

If  $\omega \neq 1$  is the complex cube roof of up

and matrix  $H = \begin{bmatrix} \omega & 0 \\ 0 & \omega \end{bmatrix}$ , then  $H^{70}$  in equal

[2]  $f(x) = (x - 1)^2 + 1 = y$ 

Sol.

$$f(x) = (x - 1)^2 + 1 = y$$

$$(x-1)^2 = y-1$$

$$x - 1 = \pm \sqrt{y - 1}$$

$$x = 1 \pm \sqrt{y-1}$$

$$f^{-1}(y) = 1 \pm \sqrt{y-1}$$

$$f^{-1}(y) = 1 + \sqrt{y}$$
:  $y \ge 1$ 

Statement 24s true

$$f(x) = f^{-1}(x)$$

$$(x-1)^2 + 1 + \sqrt{x-1}$$

atement -1 is true

Noting these we get x = 1, 2

Let [·] denote the greatest integer function

then the value of  $\int_{0}^{1.5} x \left[ x^{2} \right] dx$  is:

- (1)
- (2)
- (3)
- Sol.

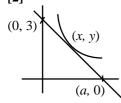
$$\int_{0}^{1.5} x[x^{2}]dx = \int_{0}^{1} 0 \ dx + \int_{1}^{\sqrt{2}} x \ dx + \int_{\sqrt{2}}^{1.5} 2x \ dx$$

$$= 0 + \left(\frac{x^2}{2}\right)_1^{\sqrt{2}} + \left(x^2\right)_{\sqrt{2}}^{1.5}$$
$$= \left(1 - \frac{1}{2}\right) + (2.25 - 2) = \frac{3}{4}$$

- The curve that passes through the point (2, 3), and has the property that the segment of any tangent to it lying between the coordinate axes is bisected by the point of contact, is given by:
  - (1) 2y 3x = 0

  - (3)  $x^2 + y^2 = 13$
  - (4)  $\left(\frac{x}{2}\right)^2 + \left(\frac{y}{3}\right)^2 = 2$

Sol.



$$x = \frac{a}{2}, \ y = \frac{b}{2}$$

$$\Rightarrow a = 2x \quad b = 2y$$

& 
$$\frac{dy}{dx} = \frac{-b}{a}$$

$$\Rightarrow \frac{dy}{dx} = \frac{-y}{x} \Rightarrow \frac{dy}{y} = \frac{dx}{x}$$

$$\Rightarrow \int \frac{dy}{y} = -\int \frac{dx}{x}$$

$$\Rightarrow \log y = -\log x + \log g \Rightarrow xy = 0$$

- : it passes through (2,5)
- $\therefore c = 6$   $\therefore \text{ equation of curve is } xy = 6$

- 65. A scientist is weighing each of 30 fisher Their mean weight worked out is and a standard deviation of 2 gm Date it was found that the measuring sca misaligned and always under reported every fish weight by 2 gm. The correct mean and standard deviation (in gm) of fishes are respectively
  - 32, 2
  - (2)32, 4
  - 28, 2 (3)
  - (4)

Sol.  $[1]_{^{\triangleright}}$ 

> There is no change in mean deviation if each observation increased by a constant number while mean increased by that constant number

Hence

$$M. = 30 + 2 = 32$$

$$M.D. = 2$$

The lines x + y = |a| and ax - y = 1 intersect each other in the first quadrant. Then the set of all possible values of a is the interval:

- $(0, \infty)$
- (2) $[1, \infty)$
- $(-1, \infty)$
- (-1, 1]

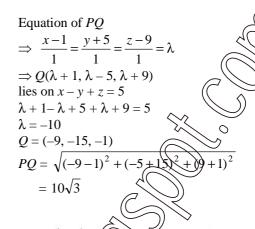
Sol.

$$x + y = \pm a ax - y = 1 (1 + a)x = |a| + 1 x = \frac{|a| + 1}{1 + a} x = \frac{a |a| + 1}{1 + a} x = \frac{a |a| - 1}{1 + a}$$

$$\frac{|a|+1}{1+a} > 0, \qquad \frac{a|a|-1}{1+a} > 0$$

$$\Rightarrow a > 1$$

- 67. If the vectors  $p\hat{i} + \hat{j} + \hat{k}$ ,  $\hat{i} + q\hat{j} + \hat{k}$  and  $\hat{i} + \hat{j} + r\hat{k}$   $(p \neq q \neq r \neq 1)$  are coplanar, then the value of pqr (p + q + r) is :
  - (1) 2
  - (2) 0
  - (3) -1
  - (4) 2
- Sol. [4]  $\begin{vmatrix} p & 1 & 1 \\ 1 & q & 1 \\ 1 & 1 & r \end{vmatrix} = 0$  p(qr-1) - 1 (r-1) + 1 (1-q) = 0 pqr - p - r + 1 + 1 - q = 0 pqr - (p + q + r) + 2 = 0
- 68. The distance of the point (1, -5, 9) for the plane x y + z = 5 measured straight line x = y = z is :
  - $(1) 10\sqrt{3}$
  - (2)  $5\sqrt{3}$
  - (3)  $3\sqrt{10}$
  - (4)  $3\sqrt{5}$
- Sol. [1]



- 69. Let a, b, c be three non-zero vectors which are pairwise non-collinear. If  $\vec{a} + 3\vec{b}$  is collinear with  $\vec{c}$  and  $\vec{b} + 2\vec{c}$ :
  - (Cottinear with  $\overrightarrow{a}$ , then  $\overrightarrow{a} + 3\overrightarrow{b} + 6\overrightarrow{c}$
  - (2) c
  - (3)  $\overset{\rightarrow}{0}$
  - $(4) \quad \stackrel{\rightarrow}{a} + \stackrel{\rightarrow}{c}$
- Sol. [3]  $\vec{a} + 3\vec{b} = \lambda \vec{c}$   $\vec{b} + 2\vec{c} = \mu \vec{a}$   $\vec{b} + 2\vec{c} = \mu(\lambda \vec{c} - 3\vec{b})$   $\vec{b} + 2\vec{c} = \lambda\mu\vec{c} - 3\mu\vec{b}$   $(1 - 3\mu)\vec{b} + (2 - \lambda\mu)\vec{c} = 0$   $1 + 3\mu = 0$   $2 - \lambda\mu = 0$   $\mu = -\frac{1}{3}$   $\lambda\mu = 2$   $\lambda = -6$  $\vec{a} + 3\vec{b} + 6\vec{c} = 0$

- 70. If A(2, -3) and B(-2, 1) are two vertices of a triangle and third vertex moves on the line 2x + 3y = 9, then the locus of the centroid of the triangle is:
  - $(1) \quad x y = 1$
  - (2) 2x + 3y = 1
  - (3) 2x + 3y = 3
  - (4) 2x 3y = 1
- Sol. [2] A(2, -3) B(-2, 1)Centroid, (h, k)Let third vertex is  $(\alpha, \beta)$   $\frac{2-2+\alpha}{3} = h$ ,  $\frac{-3+1+\beta}{3} = k$   $\Rightarrow \alpha = 3h$   $\Rightarrow \beta = 3k + 2$   $\therefore 2\alpha + 3\beta = 9$  2(3h) + 3(3k + 2) = 9 6h + 9k + 6 = 9 6h + 9k = 3 2h + 3k = 1 $\log 2x + 3y = 1$
- 71. There are 10 points in a plane, out of these 6 are collinear. If N is the number of triangles formed by joining these points, then:
  - (1)  $N \le 100$
  - (2)  $100 < N \le 140$
  - (3)  $140 < N \le 190$
  - (4) N>190
- Sol. [1] Max. traingles =  ${}^{6}C_{3} - {}^{6}C_{3}$ = 120 - 20= 100

72. Define F(x) as the product of two real functions  $f_1(x) = x$ ,  $x \in \mathbb{R}$  and

$$f_2(\mathbf{x}) = \begin{cases} \sin\frac{1}{x}, & \text{if } x \neq 0\\ 0, & \text{if } x = 0 \end{cases}$$

as follows:

$$F(x) = \begin{cases} f_1(x) & \text{if } x \neq 0 \\ & \text{if } x = 0 \end{cases}$$

Statement 1:

F(x) is continuous on  $\mathbb{R}$ .

statement - 2 :

 $f_1(x)$  and  $f_2(x)$  are continuous on IR.

- Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for statement-1.
- (2) Statement-1 is true, statement-2 is true; statement-2 is not a correct explanation for statement-1.
- (3) Statement-1 is true, statement 2 is false.
- (4) Statement-1 is false, statement-2 is true.

 $f_1(x) = x$  is continuous every R

& 
$$f_2(x) = \begin{cases} \sin\frac{1}{x}; & x \neq 0 \\ 0 & x = 0 \end{cases}$$
 is discontinuous at  $x = 0$ 

 $\Rightarrow$  product of f<sub>1</sub>(x) and f<sub>2</sub>(x) is continuous

:. St. (1) is correct and (2) is false

### 73. Statement - 1:

For each natural number n,  $(n+1)^7 - n^7 - 1$  is divisible by 7.

### Statement - 2:

For each natural number n,  $n^7 - n$  is divisible by 7.

- (1) Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for statement-1.
- (2) Statement-1 is true, statement-2 is true; statement-2 is *not* a correct explanation for statement-1.
- (3) Statement-1 is true, statement-2 is false.
- (4) Statement-1 is false, statement true.

# Sol. [1]

By induction, to proof

 $S(n) = n^7 - n$  is divisible by 5

Let 
$$n = 1$$

$$S(n = 1) = 1^7 - 1 = 0$$

Hence it is true for n

Let the statement is true for n = k

 $\Rightarrow$  P(n = k)  $\Rightarrow$  R k is divisible by 7.

$$\Rightarrow k^7 - k = 7$$

Now to proof the statement is true for n = k + 1

$$\Rightarrow$$
 P( $k + 1$ )  $\Rightarrow$   $(k + 1)^7 - (k + 1)$  is

divisishte by 7

$${}^{7}C_{1}k + {}^{7}C_{2}k^{2} + \dots + {}^{7}C_{6}k^{6} + k^{7}] - k - 1$$

$$=7.\lambda + (k^7 - k)$$

$$=7\lambda+7\lambda'=7.(\lambda+\lambda')$$

which is divisible by 7.

.. Statement - 2 is true

Statement -1

 $n^7 - n$  is divisible by 7

 $\Rightarrow$  use it put n = n + 1

$$(n+1)^7 - (n+1) = 72$$

$$\Rightarrow [(n+1)^7 - n^7 + 1 + (n^7) - n) = 7\lambda$$

= Stanement -1 \ 7λ

statement-1 is true and statement-2 is also correct explanation of Statement -1.

74. The equation of the circle passing through the points (1, 0) and (0, 1) and having the small st radius is:

$$(1) x^2 + y^2 - 2x - 2y + 1 = 0$$

(2) 
$$x^2 + y^2 - x - y = 0$$

(3) 
$$x^2 + y^2 + 2x + 2y - 7 = 0$$

(4) 
$$x^2 + y^2 + x + y - 2 = 0$$

# Sol. [2]

Points will be end of diameter (x-1)(x-0) + (y-0)(y-1) = 0

$$x^2 + y^2 - x - y = 0$$

75. The equation of the hyperbola whose foci are (−2, 0) and (2, 0) and eccentricity is 2 is given by:

$$(1) \quad x^2 - 3y^2 = 3$$

$$(2) \quad 3x^2 - y^2 = 3$$

$$(3) \quad -x^2 + 3y^2 = 3$$

$$(4) \qquad -3x^2 + y^2 = 3$$

Sol.

$$ae = 2$$

$$e = 2$$

$$a = 1$$

$$e^{2} = 1 + \frac{b^{2}}{a^{2}}$$

$$4 = 1 + b^{2}$$

$$b^{2} = 3$$

$$\frac{x^{2}}{1} - \frac{y^{2}}{3} = 1$$

**76.** If the trivial solution is the only solution of the system of equations

$$x - ky + z = 0$$

$$kx + 3y - kz = 0$$

$$3x + y - z = 0$$

then the set of all values of k is :

- (1)  $R \{2, -3\}$
- (2) R  $\{2\}$
- (3)  $R \{-3\}$
- (4) {2, -3}
- Sol. [1]

 $\Delta \neq 0$  for trivial solution.

$$\begin{vmatrix} 1 & -k & 1 \\ k & 3 & -k \\ 3 & 1 & -1 \end{vmatrix} \neq 0$$

$$k^2 + k - 6 \neq 0$$

$$k \in R - \{-3, ($$

77. Sachin and Rahul attempted to solve a quadratic equation. Sachin make a mistake in writing down the constant form and ended up in roots (4, 3). I fahul made a mistake in writing down coefficient of x to get roots (3, 2). The correct Poots of equation are:

- (1) 6, 1
- (2) 4, 3
- (3) -6
- (4) -4
- Sol.

Let quadratic equation be

$$\int_{0}^{2} 4bx + c = 0$$

$$+\beta = 4 + 3 = 7 = -b$$

$$b = -7$$

$$\alpha$$
 .  $\beta=3.2=6=c$ 

:. correct quadratic equation

$$x^2 - 7x + 6 = 0$$

$$(x-1)(x-6)=0$$

$$x = 1, 6$$

78. Let  $a_n$  be the  $n^{th}$  term of an A.P. If  $\sum_{r=1}^{100} a_{2r} = \alpha \text{ and } \sum_{r=1}^{100} a_{2r-1} = \beta \text{, then the}$ 

common difference of the A.P. is:

- (1)  $\alpha \beta$
- $(2) \qquad \frac{\alpha \beta}{100}$
- (3)  $\beta \alpha$
- $(4) \qquad \frac{\alpha \beta}{200}$
- Sol. [2]

$$\sum_{r=1}^{100} a_{2r} = \alpha$$

$$\sum_{r=1}^{100} a_{2r-1} + d = \alpha$$

$$\sum_{r=1}^{100} a_{2r-1} + \sum_{r=1}^{100} d = \alpha$$

$$\beta + 100d = \alpha$$

$$d = \frac{\alpha - \beta}{100}$$

79. Consider the differential equat

$$y^2 dx + \left(x - \frac{1}{y}\right) dy = 0$$
. If  $y(1) = 1$ 

is given by:

(1) 
$$4 - \frac{2}{y} - \frac{e^{\frac{1}{y}}}{e}$$

(2)

$$\frac{1}{y} - \frac{1}{e^y}$$

(4) 
$$1 - \frac{1}{y} + \frac{e^{\frac{1}{y}}}{e}$$

[3]

$$\frac{dy}{dx} = -\frac{y^2}{x - \frac{1}{y}}$$

$$\frac{dx}{dy} = -\frac{x - \frac{1}{y}}{y^2}$$

$$\frac{dx}{dy} + \frac{x}{y^2} = \frac{1}{y^3}$$

I.F. = 
$$e^{\int \frac{1}{y^2} dy} = e^{-\frac{1}{y}}$$

$$x \cdot e^{-1/y} = \int \frac{1}{y^3} \cdot e^{-1/y} dy$$
$$= -\int_{I} t \cdot e_{II}^t dt \qquad t = -\frac{1}{y}$$
$$= -\left\{ e^t - \int 1 \cdot e^t dt \right\}$$

$$xe^{-1/y} = -te^t + e^t + e^t$$

$$xe^{-1/y} = +\frac{1}{y}e^{-1/y} + e^{-1/y} + c$$

$$x = \frac{1}{y} + 1 + ce^{1/y}$$

at 
$$x = 1$$
,  $y = 1$   $1 = 2 + ce^{1}$ 

$$c = -1/e$$

$$x = \frac{1}{y} + 1 - \frac{1}{e}e^{1/y}$$

**80.** Let 
$$f: \mathbb{R} \to [0, \infty)$$
 be such that  $\lim_{x \to 5} f(x)$ 

exists and 
$$\lim_{x \to 5} \frac{(f(x))^2 - 9}{\sqrt{|x - 5|}} = 0.$$

Then  $\lim_{x \to 5} f(x)$  equals:

- (1) 0
- (2) 1
- (3) 2
- (4) 3

# Sol. [4

$$\lim_{x \to 5} \frac{(f(x))^2 - 9}{\sqrt{|x - 5|}} = 0$$

Limit can be zero only when

$$\lim_{x \to 5} f(x) = 3$$

### 81. Statement - 1:

Determinant of a skew-symmetric of order 3 is zero.

### Statement - 2:

For any matrix A,  $det(A^T) = det(A)$  and det(-A) = -det(A)

Where det(B) denotes the determinant of matrix B. Then:

- (1) Both statements are true.
- (2) Both statements are false.

Statement-1 is false and statement-2 s true.

Statement-1 is true and statement-2 is false.

# [4]

Statement-1 is true

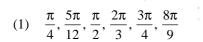
Statement-2 is false

$$|A'| = |A| \Rightarrow \text{true}$$

$$|-A| = (-1)^n |A| \Rightarrow \text{false}$$

Statement-2 is false

82. The possible values of  $\theta' \in (0, \pi)$  such that  $\sin(\theta) + \sin(4\theta) + \sin(7\theta) = 0$  are :



(2) 
$$\frac{2\pi}{9}$$
,  $\frac{\pi}{4}$ ,  $\frac{\pi}{2}$ ,  $\frac{2\pi}{3}$ ,  $\frac{3\pi}{4}$ ,  $\frac{35\pi}{36}$ 

(3) 
$$\frac{2\pi}{9}$$
,  $\frac{\pi}{4}$ ,  $\frac{\pi}{2}$ ,  $\frac{2\pi}{3}$ ,  $\frac{3\pi}{4}$ ,  $\frac{8\pi}{9}$ 

$$(4) \quad \frac{2\pi}{9}, \frac{\pi}{4}, \frac{4\pi}{9}, \frac{\pi}{2}, \frac{3\pi}{4}, \frac{8\pi}{9}$$

**Sol.** [4]

$$2\sin 4\theta\cos 3\theta + \sin 4\theta = 0$$

$$\sin 4\theta (2\cos 3\theta + 1) = 0$$

$$\sin 4\theta = 0$$

$$\cos 3\theta = -$$

$$\theta = \frac{n\pi}{4}$$

$$\frac{2\pi}{2\pi}$$

### Put $n \in I$

$$\theta = \frac{\pi}{4}, \frac{\pi}{2}, \frac{3\pi}{4}, \frac{2\pi}{9}$$



(1) 
$$\frac{32}{3}$$

(2) 
$$\frac{16}{3}$$



**Sol.** 
$$y^2 = 4ax & x^2 = 4by$$

Area bounded by these curve is 
$$\frac{16ab}{3}$$

here 
$$a = b = 1$$

$$\therefore A = \frac{16}{3}$$

84. Let f be a function defined by

$$f(x) = \begin{cases} \frac{\tan x}{x}, & x \neq 0 \\ 1, & x = 0 \end{cases}$$

### Statement - 1:

x = 0 is point of minima of f.

### Statement - 2:

f'(0) = 0.

- (1) Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for statement-1.
- (2) Statement-1 is true, statement-2 is true; statement-2 is *not* a correct explanation for statement-1.
- (3) Statement-1 is true, statement-2 is false.
- (4) Statement-1 is false, statement true.
- **Sol.** [2]

Since we know in neighbourhood of x = 0

$$\frac{\tan x}{x} > 1 \& f(0) = 1$$

 $\therefore x = 0$  is point of minima

& 
$$f'(a) = \lim_{x \to a} \frac{f(x)}{x}$$

$$\Rightarrow f'(0) = \lim_{x \to 0} \underbrace{\frac{f(0) - f(0)}{x - 0}}_{x \to 0} = \lim_{x \to 0} \underbrace{\frac{\tan x}{x}}_{x}$$

$$\Rightarrow \lim_{x \to 0} \frac{\tan x}{Q_{\mathcal{A}}} = 0$$

 $\therefore$  St. (1) & (2) both correct but (2) is not correct explanation of (1)

- 85. The only statement among the following that is a tautology is:
  - that is a fautology is
  - $(1) \cdot A \wedge (A \vee B)$
  - (2)  $A \lor (A \land B)$
  - $(3) \quad [A \land (A \to B)] \to$
  - $(4) \quad B \to [A \land (A \bigoplus B)]$

Sol.	[3]
~ ~ ~ •	L~ J

					1	
A	В	A ∧ <b>b</b>	$A \vee B$	(A→B)	$[A \land (A \rightarrow B)]$	$S \rightarrow B$
T	T	T	Z/	ケ	T	T
T	F	F\( (c)		F	F	T
F	T	F	T	T	F	T
F	F	F		T	F	T

Hence  $[A \odot (A \rightarrow B)] \rightarrow B$  is tautology

- 86 Let A, B, C be pairwise independent events with P(C)>0 and  $P(A \cap B \cap C)=0$ . Then  $P(A^c \cap B^c \mid C)$  is equal to :
  - $(1) \qquad P(A) P(B^c)$
  - (2)  $P(A^c) + P(B^c)$
  - (3)  $P(A^c) P(B^c)$
  - (4)  $P(A^c) P(B)$

Sol.[4] 
$$P\left(\frac{\overline{A} \cap \overline{B}}{C}\right)$$

$$=\frac{P(\overline{A}\cap\overline{B}\cap C)}{P(C)}$$

$$=\frac{P(C)-P(A\cap C)-P(B\cap C)+P(A\cap B\cap C)}{P(C)}$$

$$= 1 - P(A) - P(B)$$

$$=P(\overline{A})-P(B)$$
 or  $P(\overline{B})-P(A)$ 

87. Let for  $a \neq a_1 \neq 0$ ,  $f(x) = ax^2 + bx + c$ ,  $g(x) = a_1x^2 + b_1x + c_1$ and p(x) = f(x) - g(x).

> If p(x) = 0 only for x = -1 and p(-2) = 2, then the value of p(2) is:

- (1)3
- (2)
- (3) 6
- (4) 18

#### Sol. [4]

$$0 = (a - a_1) - (b - b_1) + (c - c_1) \qquad \dots (1)$$

$$2 = (a - a_1) 4 - (b - b_1) 2 + (c - c_1) \dots (2)$$

$$p(0) = c - c_1 = 2 \Rightarrow :: (x = -1) \text{ is only root}$$

$$\therefore$$
D = 0 of p(x) = 0  $\Rightarrow$  p(-2) = p(0) = c - c<sub>1</sub> = ?

To find 
$$(a - a_1) 4 + 2 (b - b_1) + (c - c_1) = p(2)$$

Let  $a - a_1 = x$  and  $b - b_1 = y$ 

$$\therefore 2x - 2y + 4 = 0$$
 ...(1)

$$4x - 2y + 2 = 2$$
 ...(2)

$$\Rightarrow x = 2, y = 4$$

$$= 8 + 8 + 2 = 18$$

88. The length of the perpendicular drawn from the point (3, -1, 1)the line

$$\frac{x}{2} = \frac{y-2}{3} = \frac{z-3}{4}$$
 is

- (1)
- (3)
- Sol.

P(3, -1, 11)L

$$\frac{x}{2} = \frac{y-2}{3} = \frac{z-3}{4} = \lambda$$

$$Q = (2\lambda, 3\lambda + 2, 4\lambda + 3)$$

D.r<sup>s</sup> of PQ = 
$$2\lambda - 3$$
,  $3\lambda + 3$ 

$$\Rightarrow 2(2\lambda - 3) + 3(3\lambda + 3) + 4(\lambda - 8) = 0$$

$$\Rightarrow 4\lambda - 6 + 9\lambda + 9\lambda + 16\lambda + 32 = 0$$

$$29\lambda = 29 \Rightarrow \lambda \Rightarrow \lambda$$

$$\Rightarrow$$
 Q  $\equiv$  (2, 5, 7)

$$PQ = \sqrt{(3-2)^{2} \pm (-1-5)^{2} + (11-7)^{2}}$$

$$= \sqrt{+36+16}$$

onsider the following relation R on the thor real square matrices of order 3.

> =  $\{(A, B) | A = P^{-1} BP \text{ for some invertible } \}$ matrix P}.

# Statement - 1:

R is an equivalence relation.

#### Statement - 2:

For any two invertible 3×3 matrices M and N,  $(MN)^{-1} = N^{-1}M^{-1}$ .

- Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for statement-1.
- Statement-1 is true, statement-2 is (2) true; statement-2 is not a correct explanation for statement-1.
- Statement-1 is true, statement-2 is (3)
- Statement-1 is false, statement-2 is true.

#### Sol. **[4]**

Statement -1

$$\mathbf{A} = \mathbf{P}^{-1} \mathbf{B} \mathbf{P}$$

$$PA = BP$$

 $P = \{(A, A) \mid PA \neq AP$ general not reflexive. So not equivalence relation.

Statement-2

$$(MN)^{-1} = N^{-1}M^{-1}$$
 True

from defination.

90. If function f(x) is differentiable at x = a

then 
$$\lim_{x \to a} \frac{x^2 f(a) - a^2 f(x)}{x - a}$$
 is:

(1) 
$$-a^2 f'(a)$$

(2) 
$$a f(a) - a^2 f'(a)$$

(3) 
$$2a f(a) - a^2 f'(a)$$

(4) 
$$2a f(a) + a^2 f'(a)$$

### Sol.

$$\lim_{x \to a} \frac{x^2 f(a) - a^2 f(x)}{x - a} \qquad \left(\frac{0}{0} \text{ form}\right)$$

Applying D.L.

$$\lim_{x \to a} 2xf(a) - a^2 f'(x)$$
$$= 2a f(a) - a^2 f'(a)$$

$$x \rightarrow a$$

$$=2a f(a)-a^2 f'(a)$$